

# Exercises: Artificial Intelligence

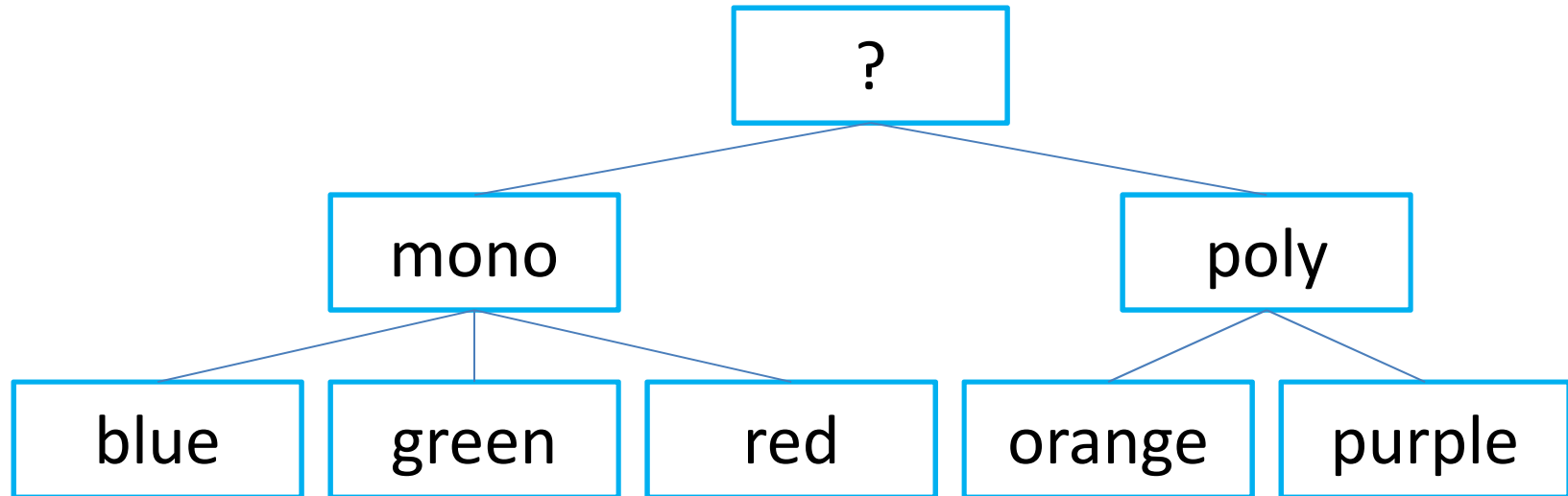
Version Spaces: Colors

Version Spaces: Colors

# PROBLEM

# Problem

- Consider the following concept hierarchy

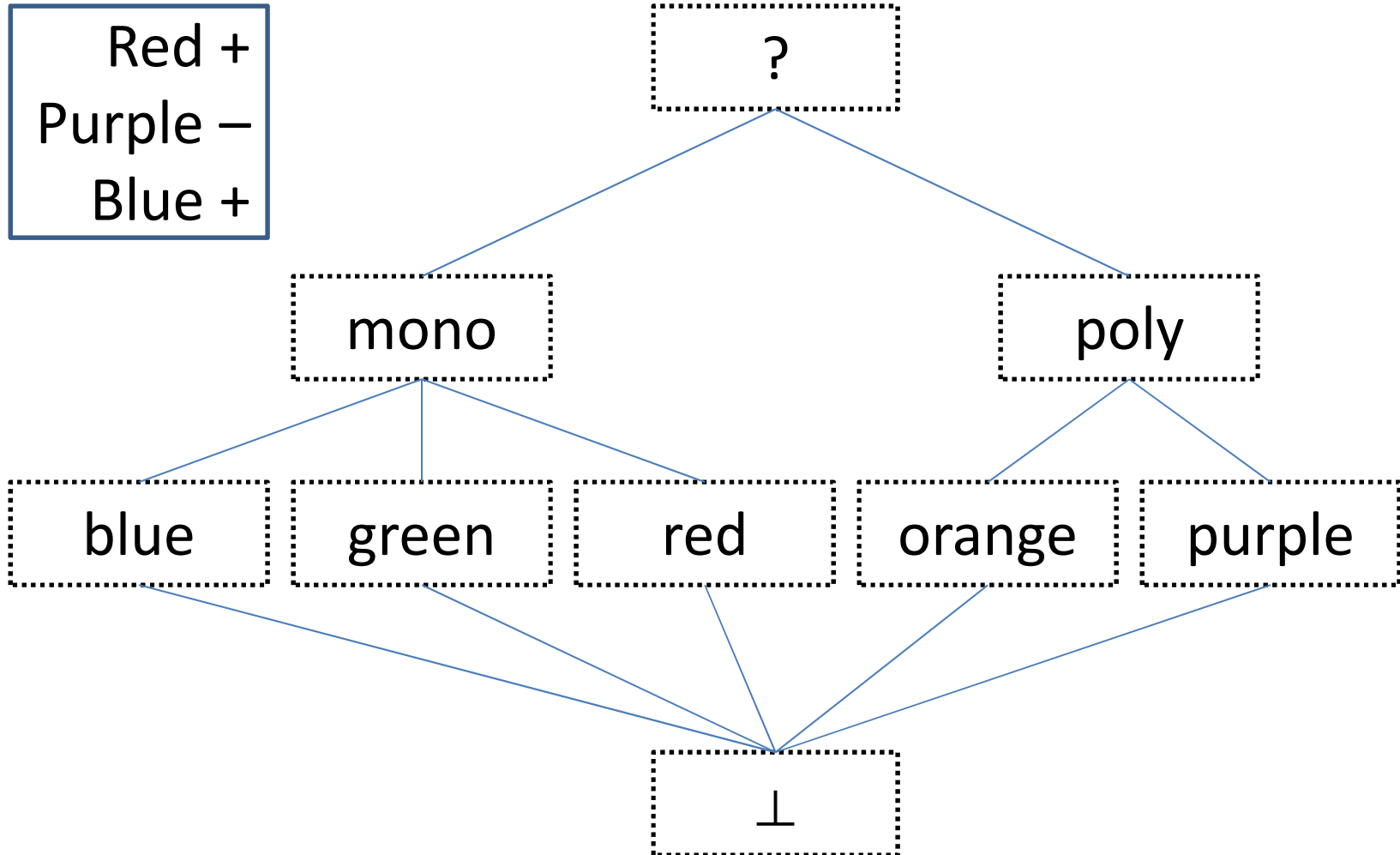


- Apply the Version-Space algorithm on:  
red: +    purple: -    blue: +

Version Spaces: Colors

# **PROBLEM OVERVIEW**

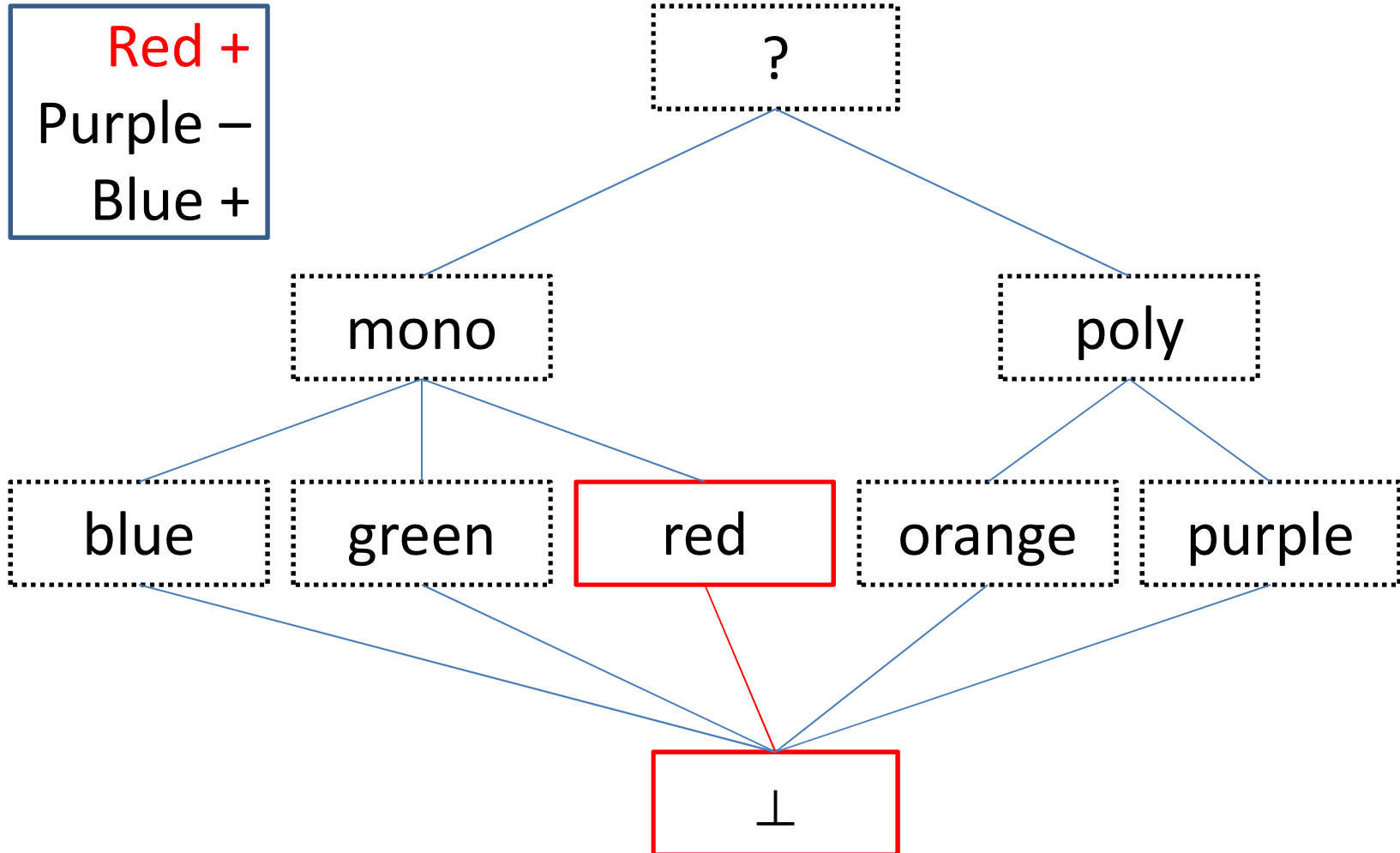
# Problem overview



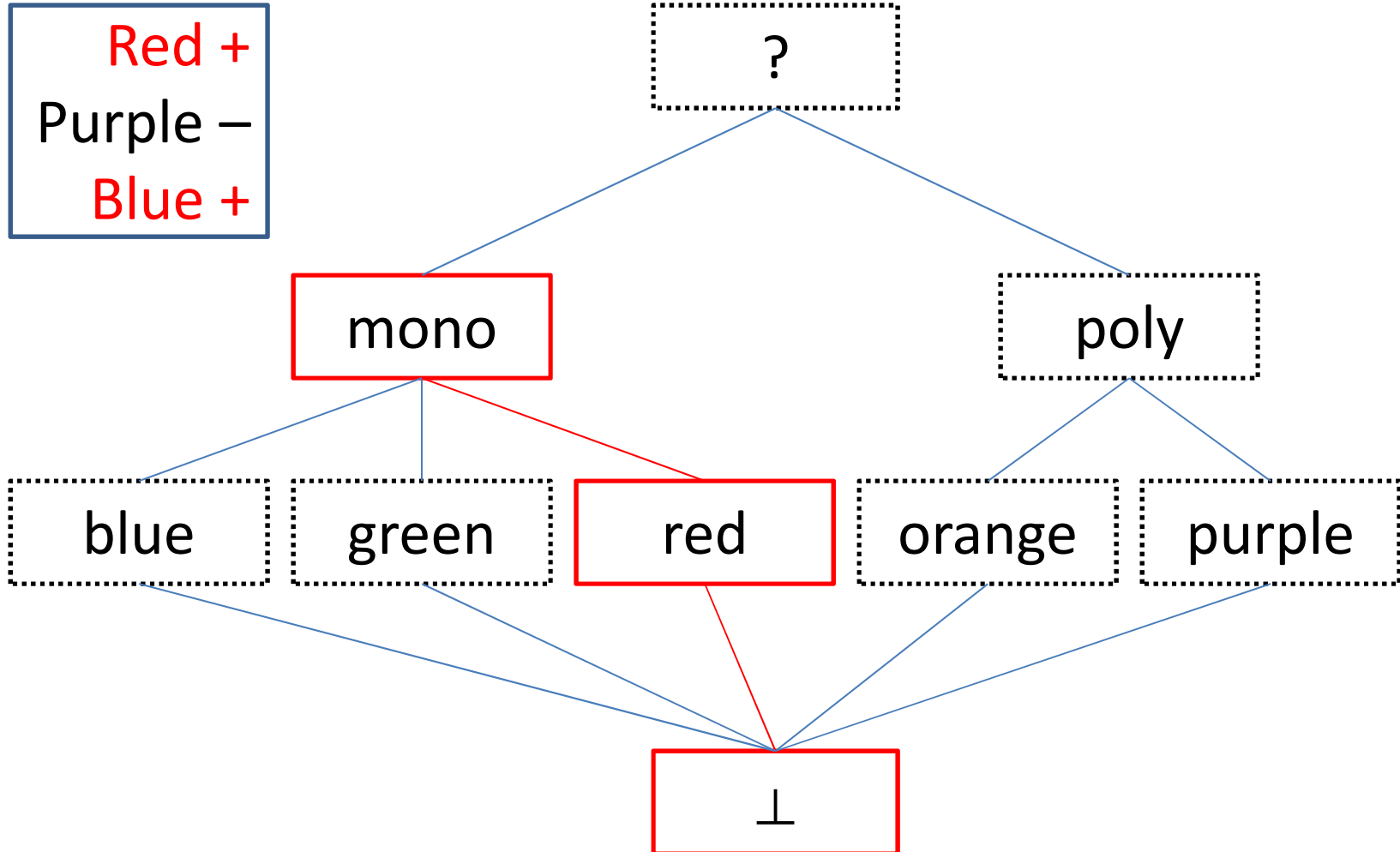
Version Spaces: Colors

# **FIND-S ALGORITHM**

# Find-S Algorithm



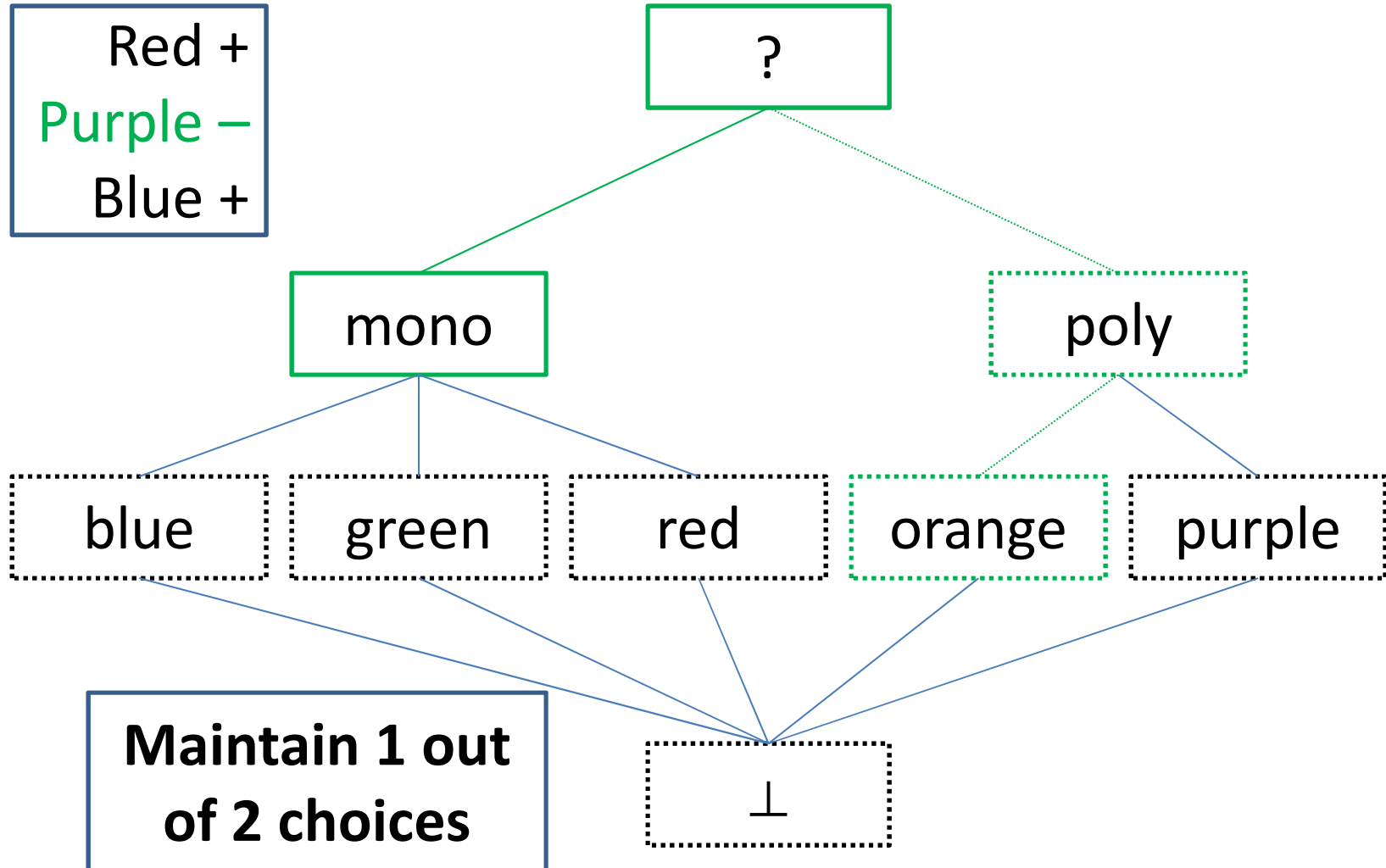
# Find-S Algorithm



Version Spaces: Colors

# **DUAL FIND-S ALGORITHM**

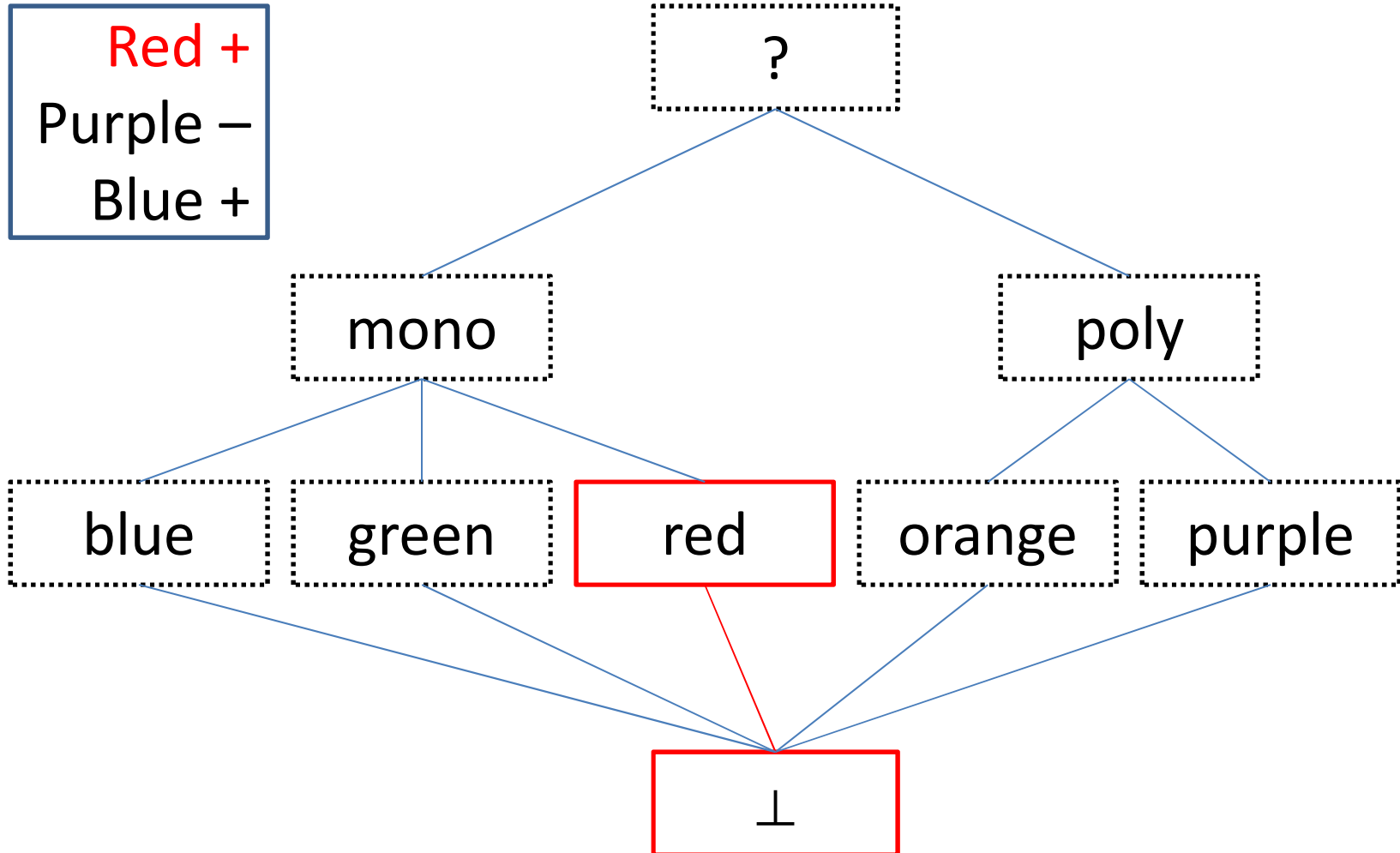
# Dual Find-S Algorithm



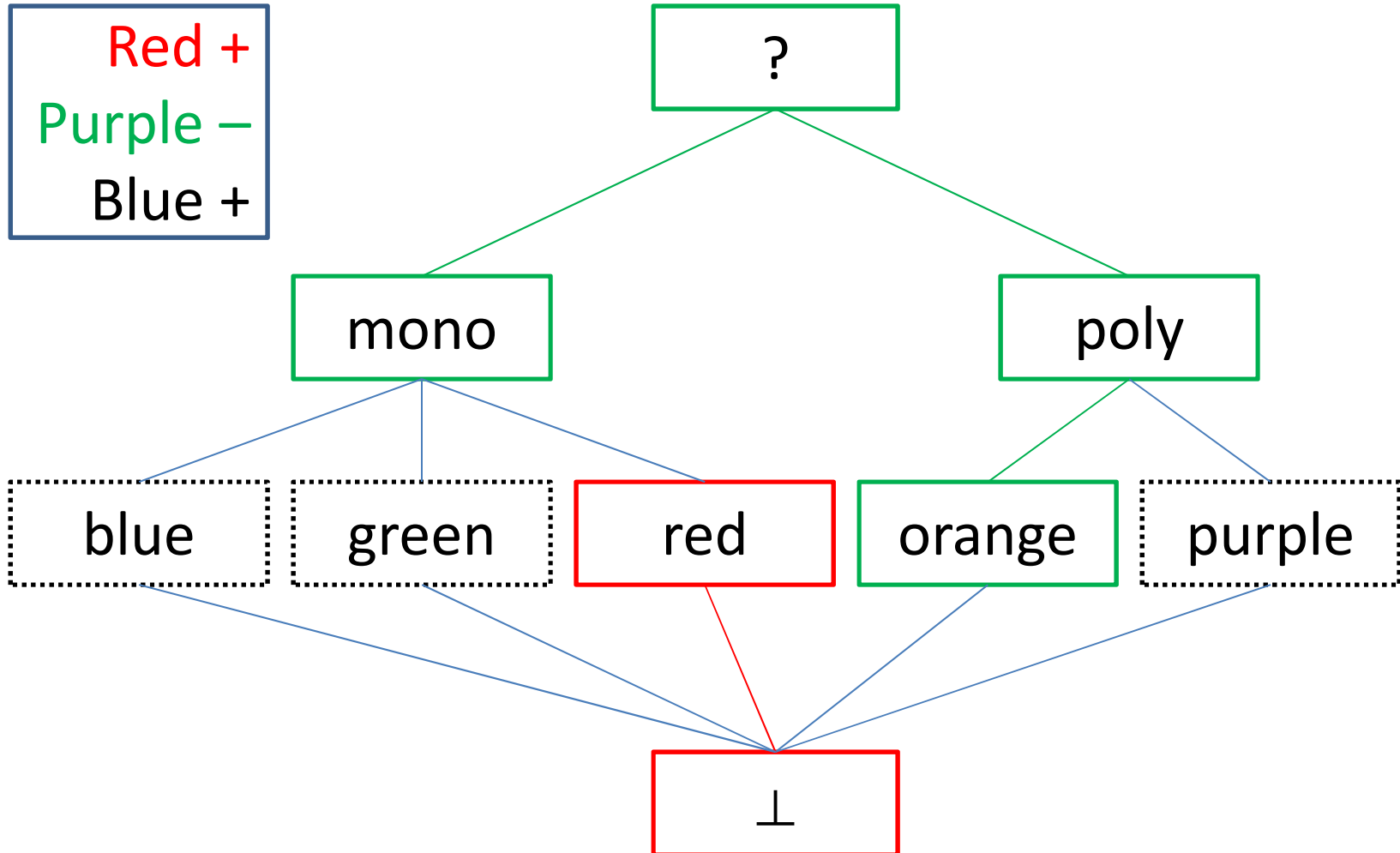
Version Spaces: Colors

# **VERSION-SPACES ALGORITHM**

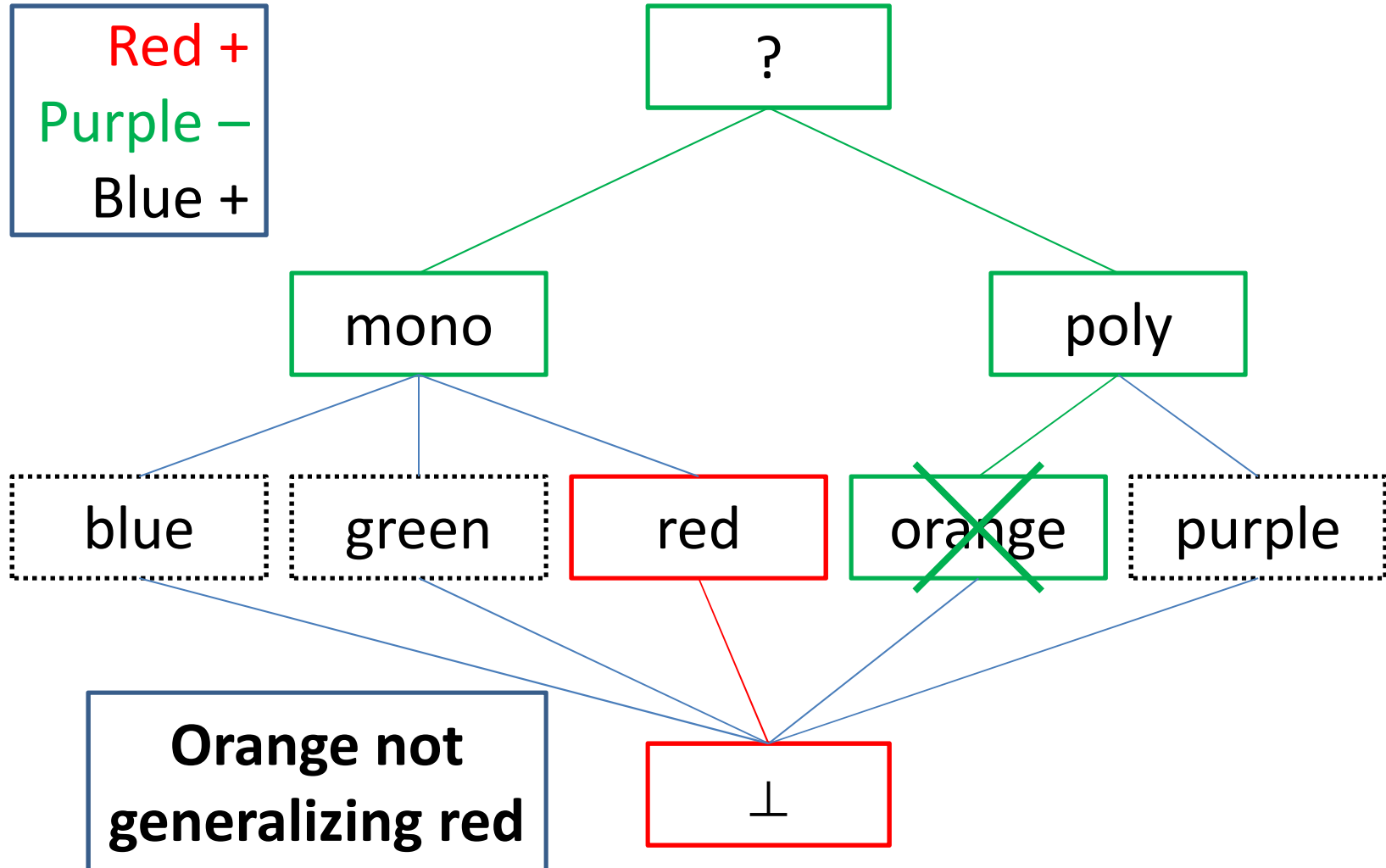
# Version-Spaces Algorithm



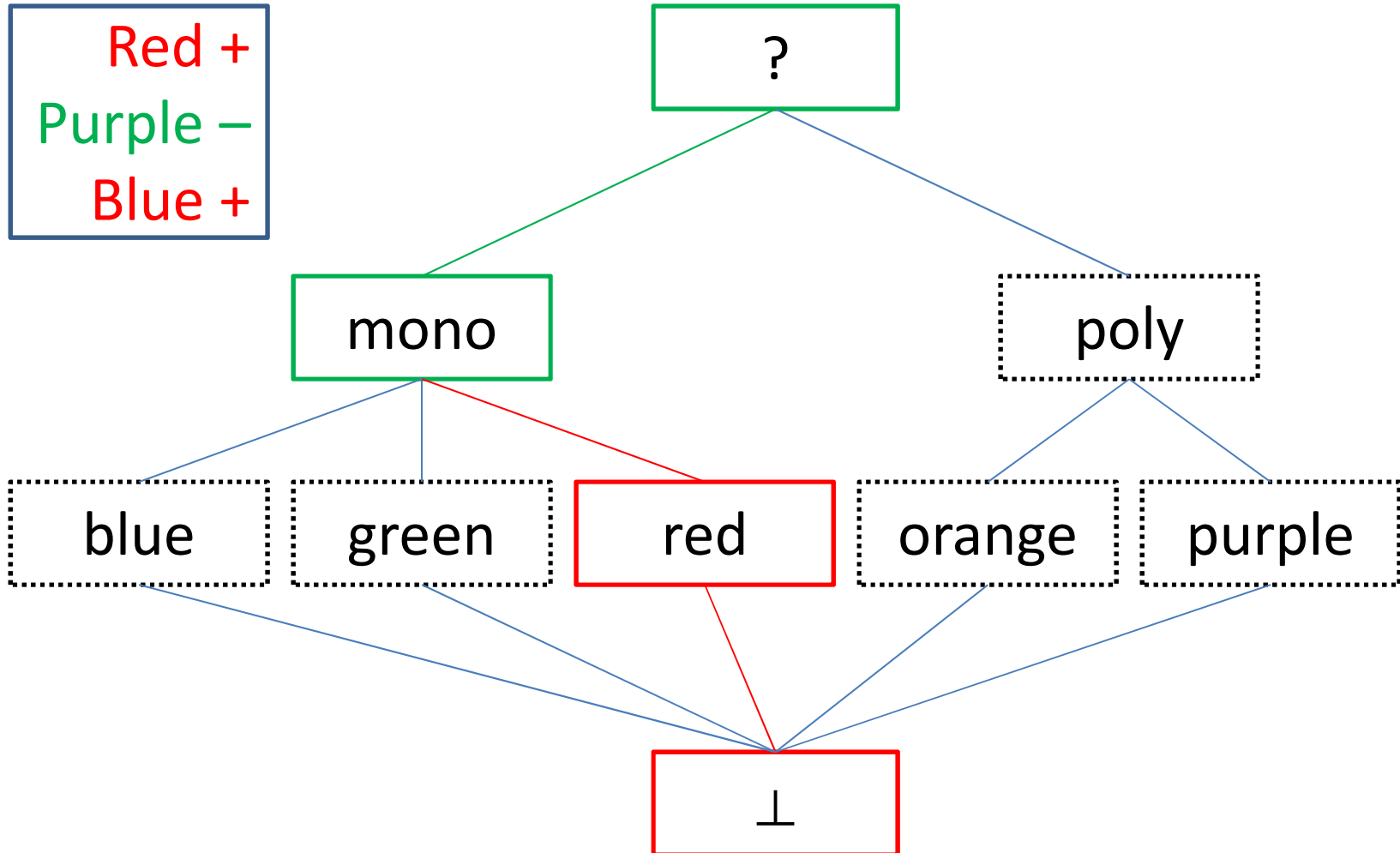
# Version-Spaces Algorithm



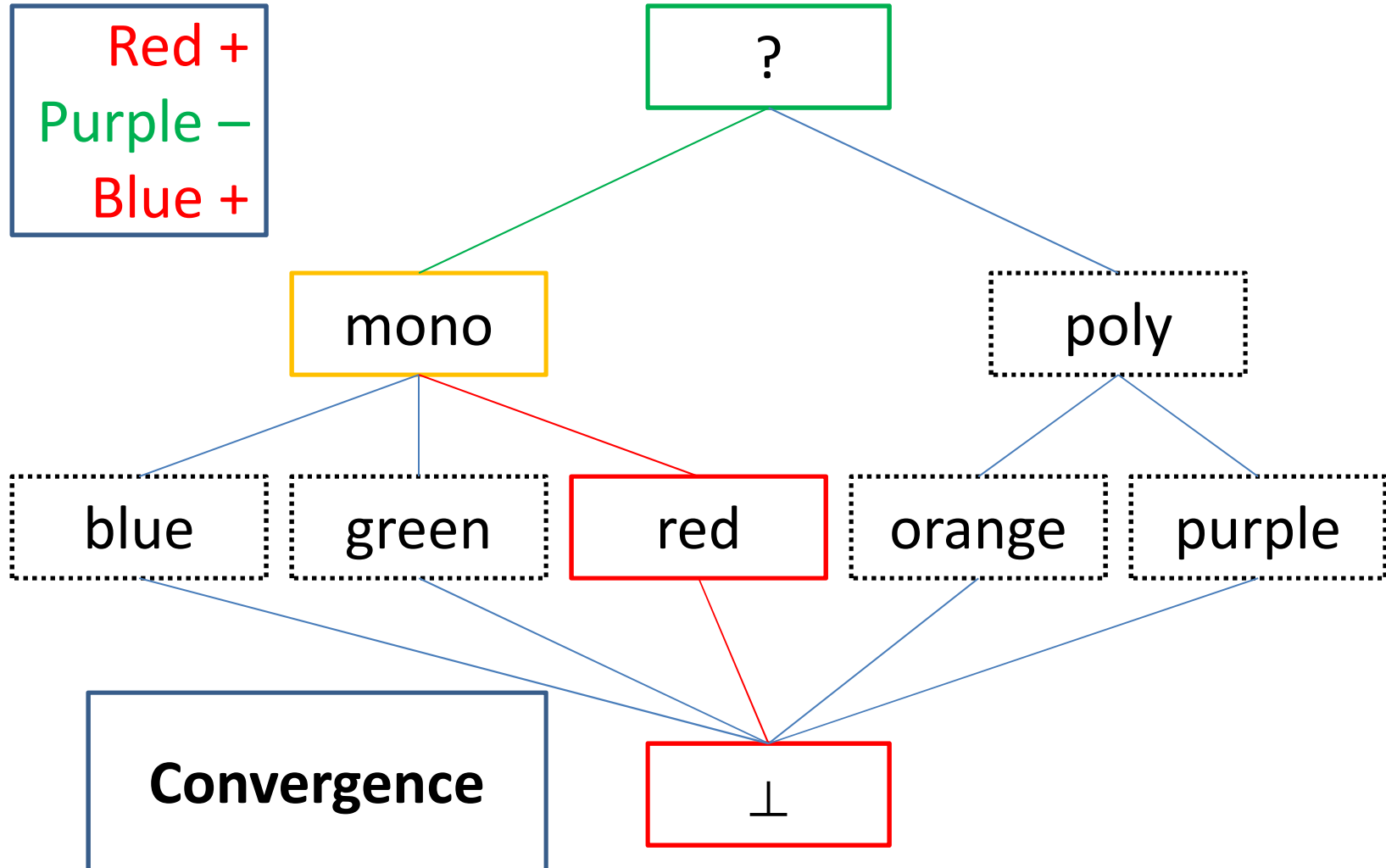
# Version-Spaces Algorithm



# Version-Spaces Algorithm



# Version-Spaces Algorithm



# Exercises: Artificial Intelligence

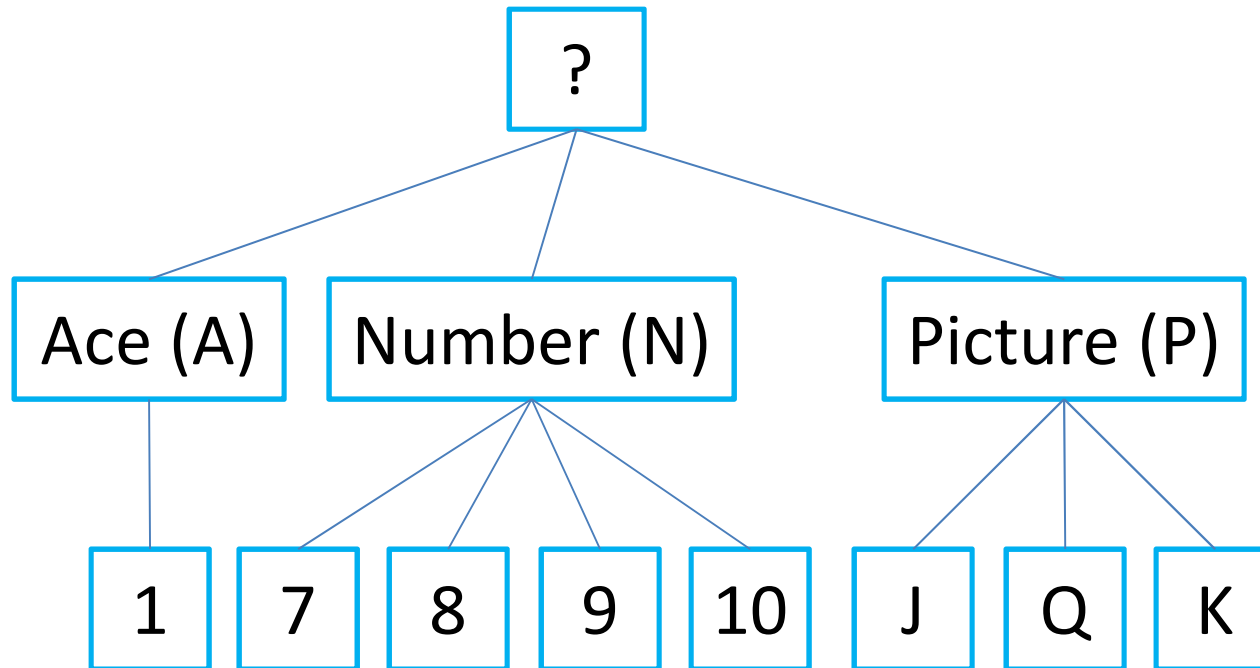
Version Spaces: Playing Cards

Version Spaces: Playing Cards

# PROBLEM

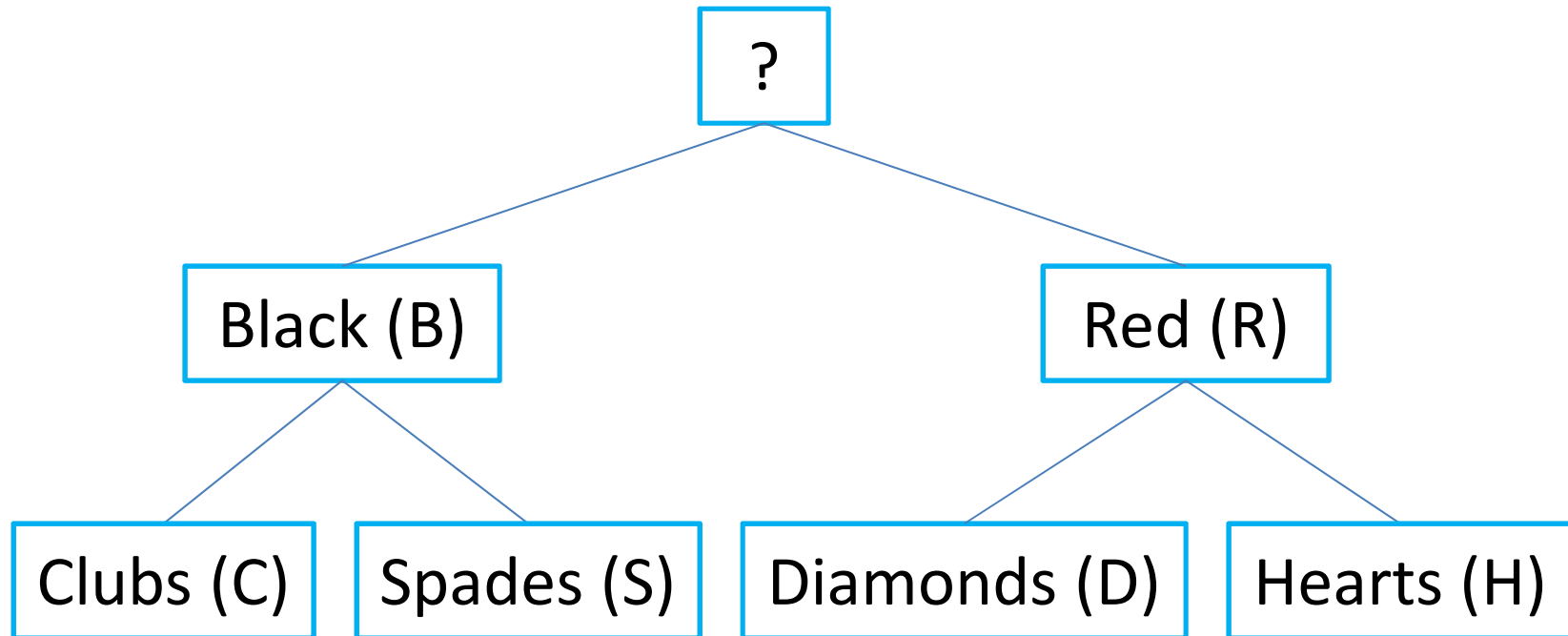
# Problem

- The concept hierarchies for *value*:



# Problem

- The concept hierarchies for *kind*:



# Problem

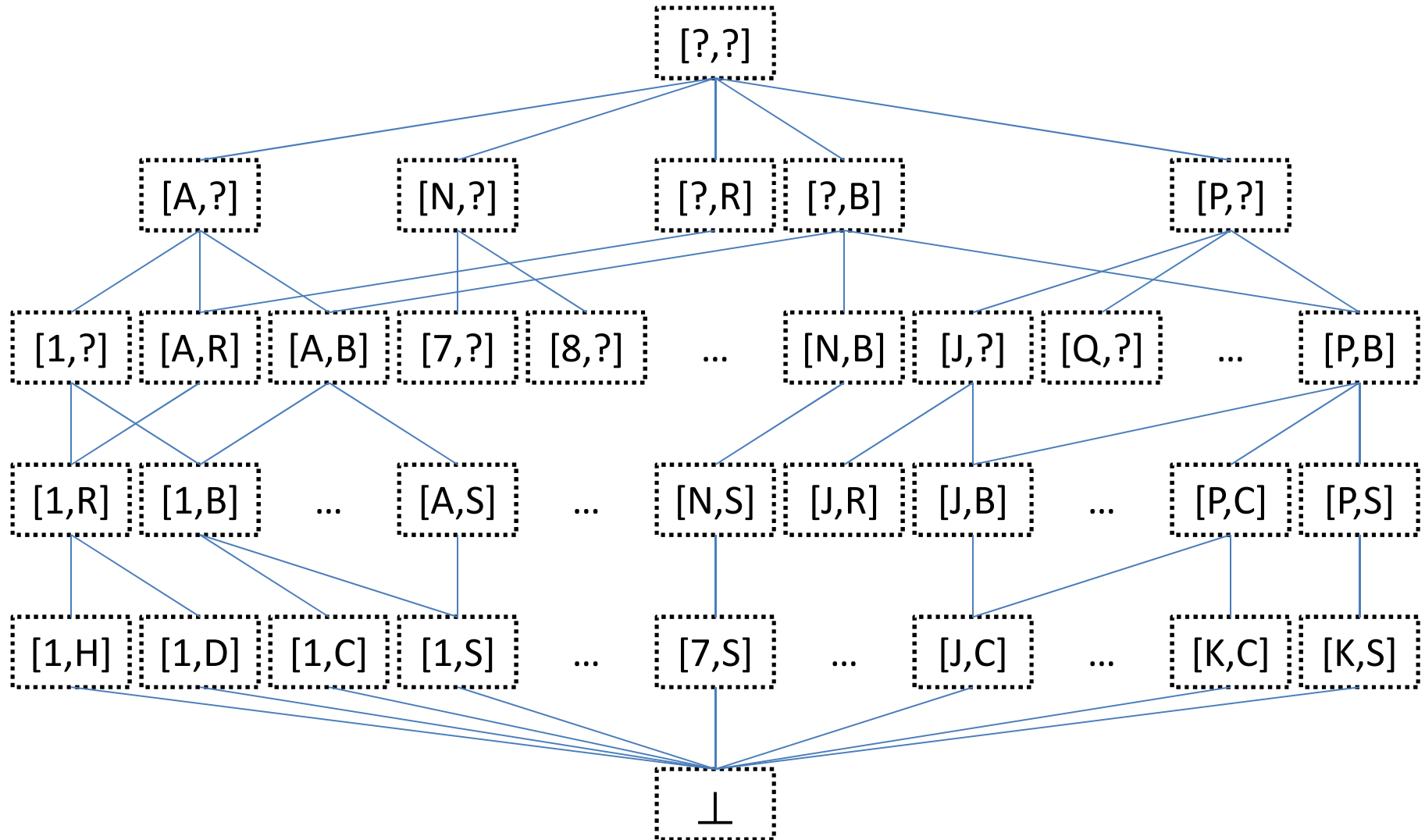
- ***Examples:***

- 7 of Diamonds +
- Ace of Clubs -
- Queen of Hearts -
- 9 of Hearts +
- 8 of Clubs -

Version Spaces: Playing Cards

# **PROBLEM OVERVIEW**

# Problem overview (Fragment)



Version Spaces: Playing Cards

# **FIND-S ALGORITHM**

# Find-S Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

[?,?]

[7,D]

⊥

# Find-S Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

[?,?]

[N,R]

[7,R]

[7,D]

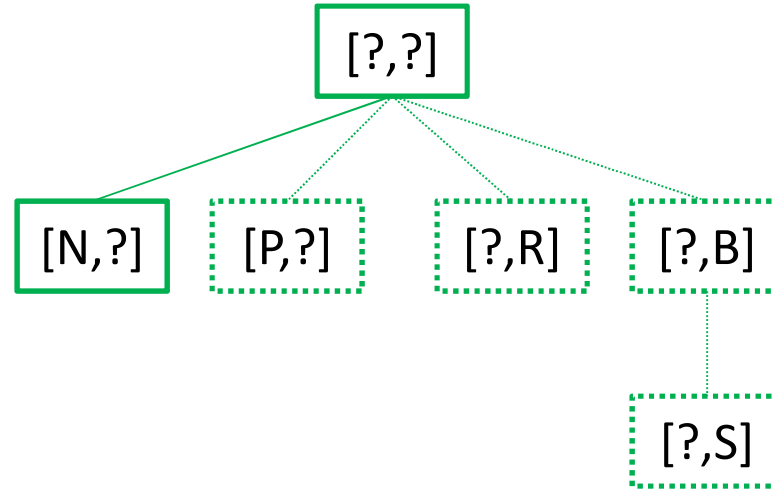
⊥

Version Spaces: Playing Cards

# **DUAL FIND-S ALGORITHM**

# Dual Find-S Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

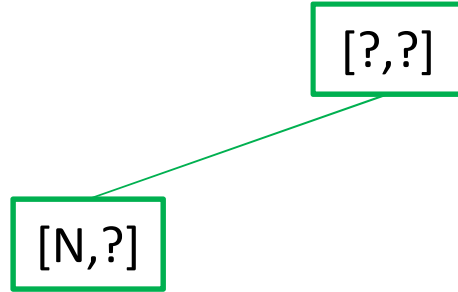


**Maintain 1 out  
of 4 choices**

⊥

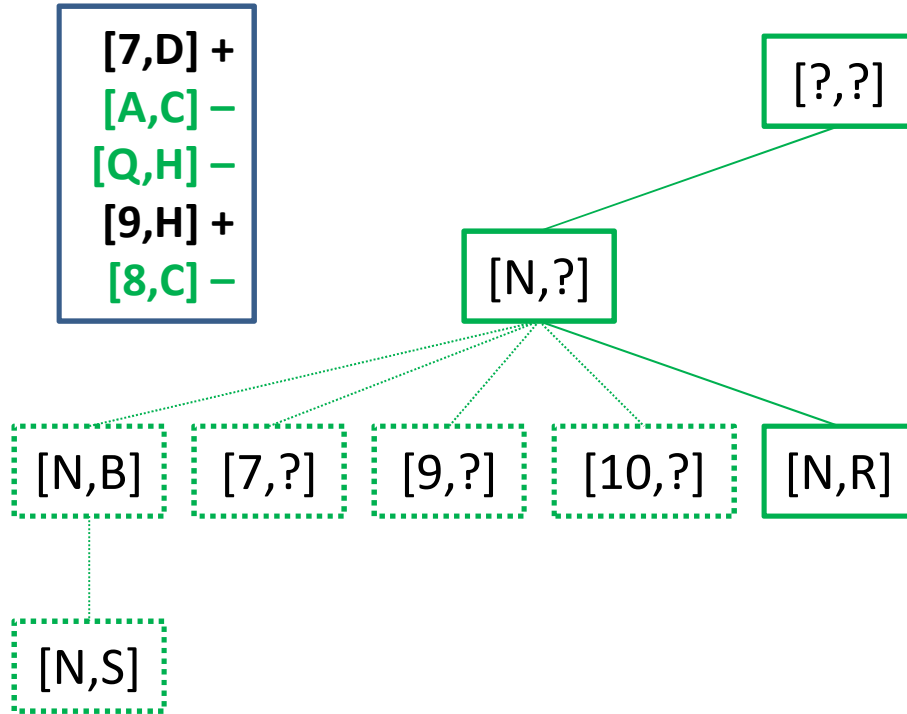
# Dual Find-S Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -



⊥

# Dual Find-S Algorithm

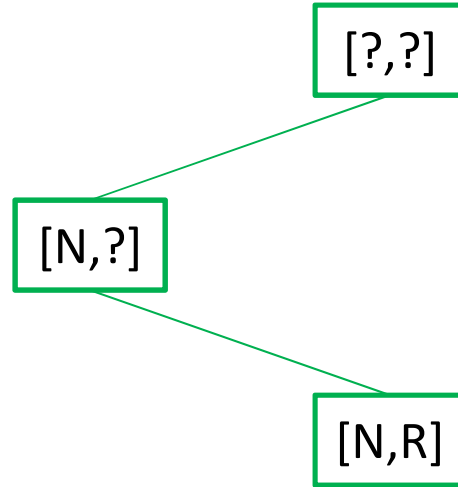


**Maintain 1 out  
of 5 choices**

⊥

# Dual Find-S Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -



⊥

Version Spaces: Playing Cards

# **VERSION-SPACES ALGORITHM**

# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

[?,?]

[7,D]

⊥

# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

[?,?]

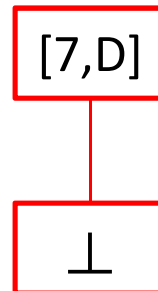
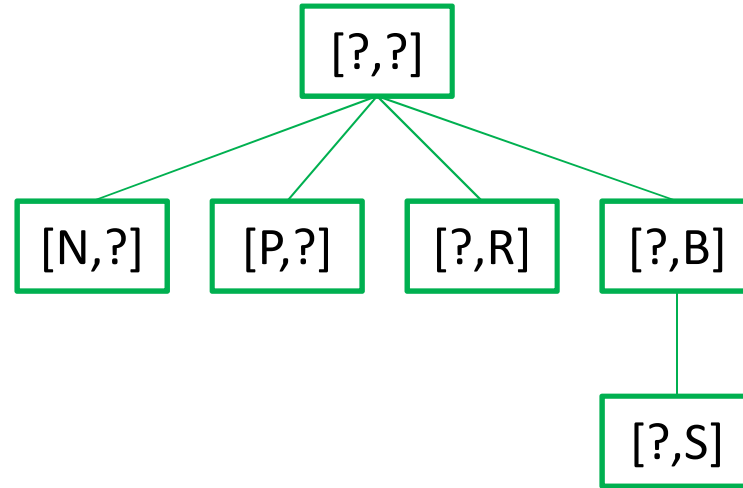
[7,D]

⊥



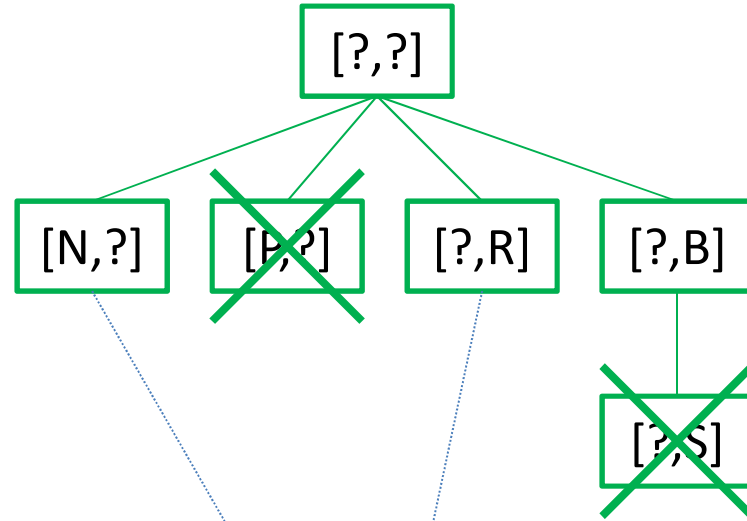
# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

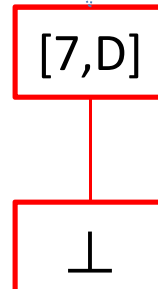


# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

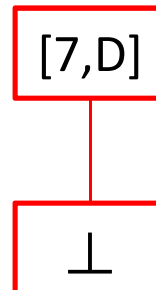
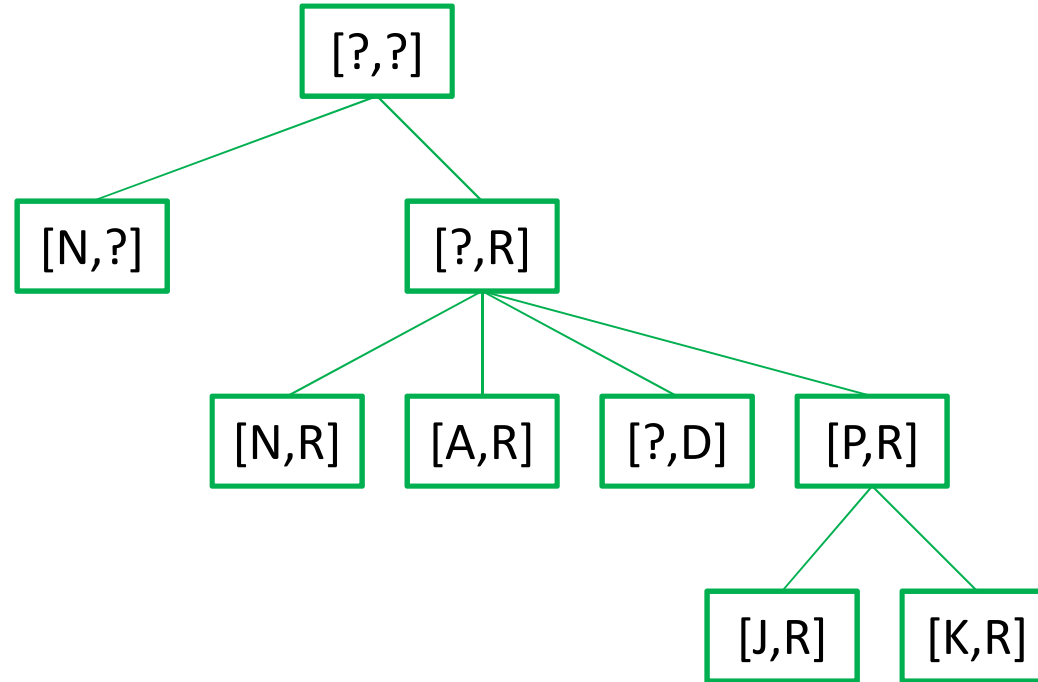


**2 out of 4 do not  
generalize the  
specific model**



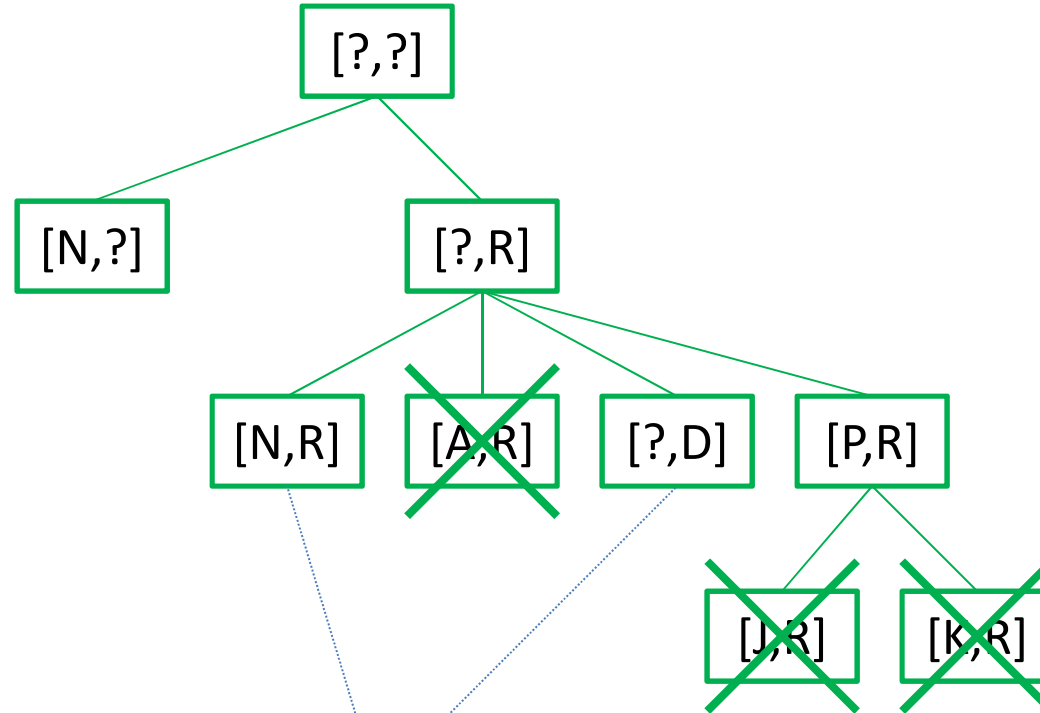
# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

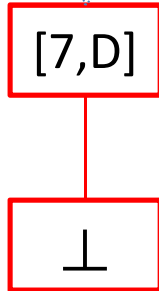


# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

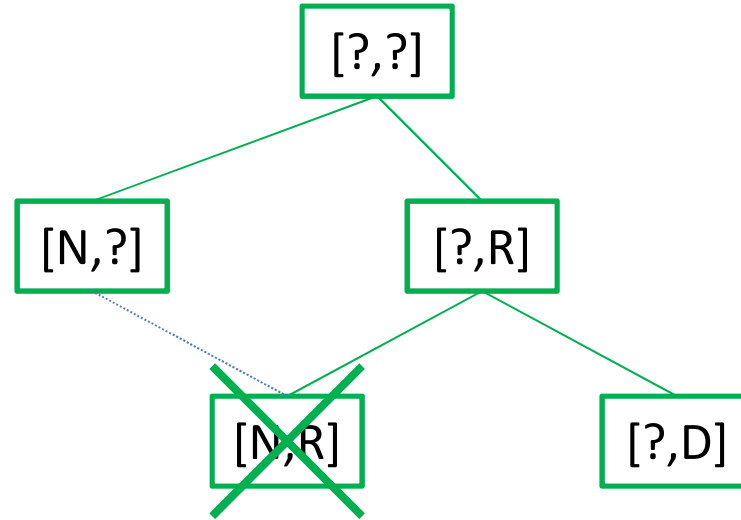


**3 out of 5 do not generalize the specific model**

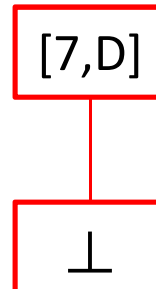


# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

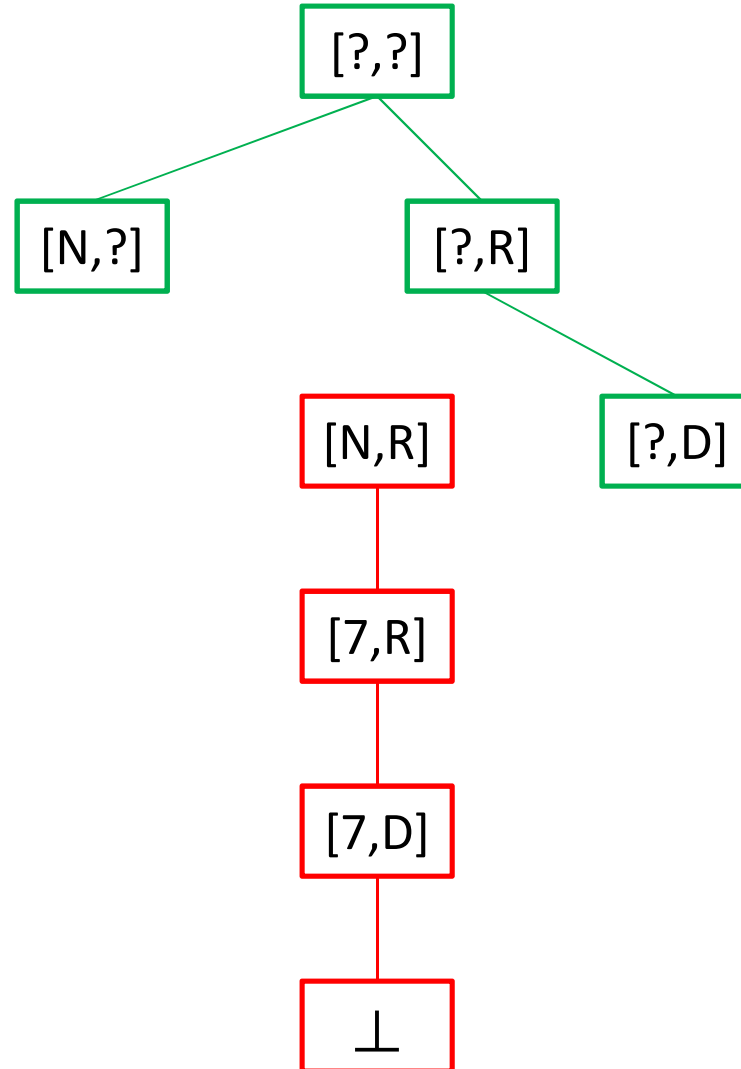


**Redundant  
Hypotheses**



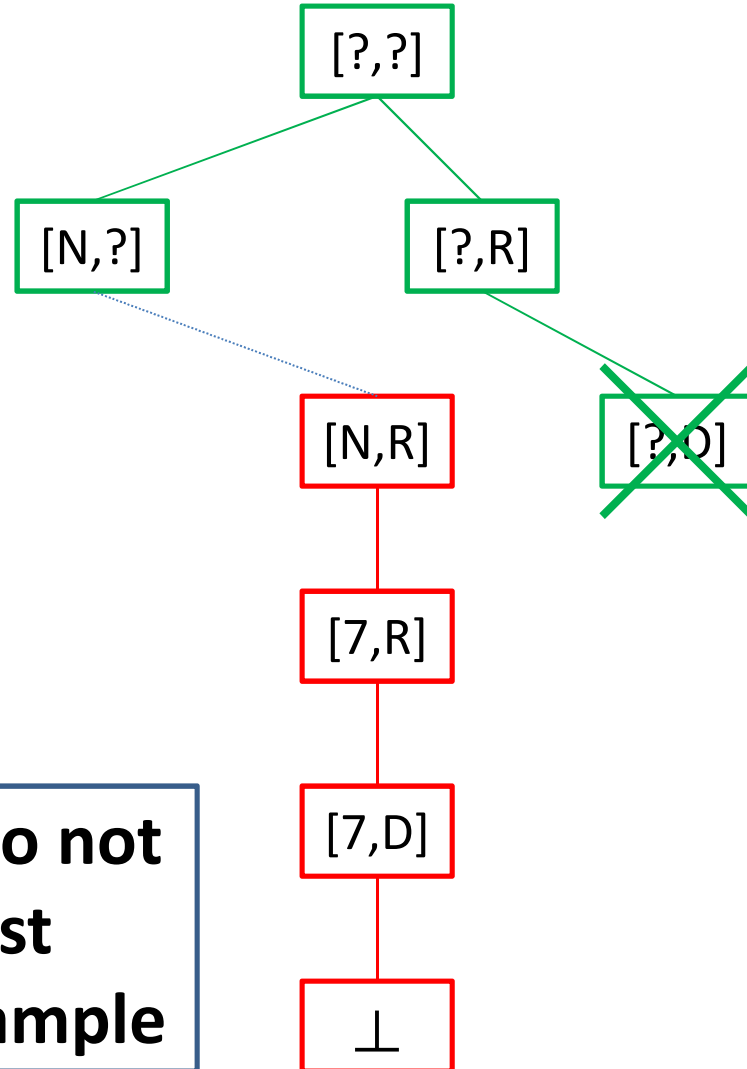
# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -



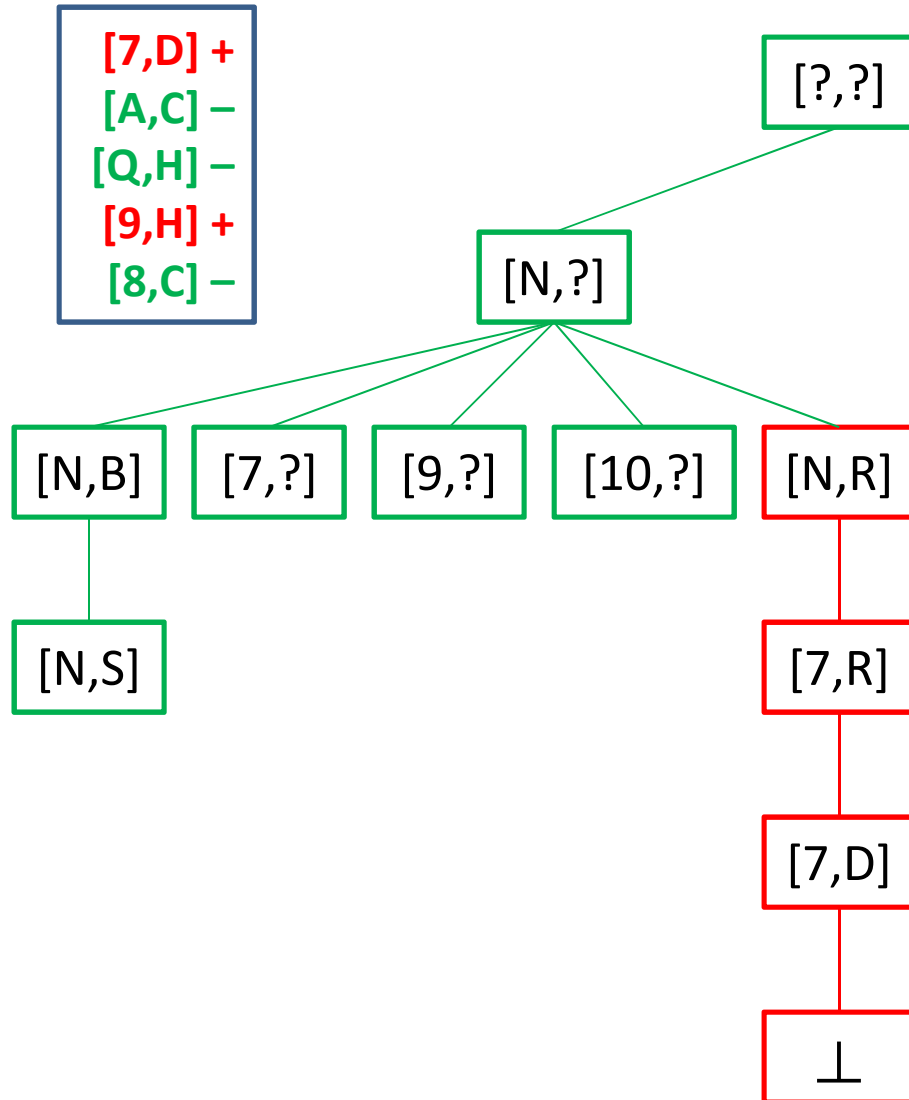
# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -

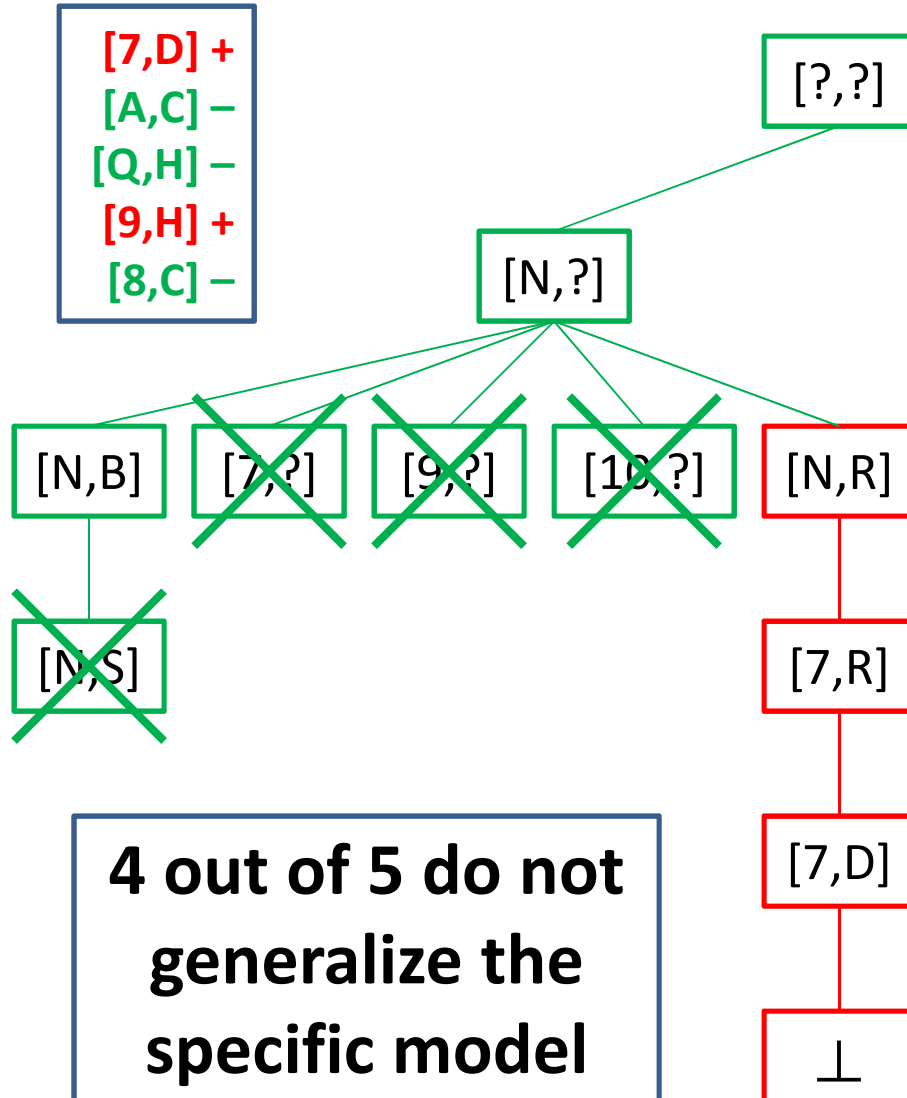


**1 out of 2 do not cover last positive example**

# Version-Spaces Algorithm

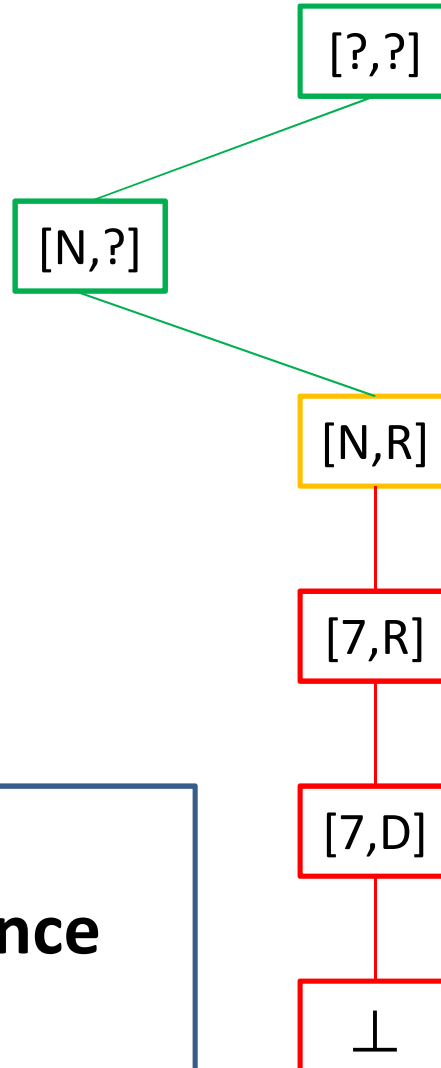


# Version-Spaces Algorithm



# Version-Spaces Algorithm

[7,D] +  
[A,C] -  
[Q,H] -  
[9,H] +  
[8,C] -



**Convergence**

# Exercises: Artificial Intelligence

Version Spaces: Ex-exam

Version Spaces: Ex-exam

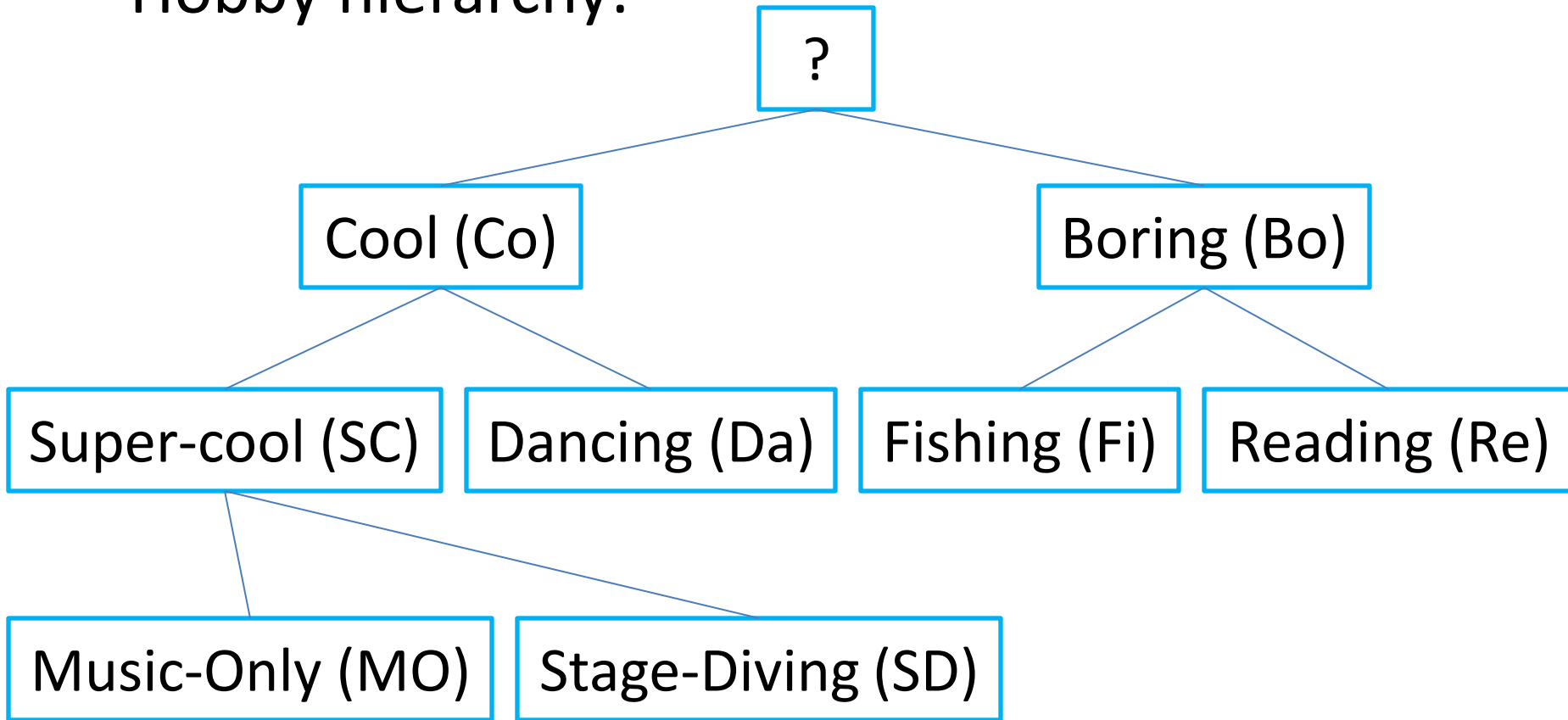
# PROBLEM

# Problem

- Searching for a new drummer.
  - Candidates hand in CV:
    - Hobby, Music preference, Age, Photo
  - 5 Profiles selected from 900
    - Evaluated: Accepted or Rejected
  - Learn Model, using Version Spaces
    - Conclude on 3 of the other 895 CVs using Model

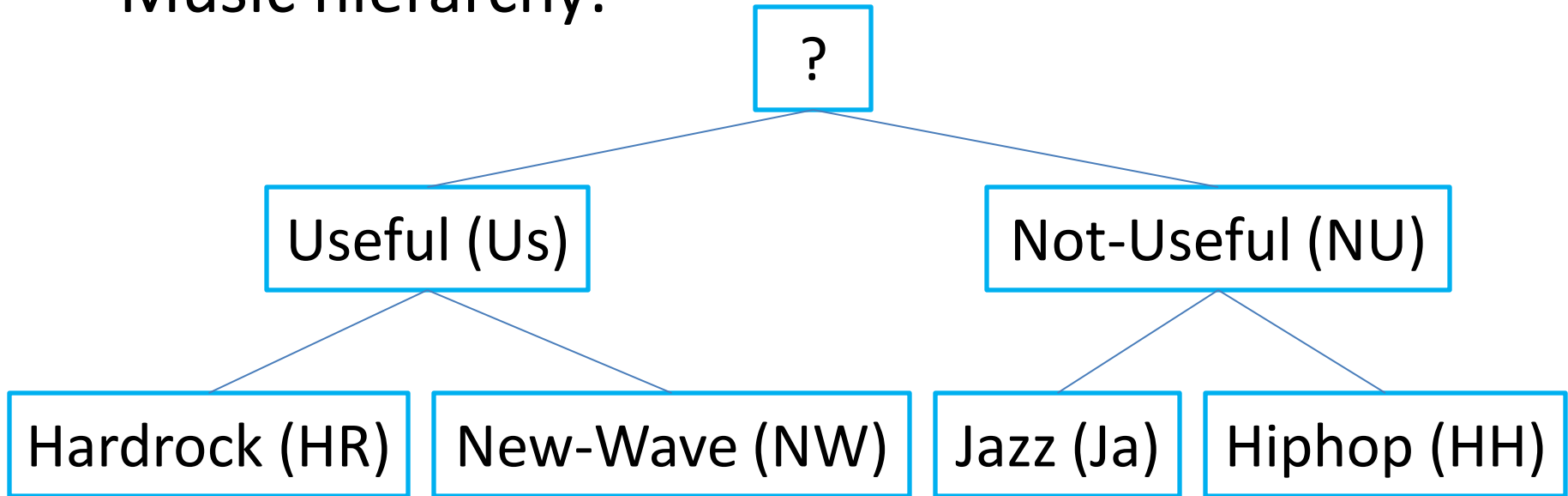
# Problem

- Hobby hierarchy:



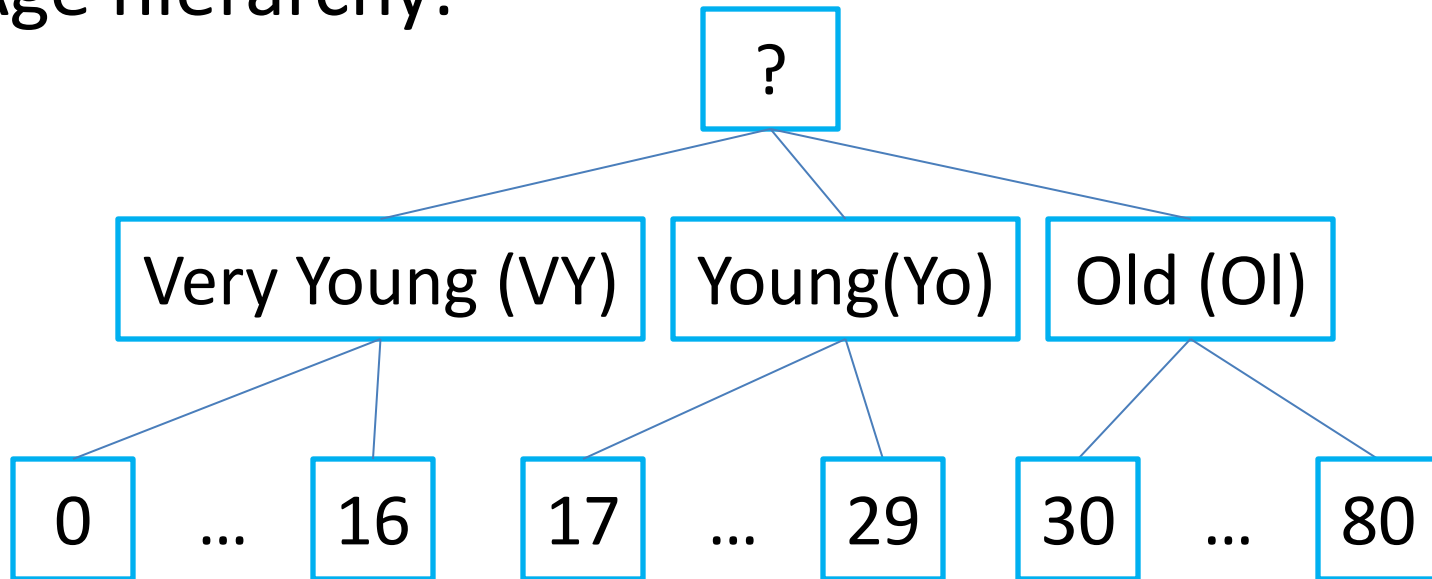
# Problem

- Music hierarchy:



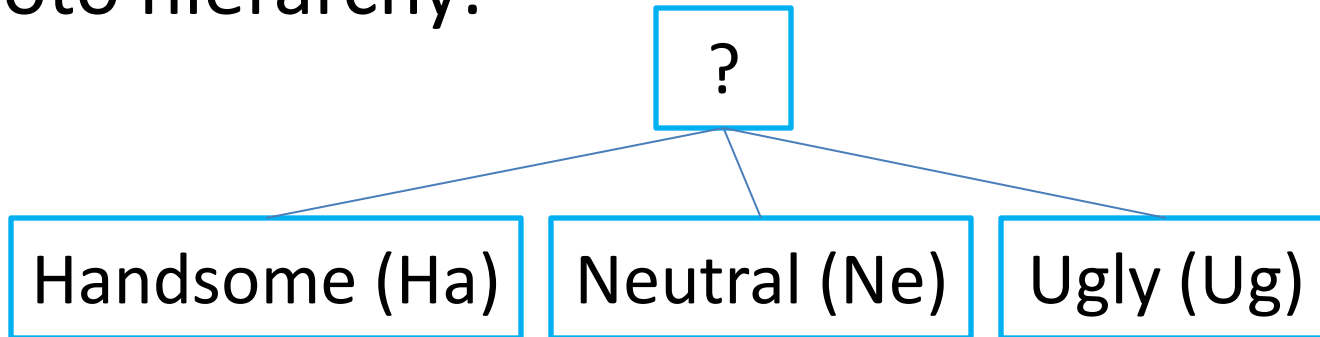
# Problem

- Age hierarchy:



# Problem

- Photo hierarchy:



# Problem

- ***Examples:***

Hobby	Music	Age	Photo	Selected?
Fishing	Hiphop	16	Handsome	No
Stage-diving	New-wave	18	Neutral	Yes
Dancing	Hardrock	32	Ugly	No
Music-only	Hardrock	25	Handsome	Yes
Stage-diving	Jazz	29	Ugly	No

Version Spaces: Ex-exam

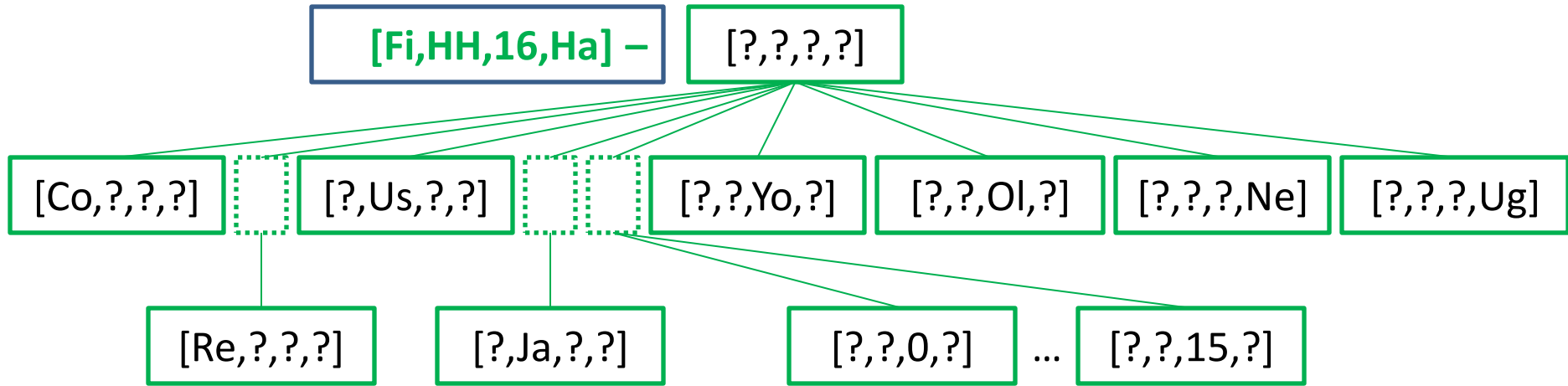
# **VERSION-SPACES ALGORITHM**

# Version-Spaces Algorithm

[?,?,?,?]

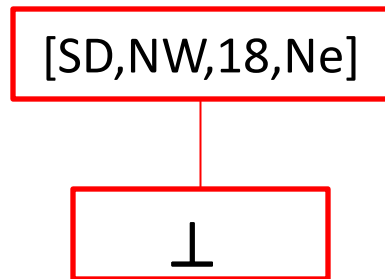
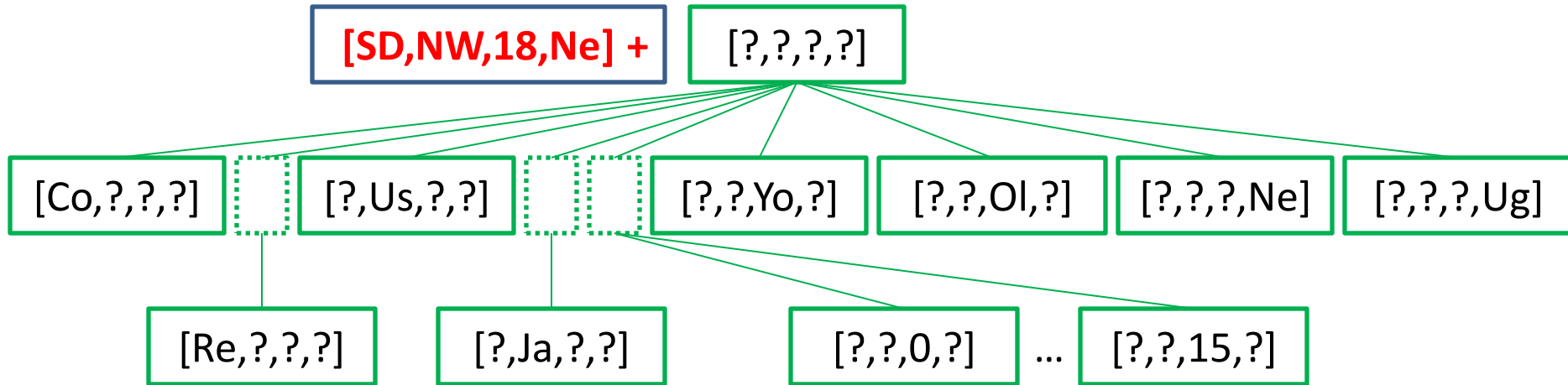
⊥

# Version-Spaces Algorithm

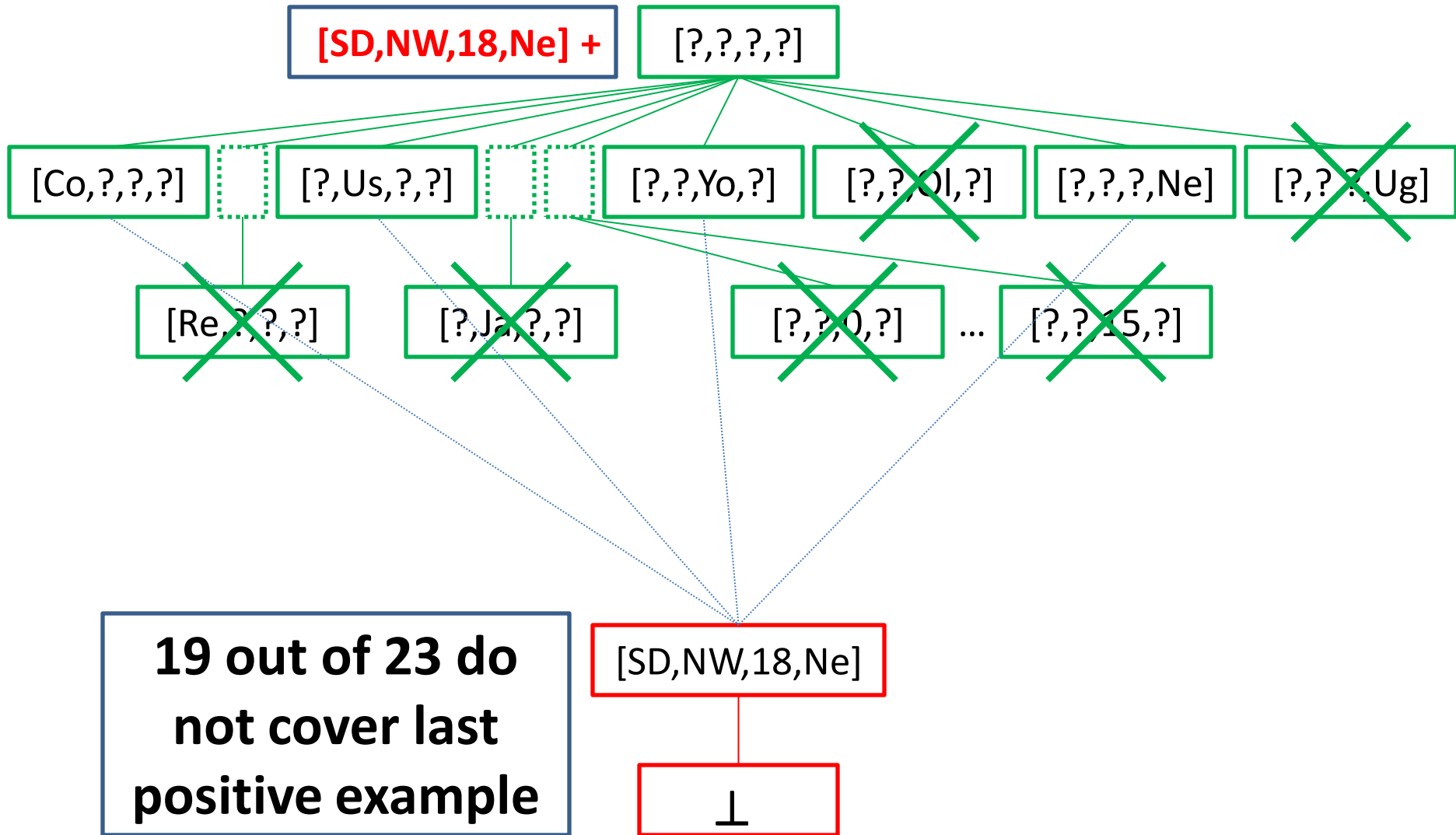


⊥

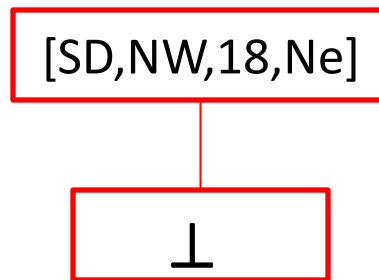
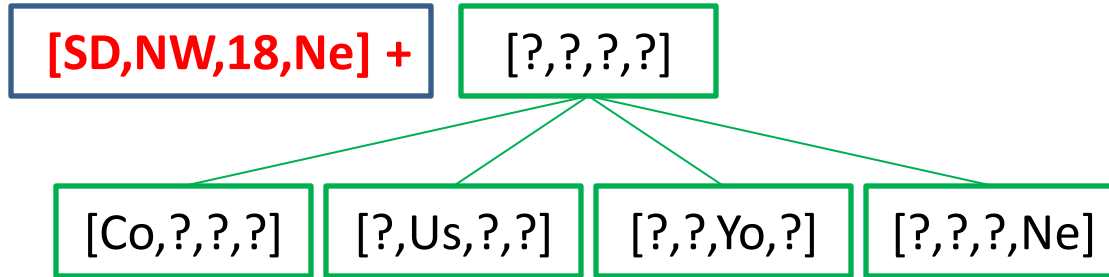
# Version-Spaces Algorithm



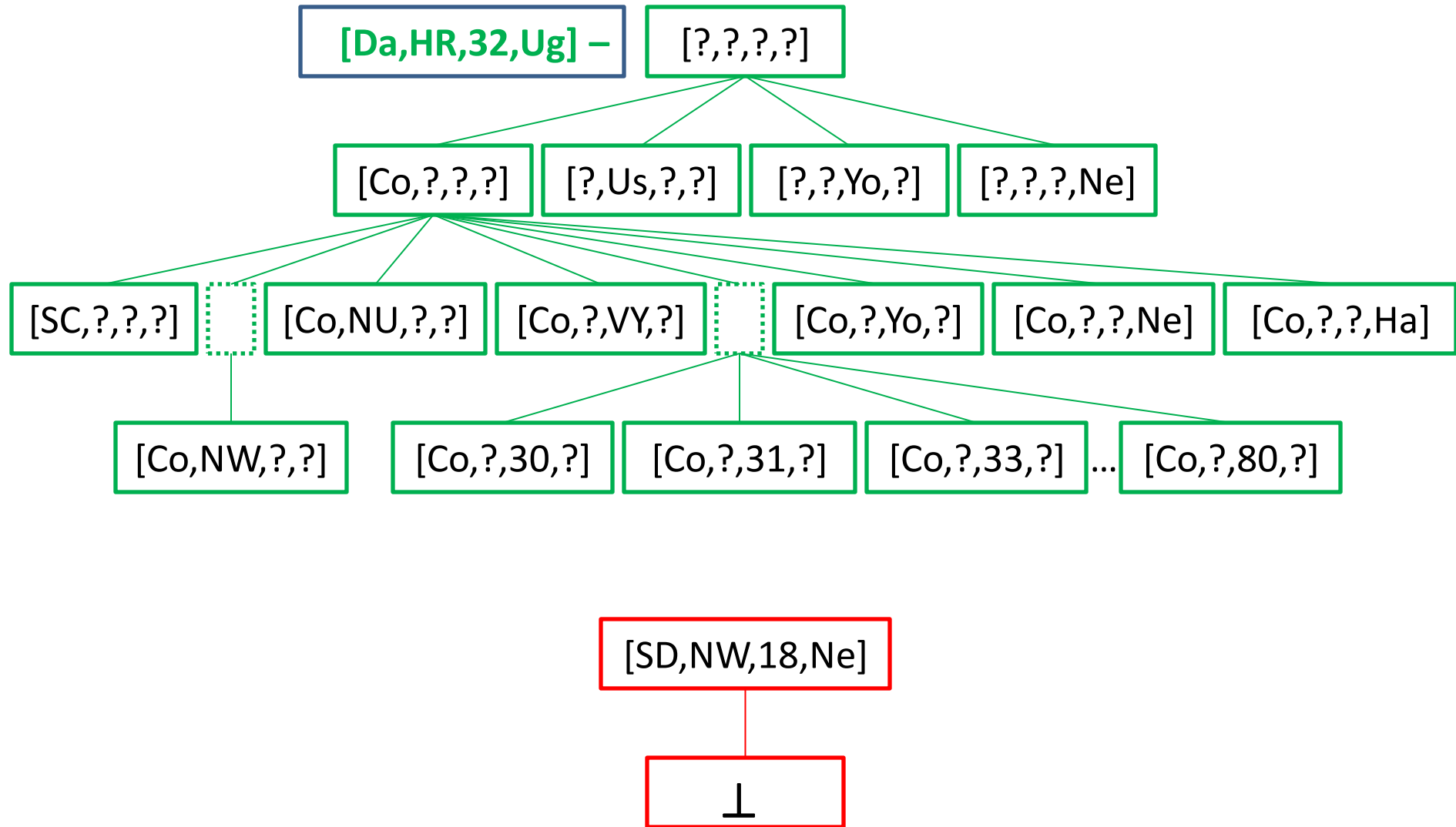
# Version-Spaces Algorithm



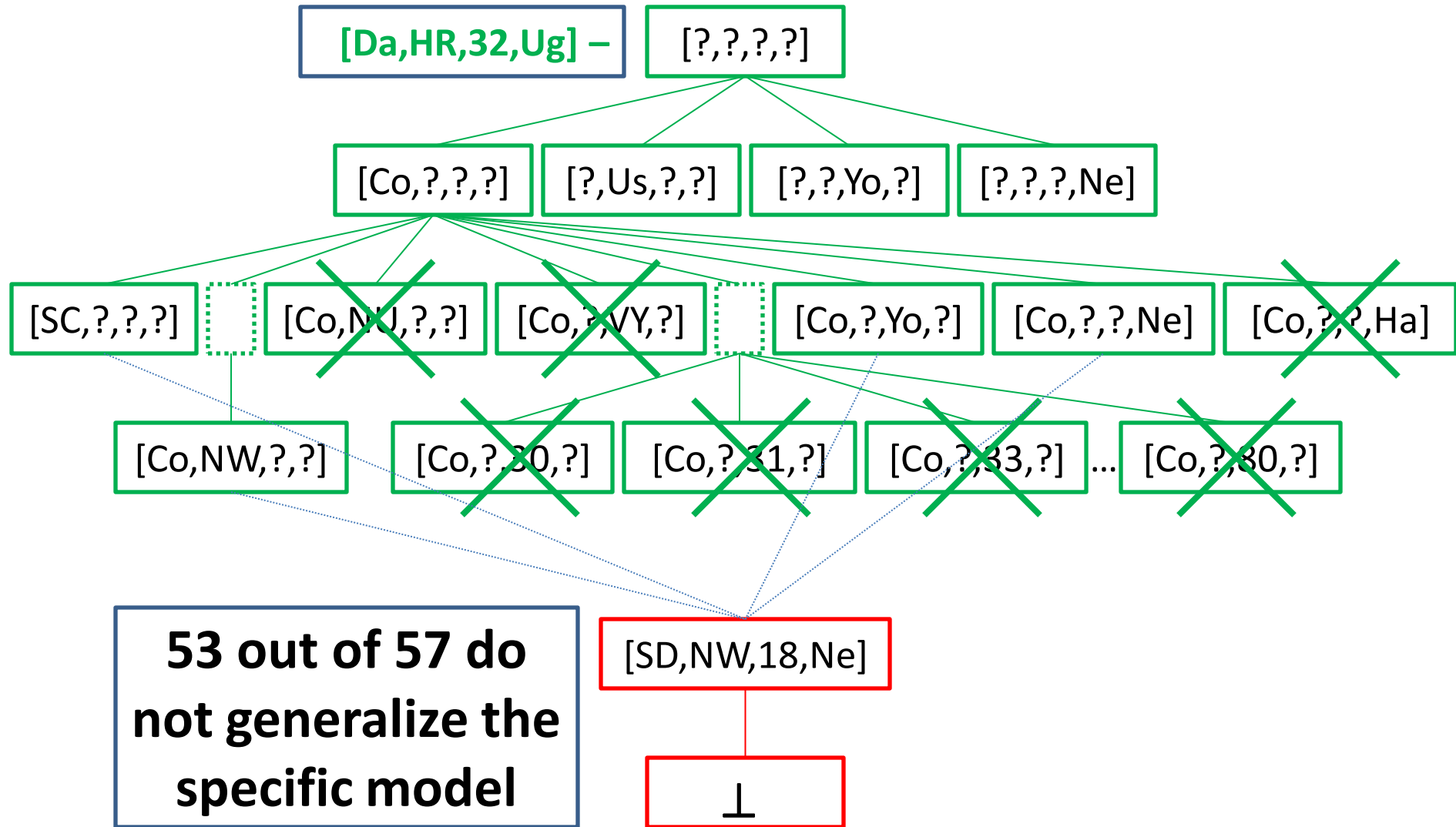
# Version-Spaces Algorithm



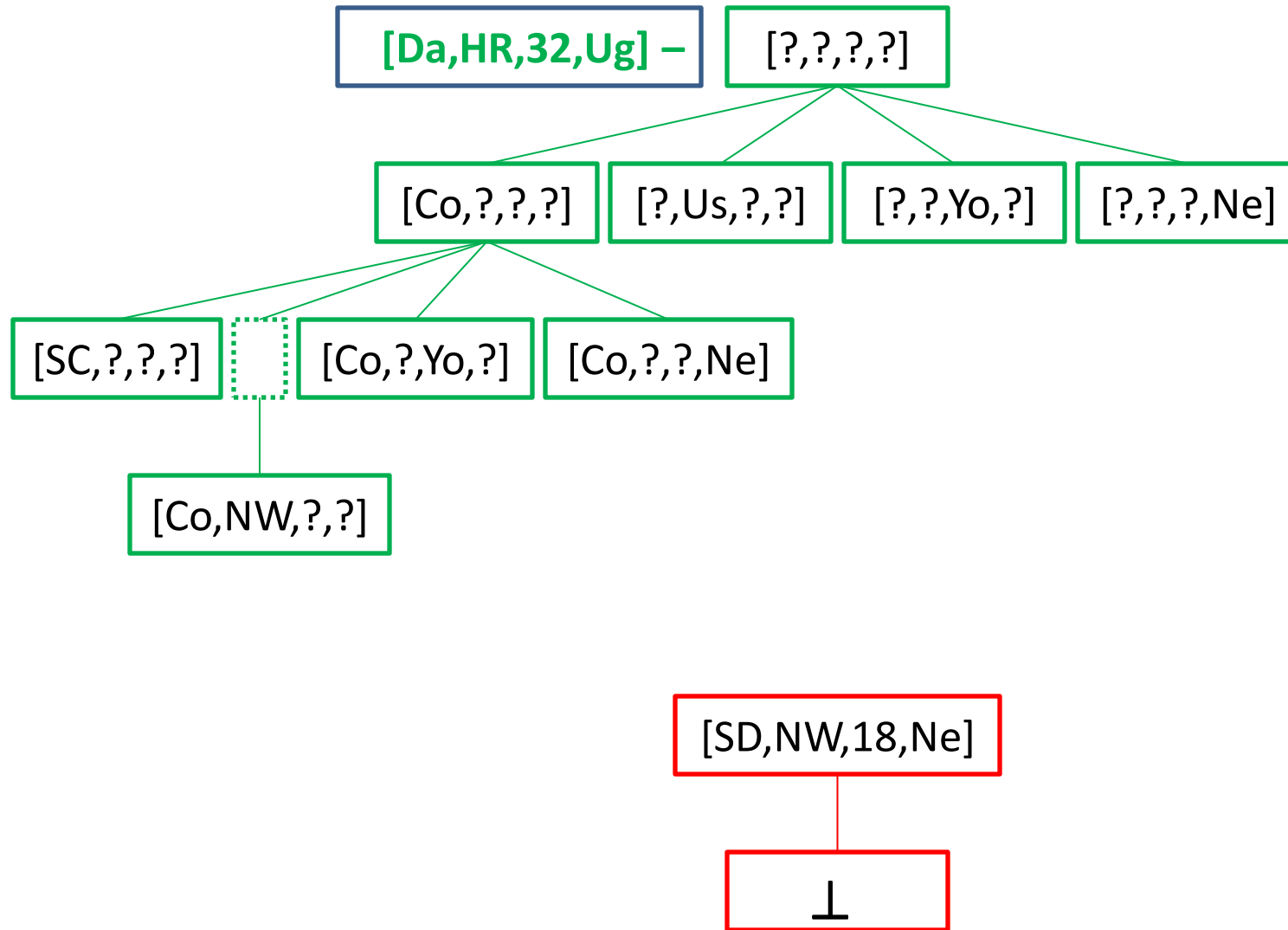
# Version-Spaces Algorithm



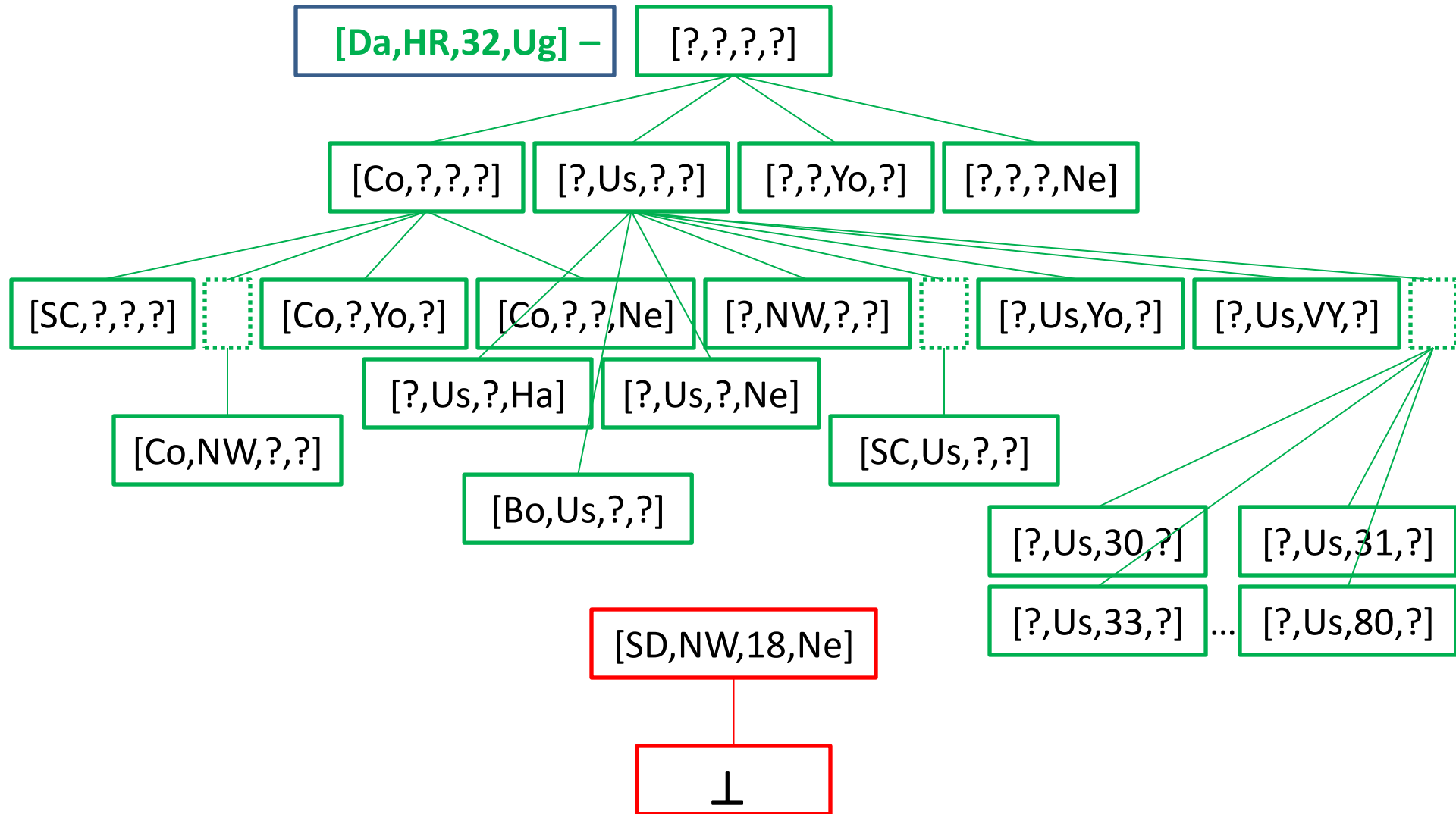
# Version-Spaces Algorithm



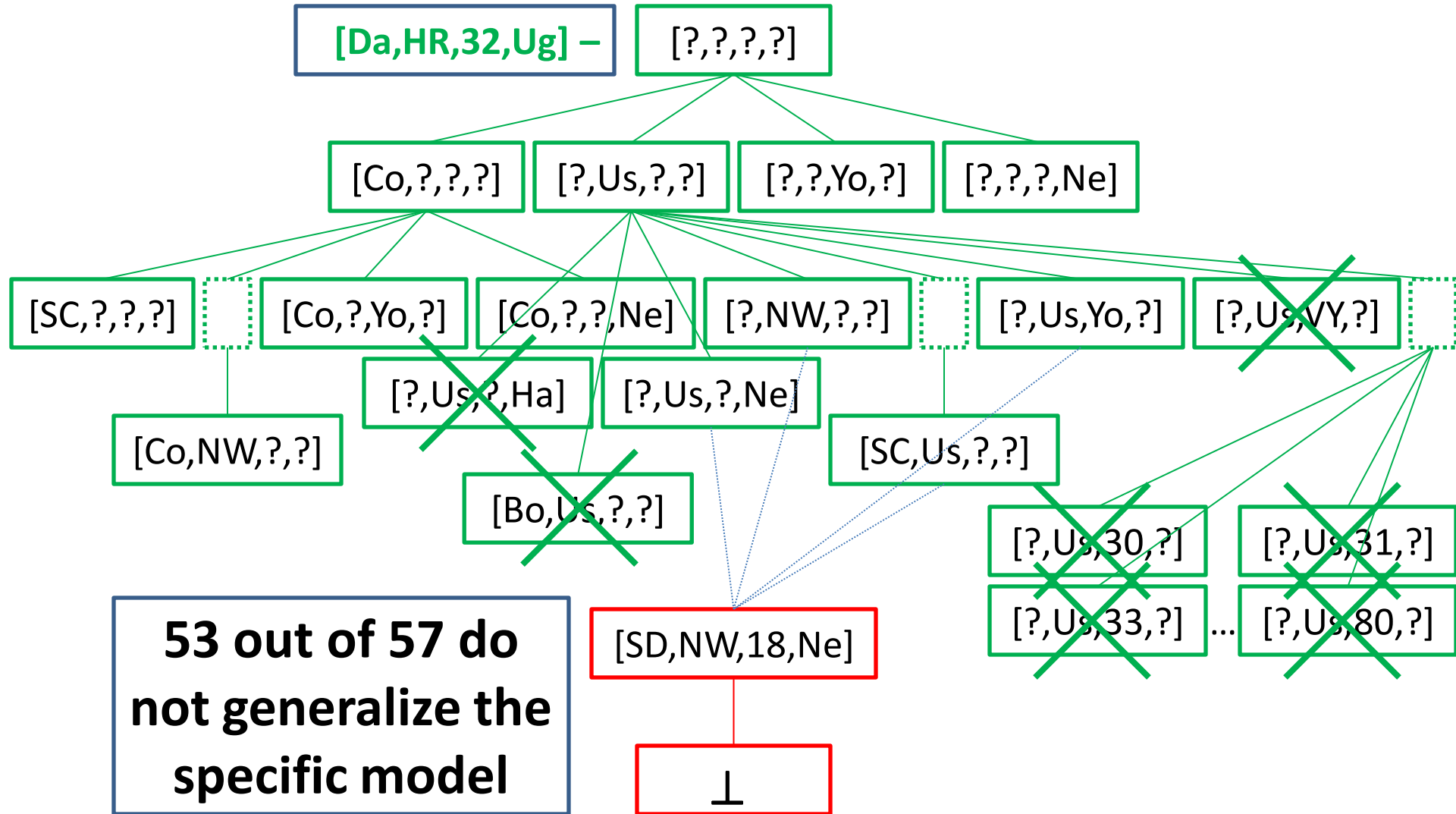
# Version-Spaces Algorithm



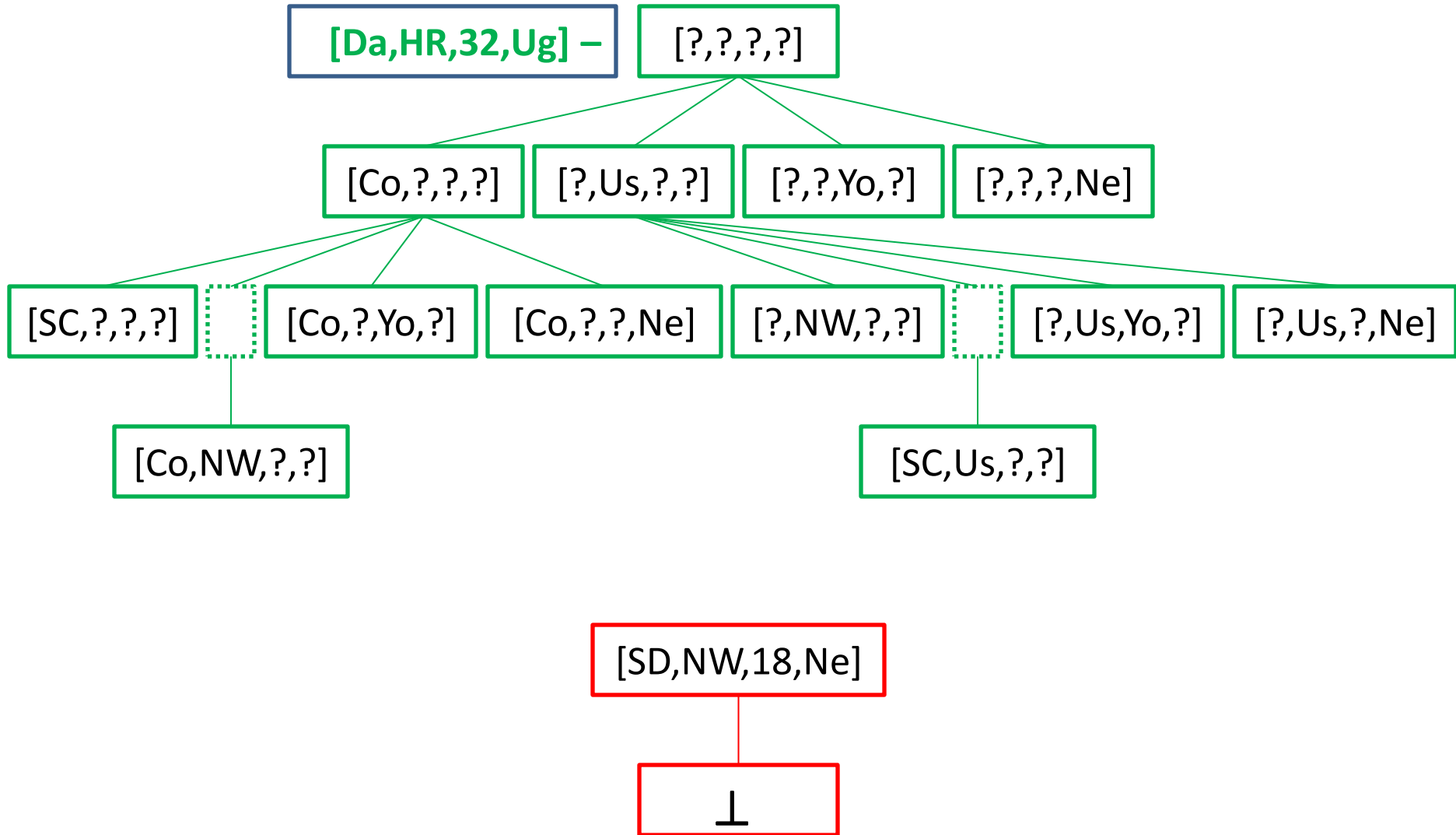
# Version-Spaces Algorithm



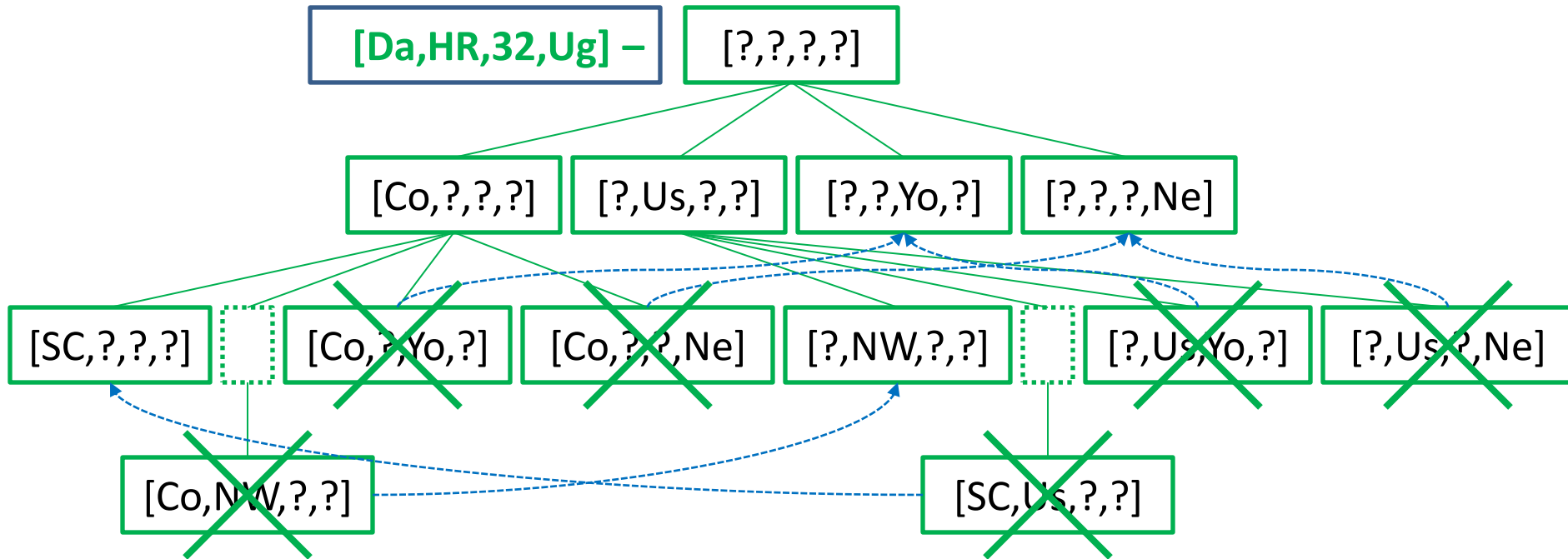
# Version-Spaces Algorithm



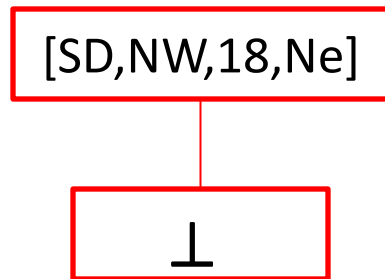
# Version-Spaces Algorithm



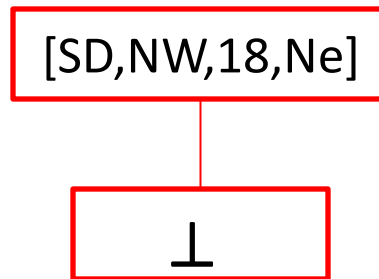
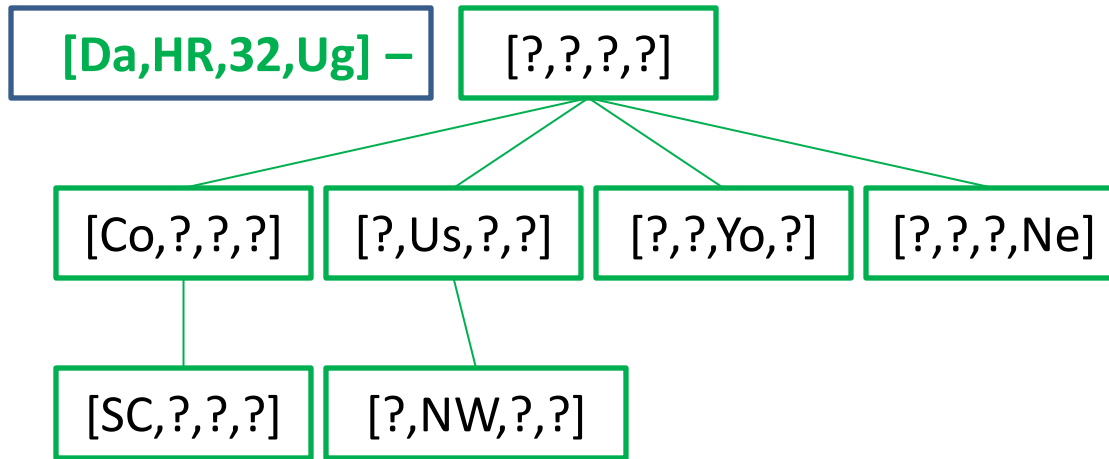
# Version-Spaces Algorithm



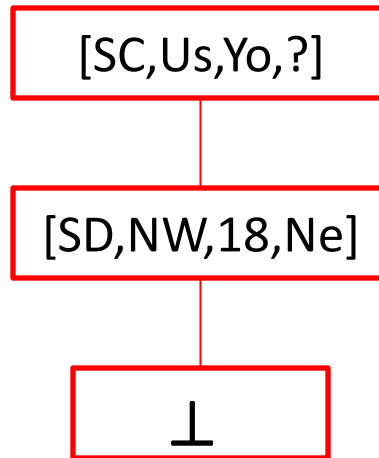
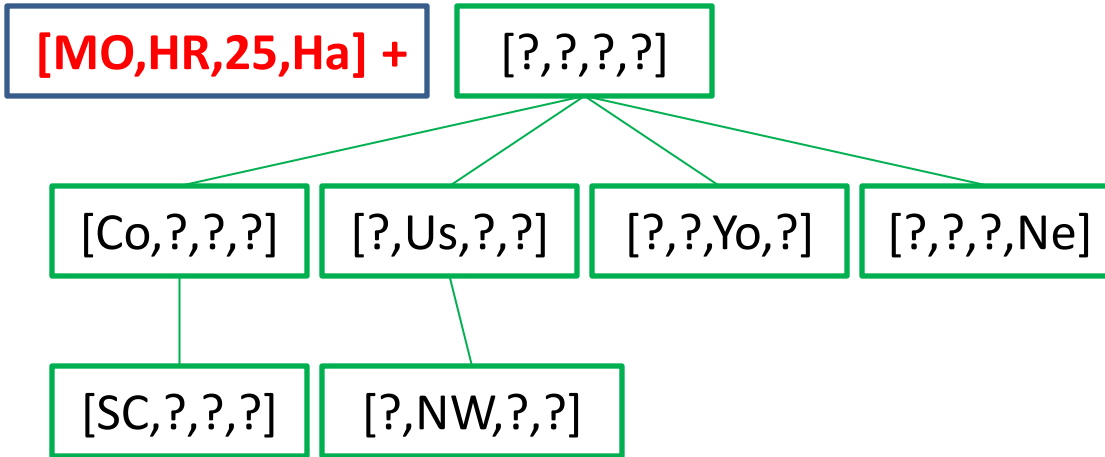
**Redundant hypotheses**



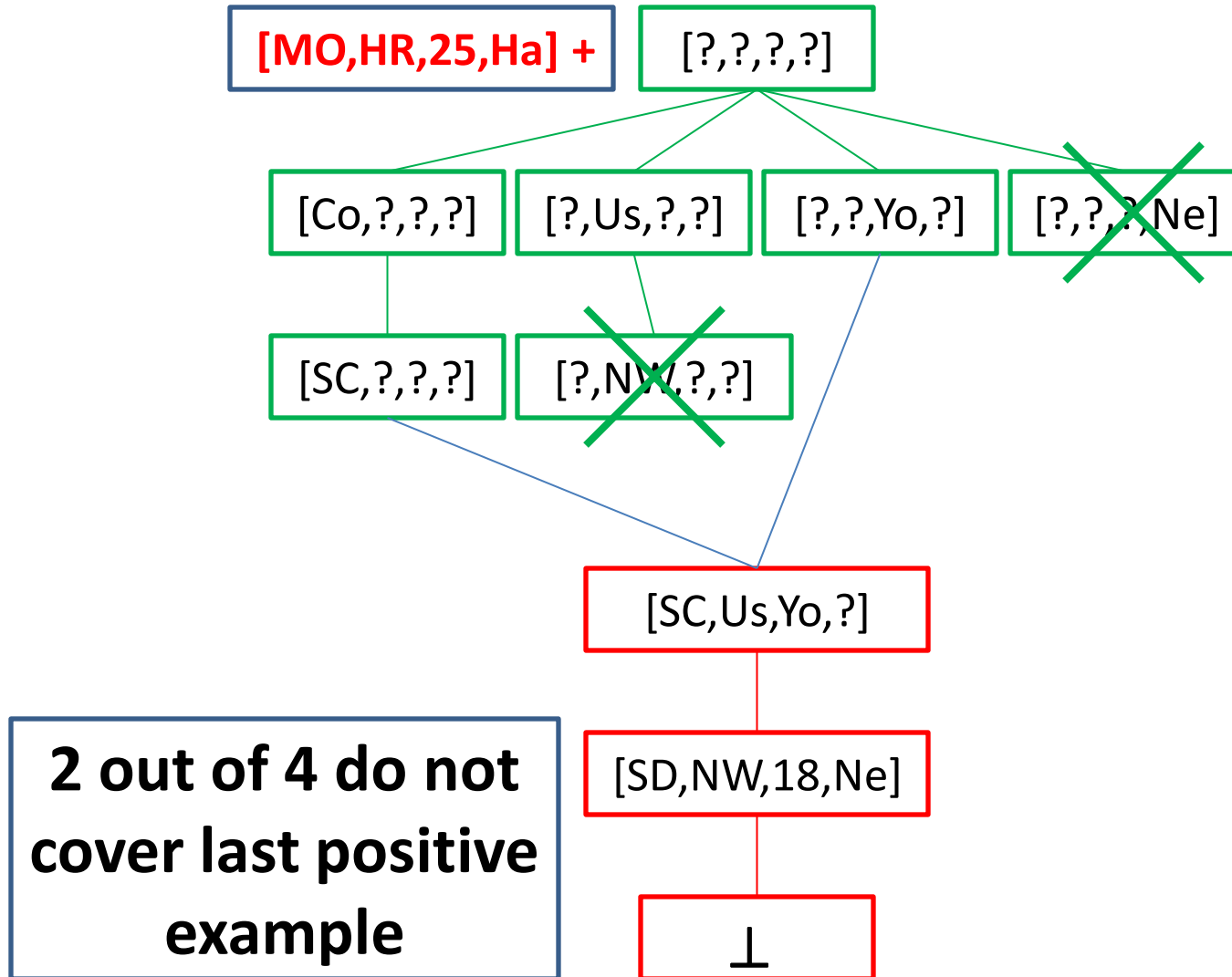
# Version-Spaces Algorithm



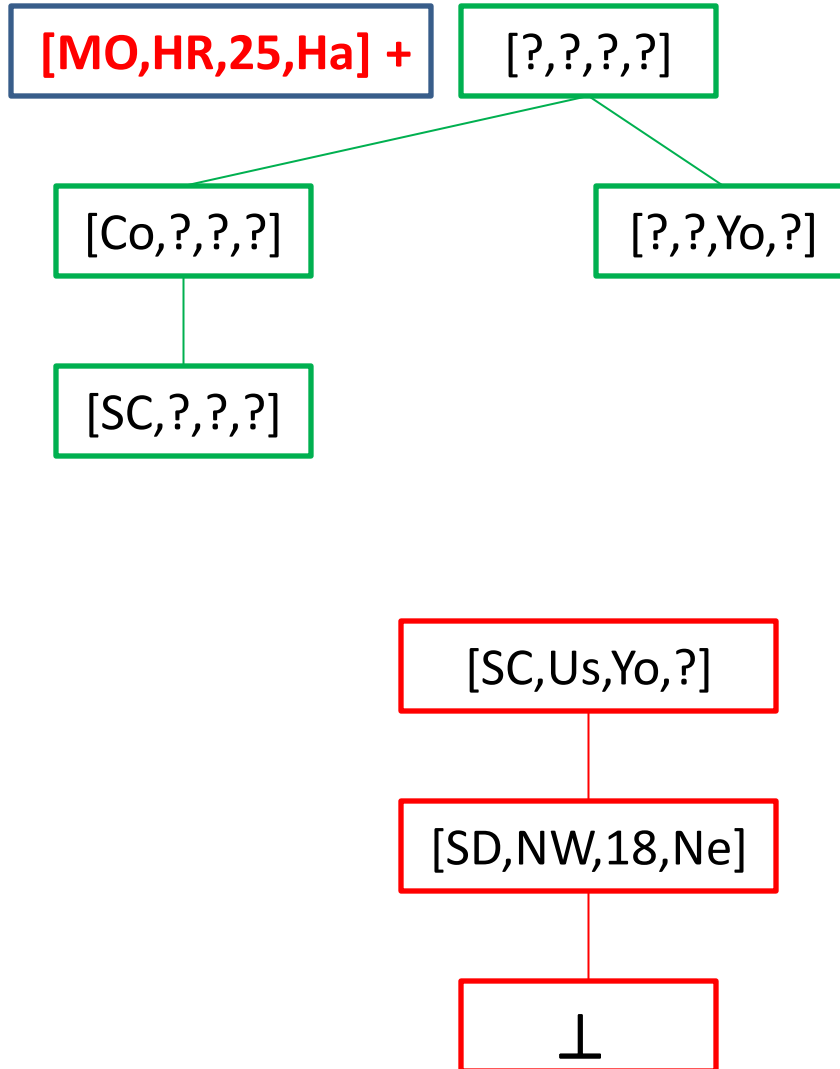
# Version-Spaces Algorithm



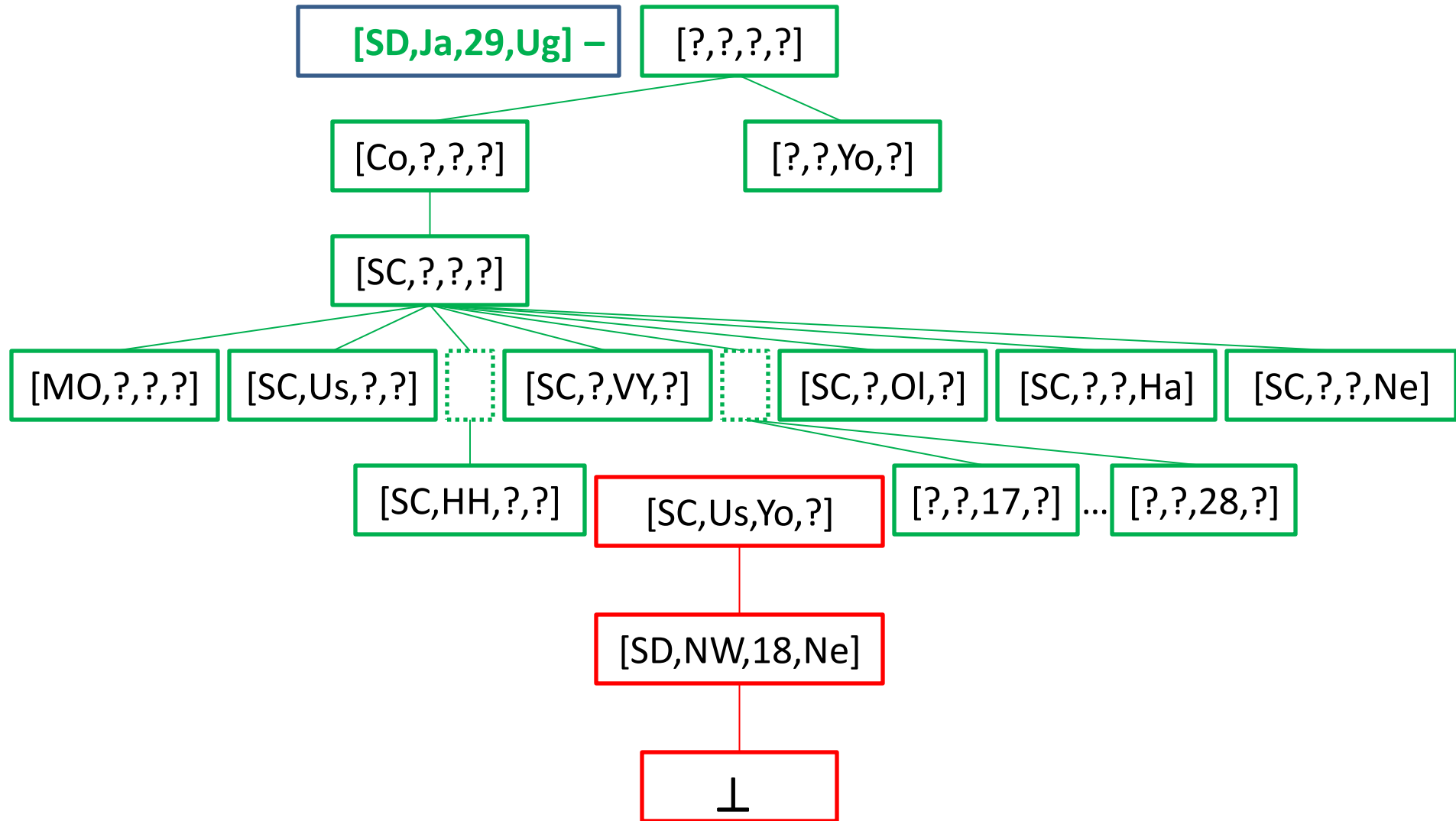
# Version-Spaces Algorithm



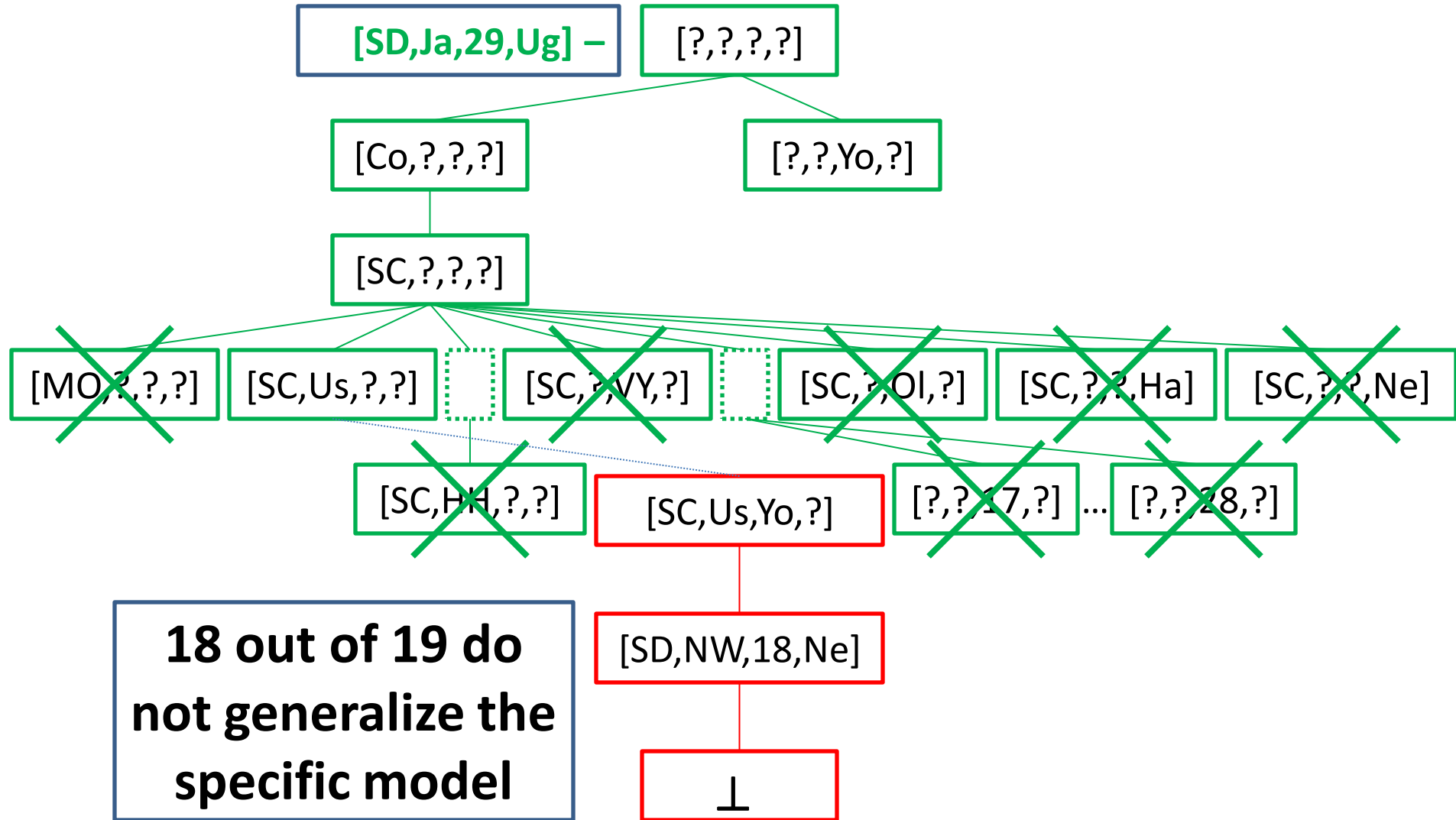
# Version-Spaces Algorithm



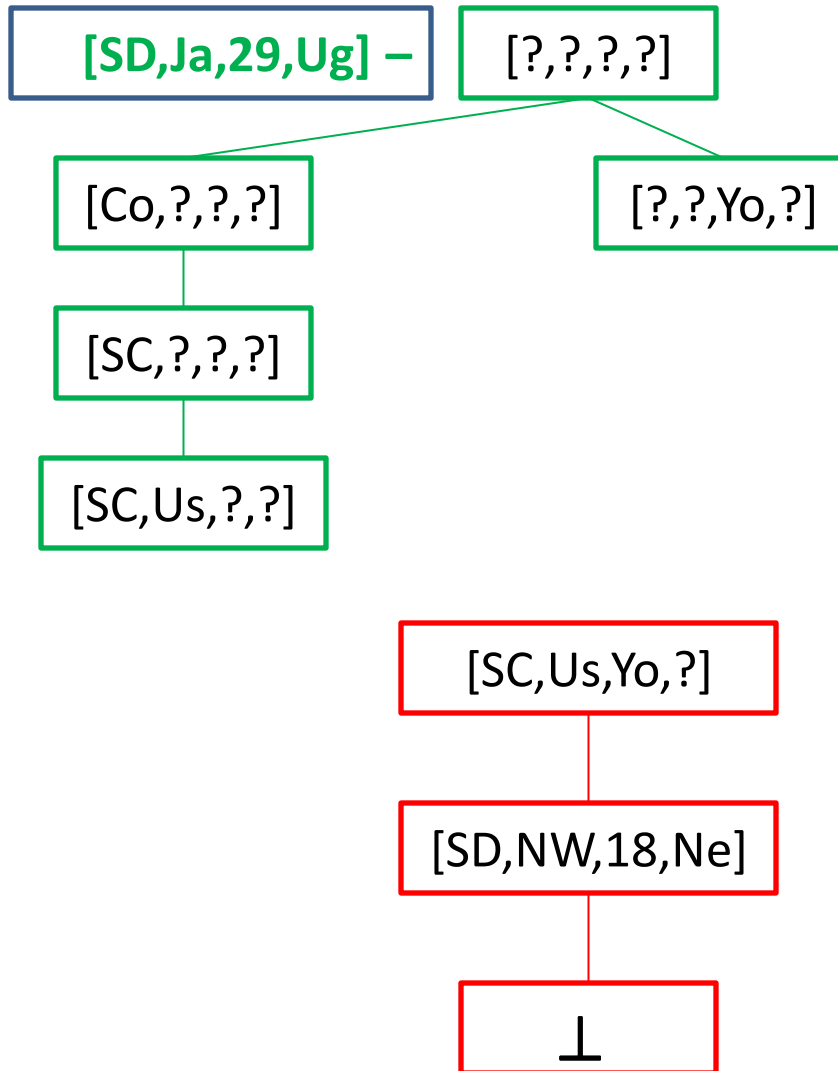
# Version-Spaces Algorithm



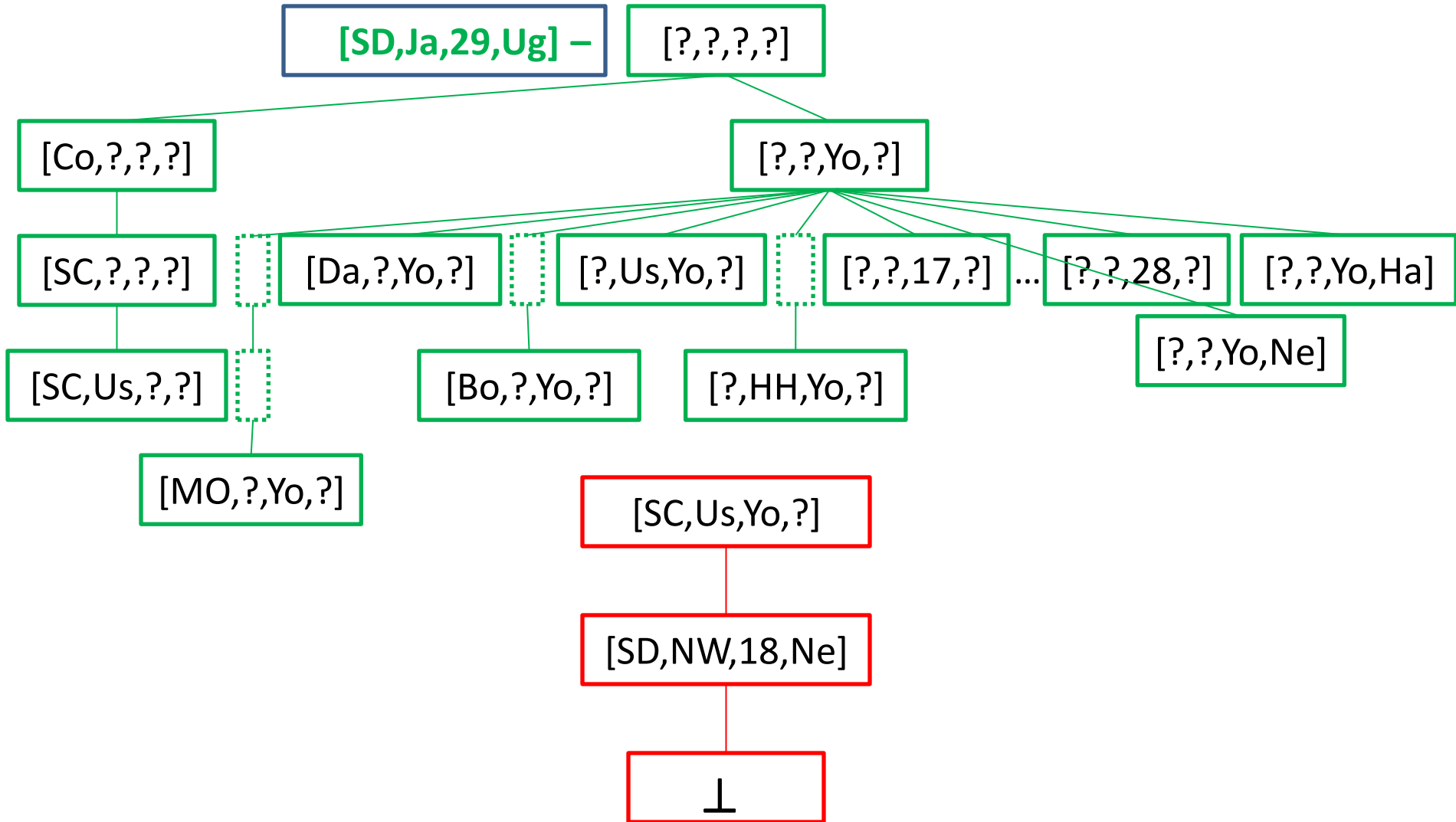
# Version-Spaces Algorithm



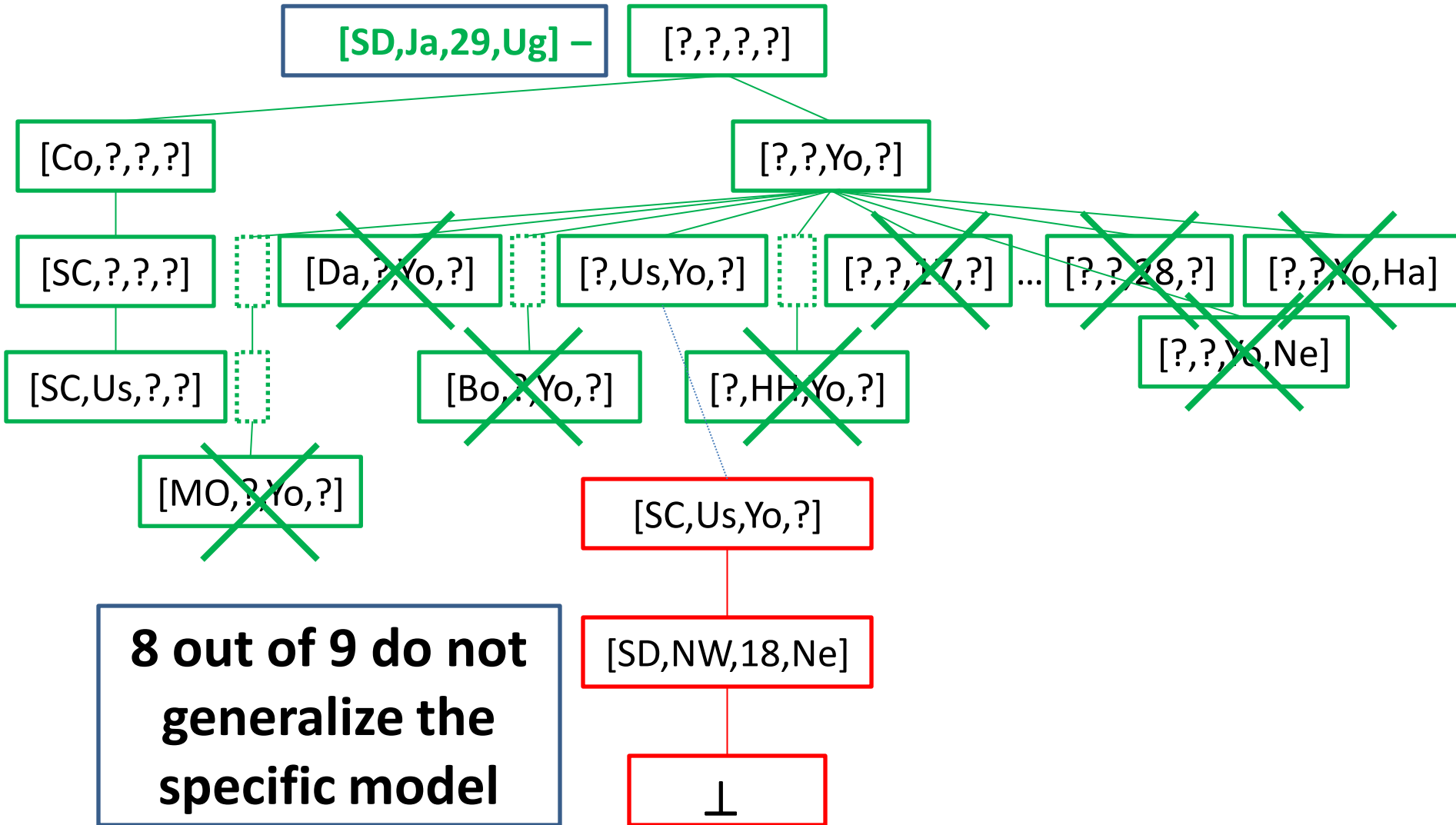
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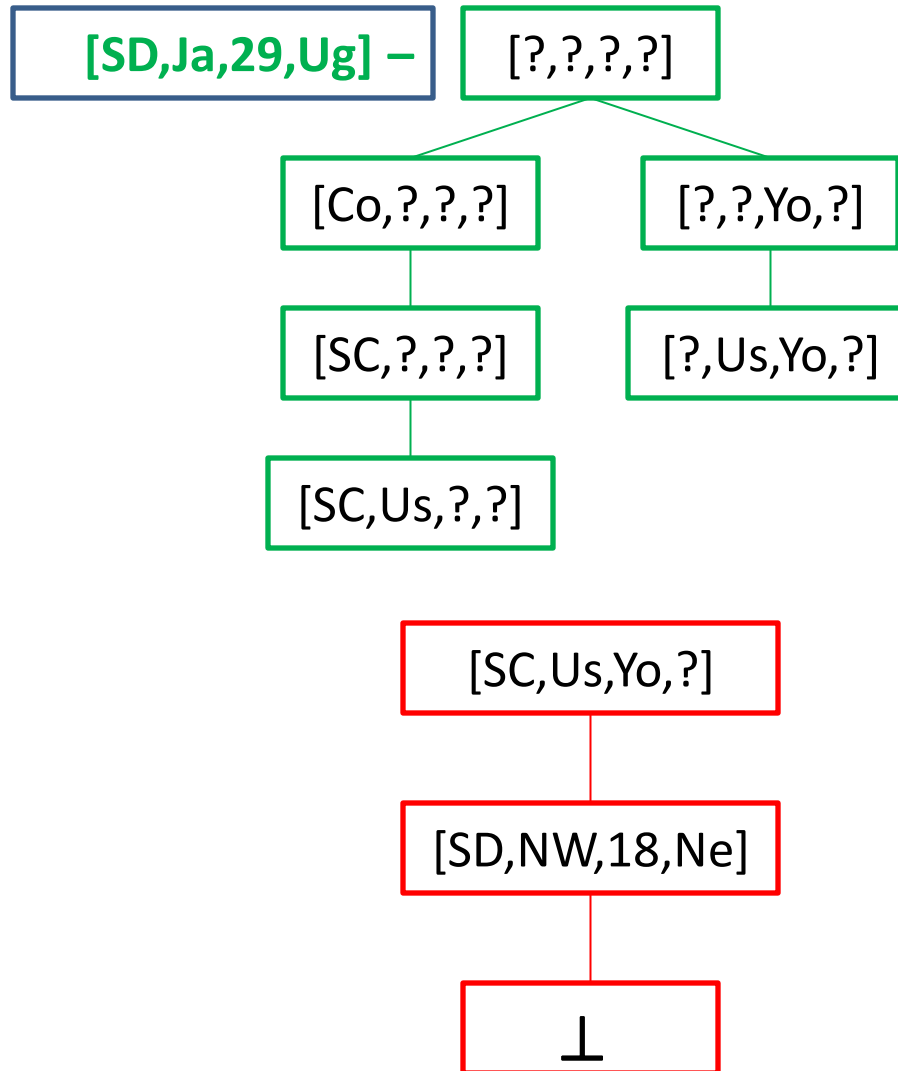
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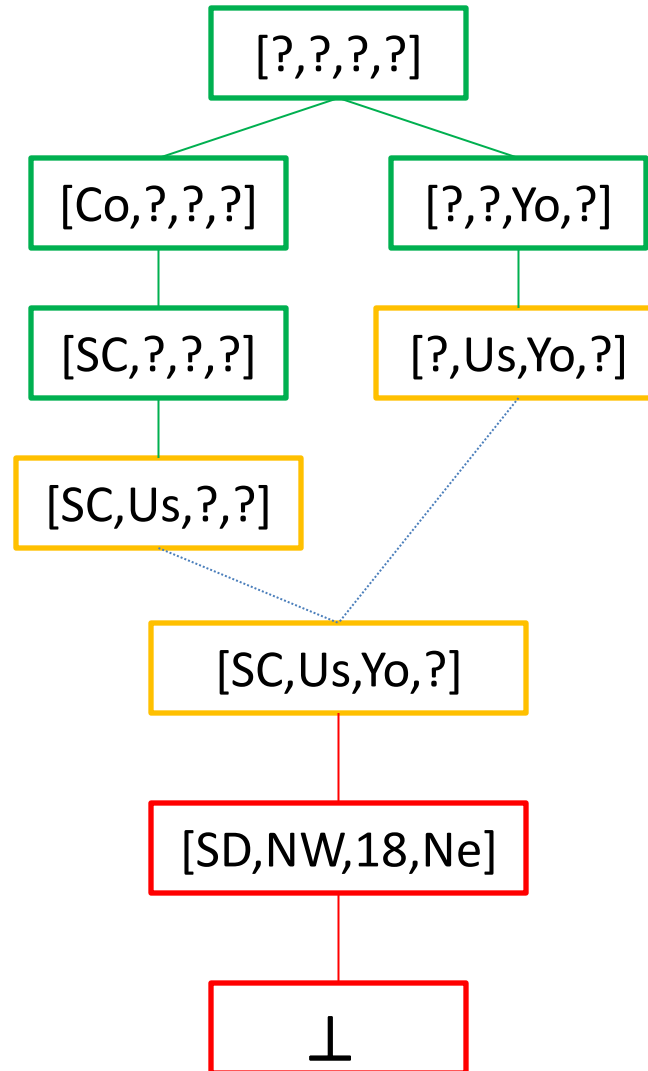
# Version-Spaces Algorithm



# Version-Spaces Algorithm



# Version-Spaces Algorithm

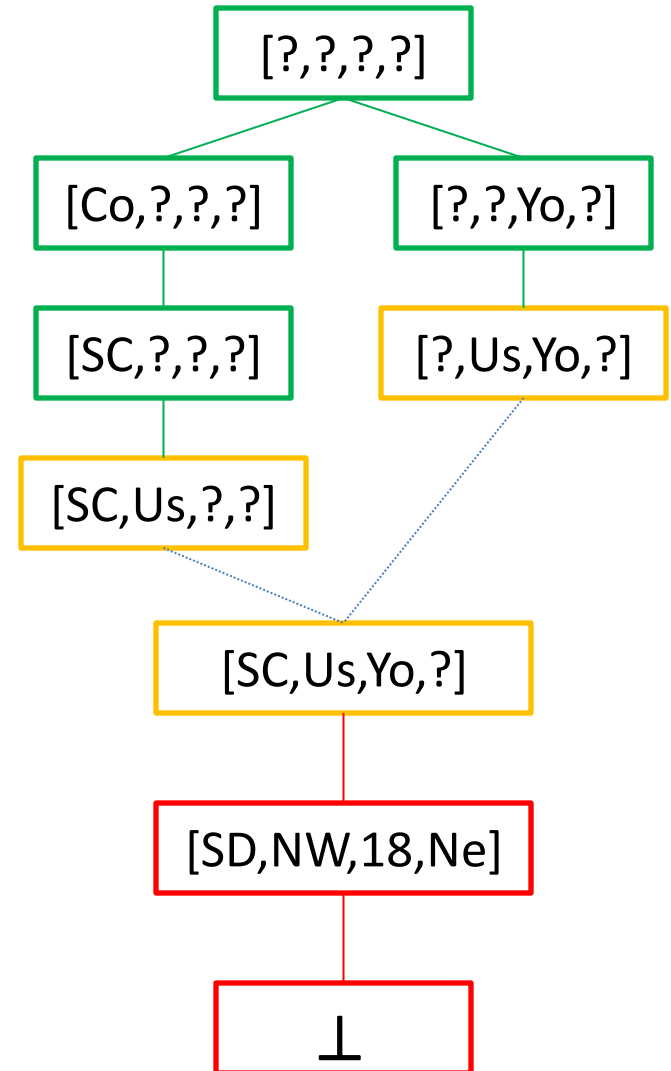


Version Spaces: Ex-exam

# **USING THE RESULT**

# Using the result

- [MO,HR,32,Ha]: **Maybe**
  - More Specific than [SC,Us,?,?]
  - Not more Specific than [SC,Us,Yo,?]
- [SD,HH,18,Ne]: **NO**
  - Not More Specific than [SC,Us,?,?]
  - Not More Specific than [?,Us,Yo,?]
- [Da,NW,22,Ug]: **Maybe**
  - More Specific than [?,Us,Yo,?]
  - Not more Specific than [SC,Us,Yo,?]



# Exercises: Artificial Intelligence

Version Spaces: Computer Screen

Version Spaces: Computer Screen

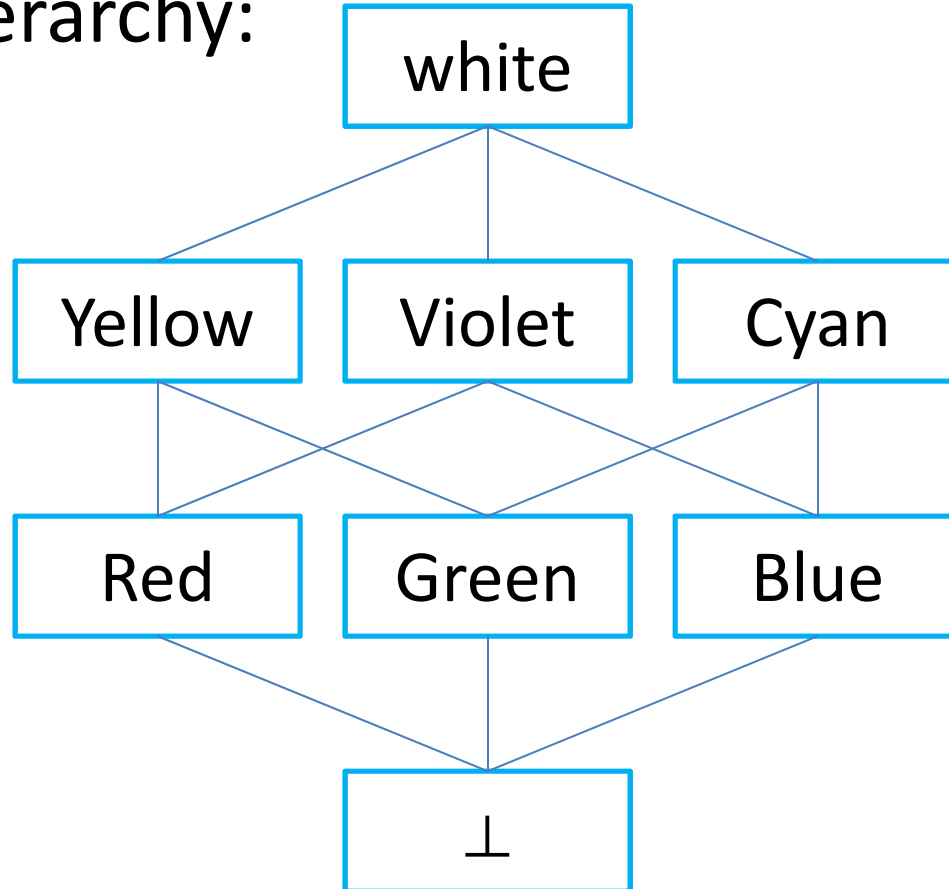
# **PROBLEM**

# Problem

- Computer Screen 6x6 pixels
  - Only colored squares can be shown:
    - $[(x,y),n,color]$ 
      - $(x,y)$ : coordinates from bottom-left corner
      - $n > 0$ : length of sides
  - Squares appear on the screen by examples
    - Give to the screen:
      - squares that should be lit
      - squares that shouldn't be lit
  - Which square is shown? Use Version Spaces.

# Problem

- Color hierarchy:



# Problem

- ***Examples:***

Location	Color	Lit?
(0,1)	Red	No
(3,2)	Red	Yes
(1,4)	Green	Yes
(4,5)	Red	No
(4,0)	green	No

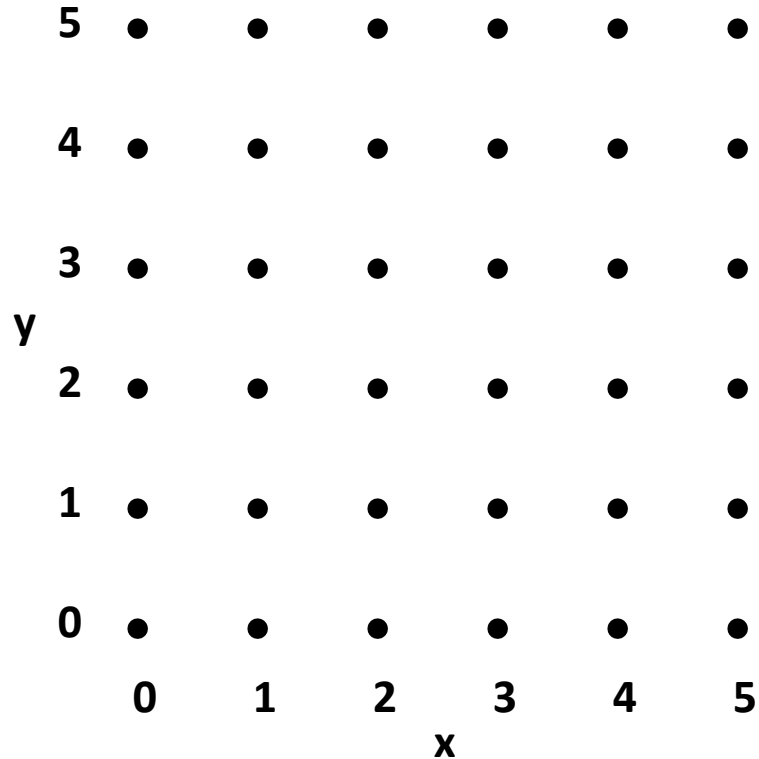
Version Spaces: Computer Screen

# **VERSION-SPACES ALGORITHM**

# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}\}$

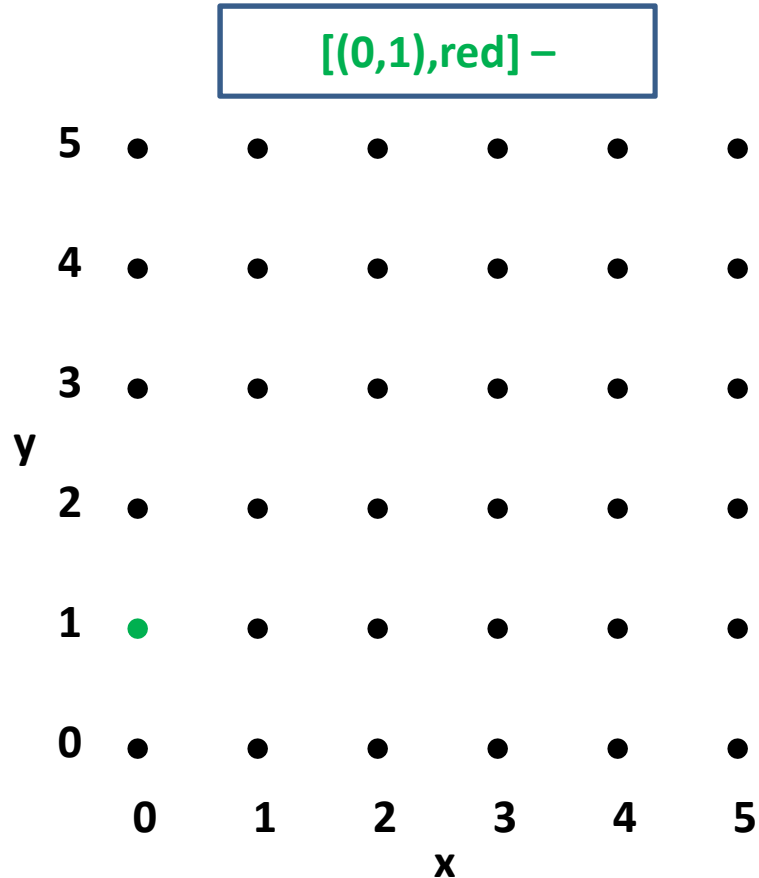
$S = \{\perp\}$



# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}\}$

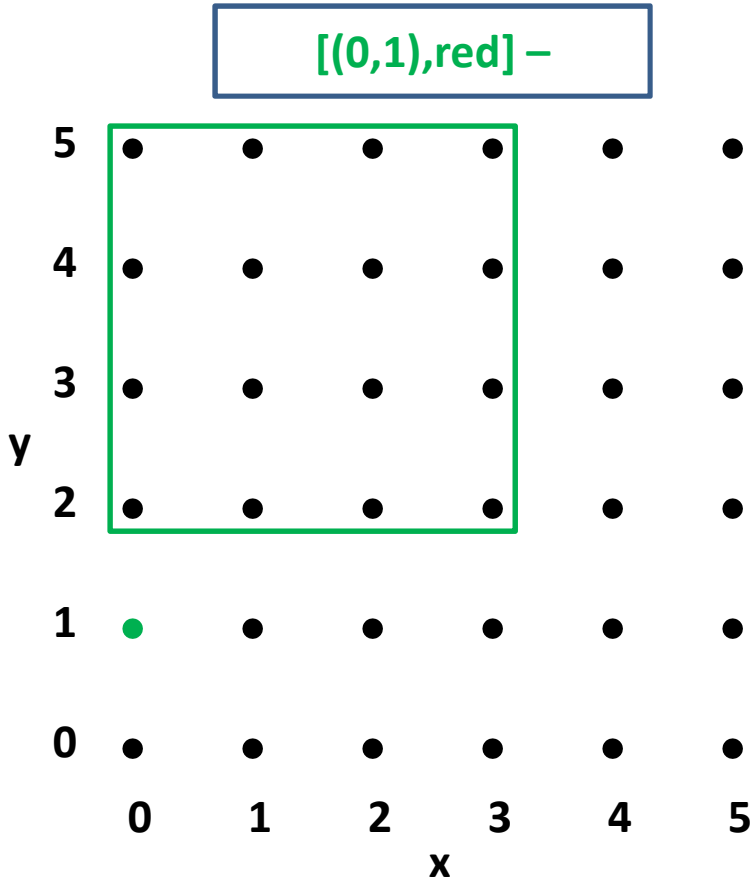
$S = \{\perp\}$



# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}\}$

$S = \{\perp\}$

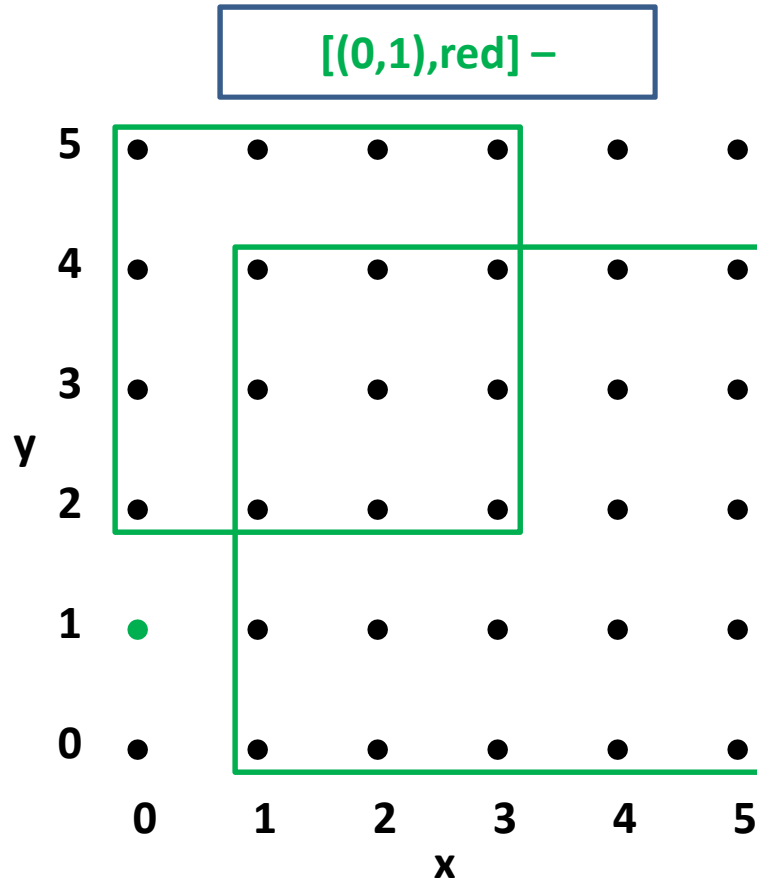


$G = \{$   
 $[(0,2),3], \text{white}]$   
 $\}$   
 $S = \{\perp\}$

# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}\}$

$S = \{\perp\}$

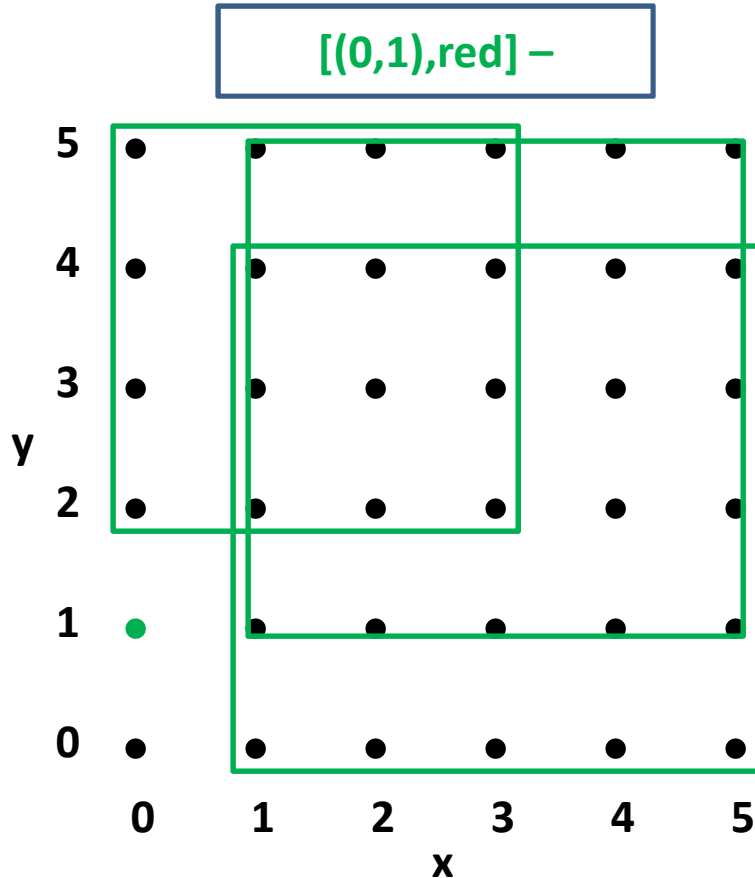


$G = \{$   
     $[(0,2),3], \text{white},$   
     $[(1,0),4], \text{white}$   
 $\}$   
 $S = \{\perp\}$

# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}]\}$

$S = \{\perp\}$



$G = \{$

$[(0,2),3], \text{white},$   
 $[(1,0),4], \text{white},$   
 $[(1,1),4], \text{white}$

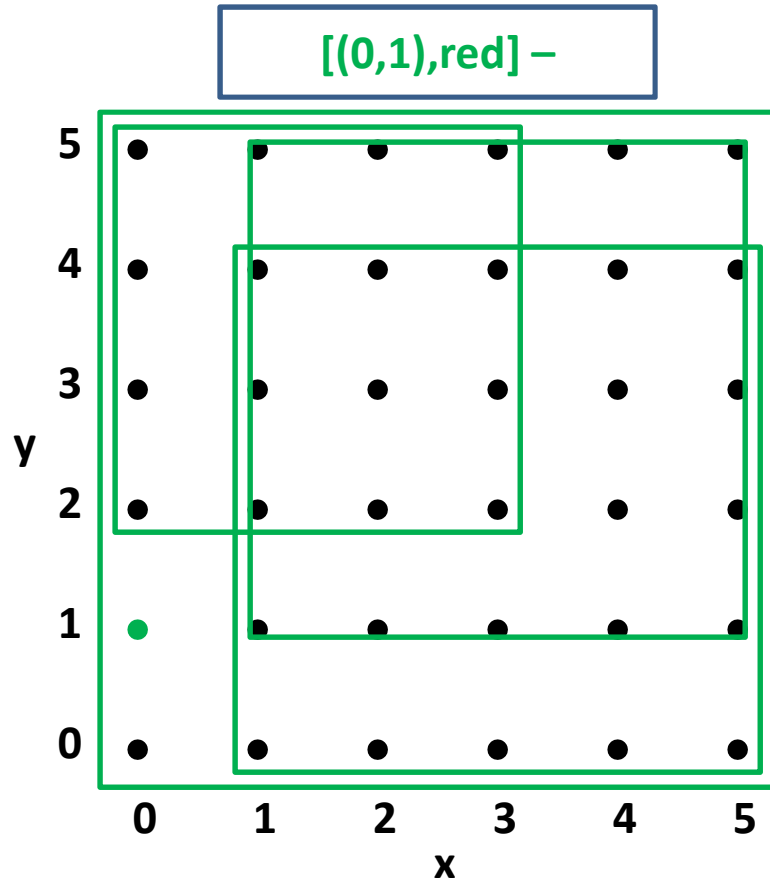
$\}$

$S = \{\perp\}$

# Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}\}$

$S = \{\perp\}$



$G = \{$

$[(0,2),3), \text{white}],$

$[(1,0),4), \text{white}],$

$[(1,1),4), \text{white}],$

$[(0,0),5), \text{cyan}]$

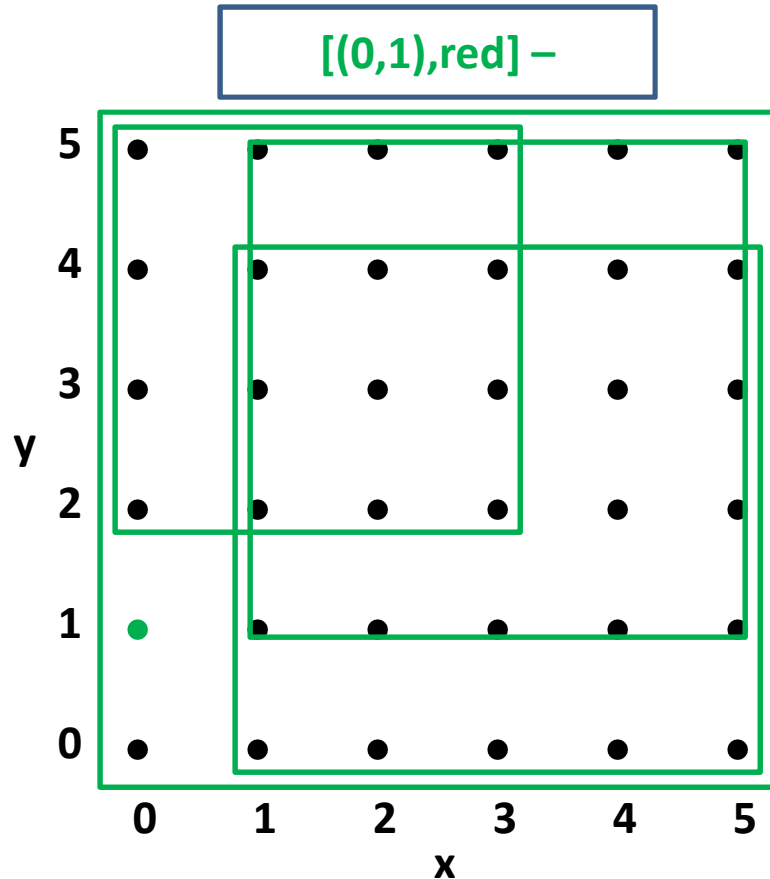
$\}$

$S = \{\perp\}$

# Version-Spaces Algorithm

$G = \{[(0,0),5],\text{white}]\}$

$S = \{\perp\}$



$G = \{$   
     $[(0,2),3],\text{white},$   
     $[(1,0),4],\text{white},$   
     $[(1,1),4],\text{white},$   
     $[(0,0),5],\text{cyan}$   
 $\}$

Redundant:

$[(0,0),5],\text{green}$

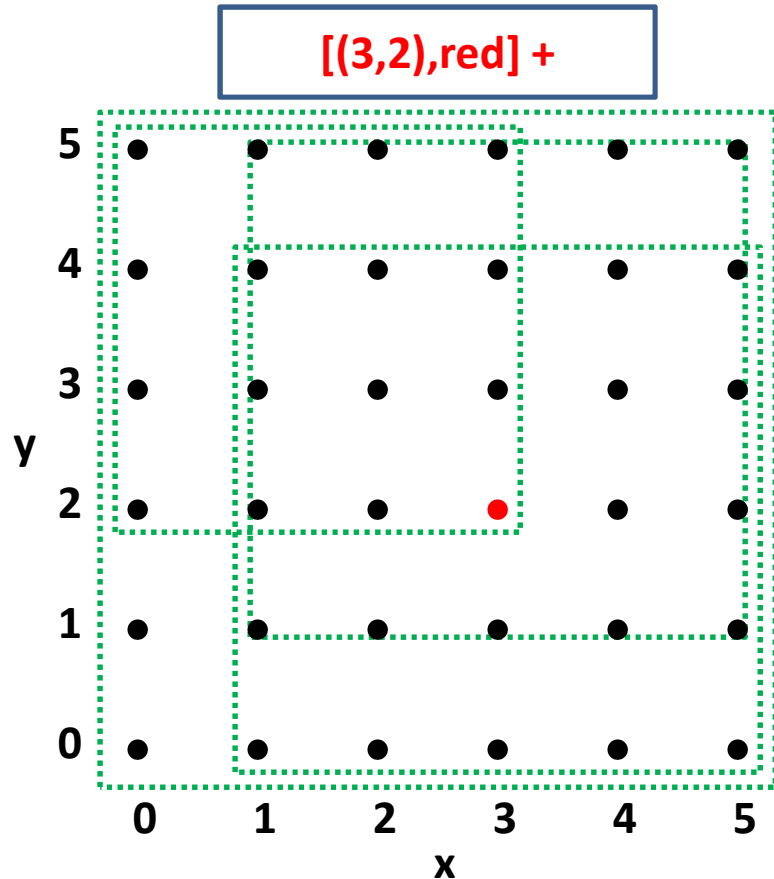
$[(0,0),5],\text{blue}$

$S = \{\perp\}$

# Version-Spaces Algorithm

$G = \{[(0,2),3,white],[(1,0),4,white],[(1,1),4,white],[(0,0),5,cyan]\}$

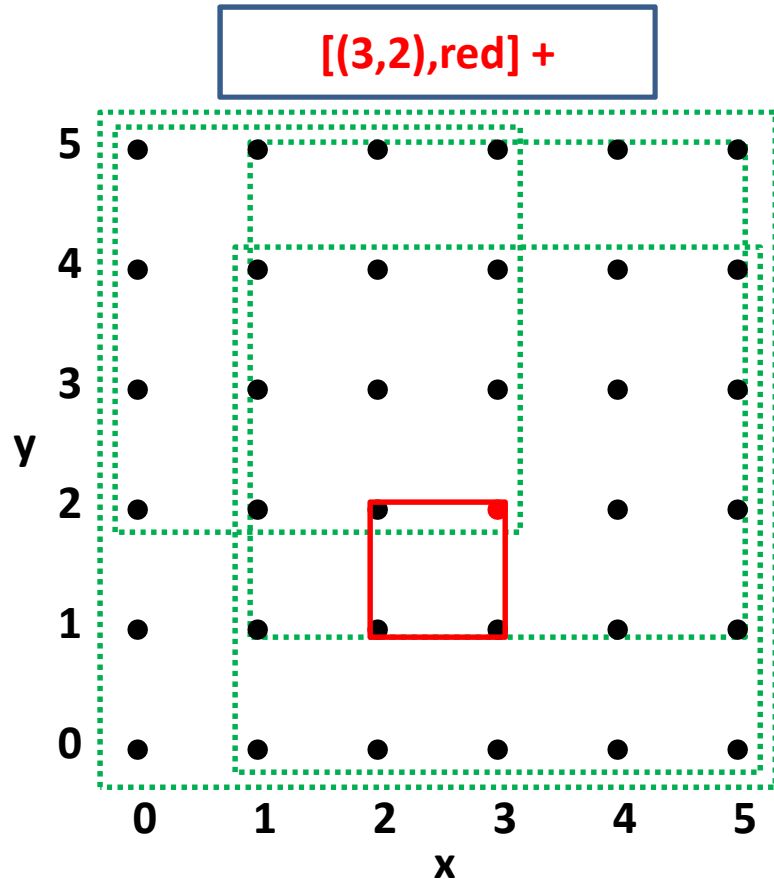
$S = \{\perp\}$



# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white], [((0,0),5),cyan] \}$

$S = \{ \perp \}$



$G = \{$

$[((0,2),3),white],$   
 $[((1,0),4),white],$   
 $[((1,1),4),white],$   
 $[((0,0),5),cyan]$

$\}$   
 $S = \{$

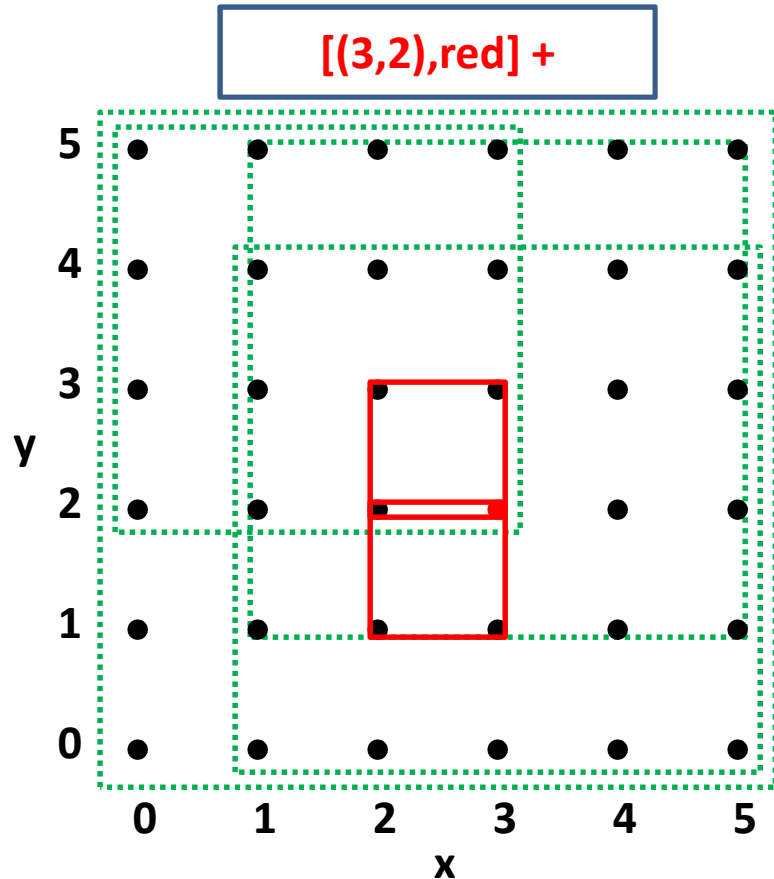
$[((2,1),1),red]$

$\}$

# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white], [((0,0),5),cyan] \}$

$S = \{ \perp \}$



$G = \{$

$[((0,2),3),white],$   
 $[((1,0),4),white],$   
 $[((1,1),4),white],$   
 $[((0,0),5),cyan]$

$\}$   
 $S = \{$

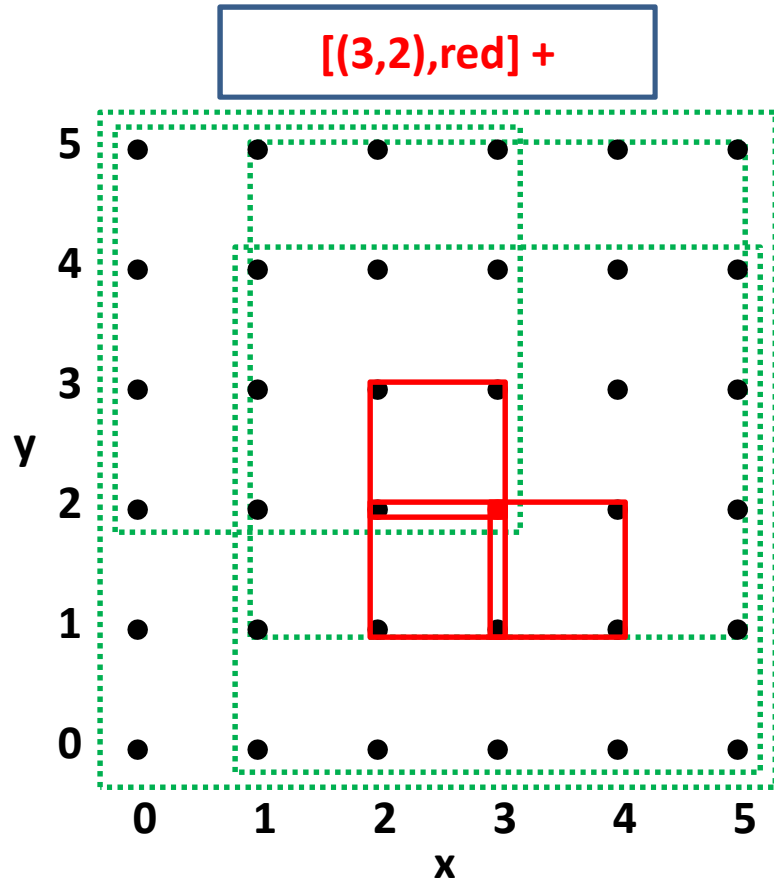
$[((2,1),1),red],$   
 $[((2,2),1),red]$

$\}$

# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white], [((0,0),5),cyan] \}$

$S = \{ \perp \}$



$G = \{$

$[((0,2),3),white],$   
 $[((1,0),4),white],$   
 $[((1,1),4),white],$   
 $[((0,0),5),cyan]$

$\}$

$S = \{$

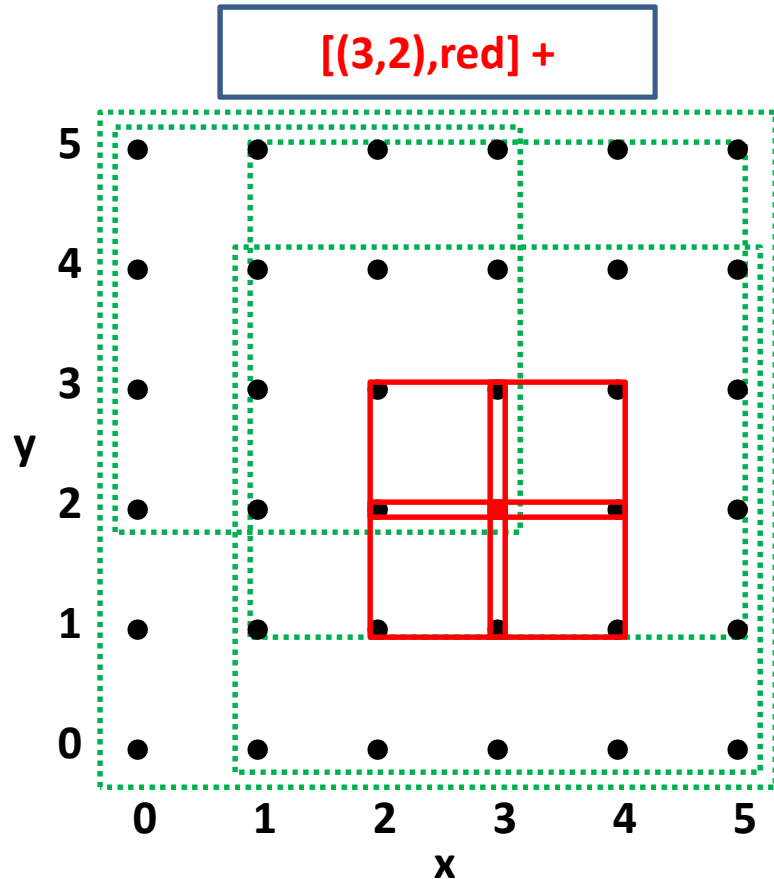
$[((2,1),1),red],$   
 $[((2,2),1),red],$   
 $[((3,1),1),red]$

$\}$

# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white], [((0,0),5),cyan] \}$

$S = \{ \perp \}$



$G = \{$

$[((0,2),3),white],$   
 $[((1,0),4),white],$   
 $[((1,1),4),white],$   
 $[((0,0),5),cyan]$

$\}$

$S = \{$

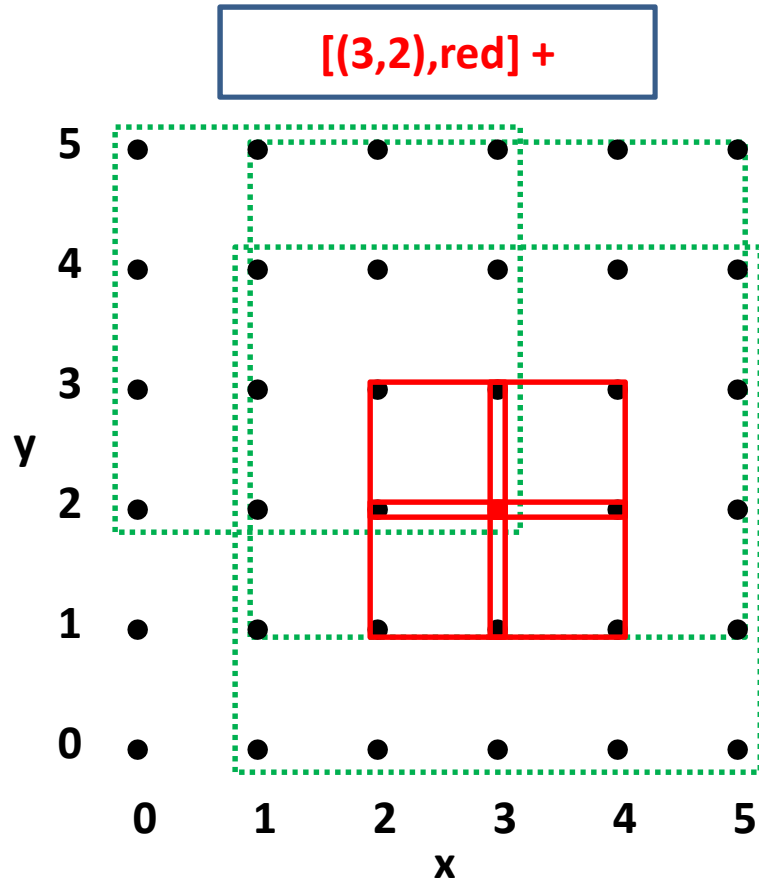
$[((2,1),1),red],$   
 $[((2,2),1),red],$   
 $[((3,1),1),red],$   
 $[((3,2),1),red]$

$\}$

# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white], [((0,0),5),cyan] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),white],$   
 $[((1,0),4),white],$   
 $[((1,1),4),white]$

$\}$

Removed:

$[((0,0),5),cyan]$

$S = \{$

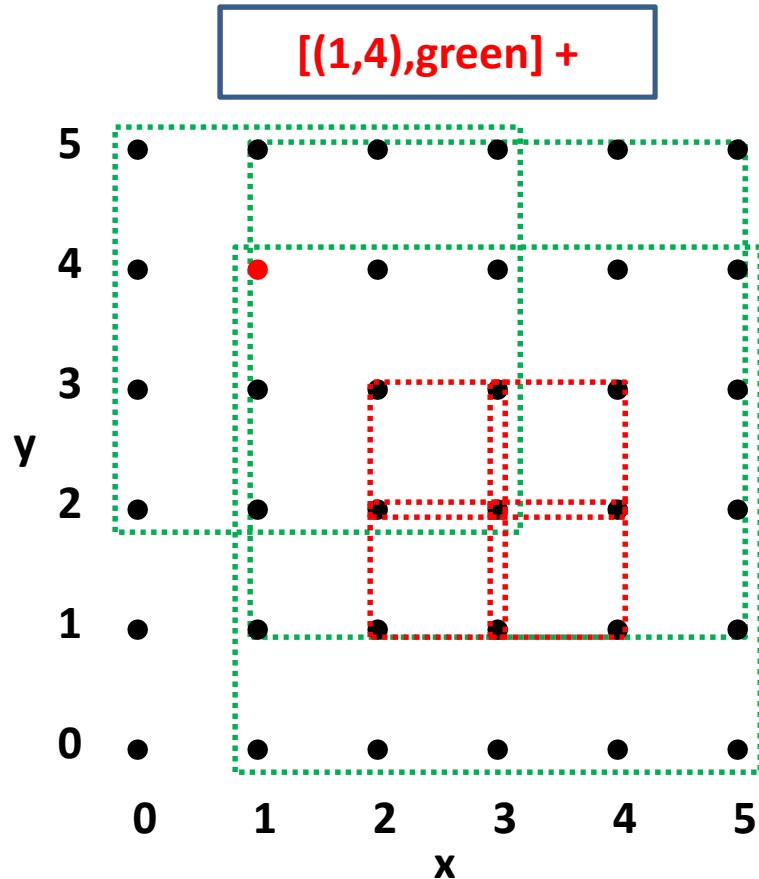
$[((2,1),1),red],$   
 $[((2,2),1),red],$   
 $[((3,1),1),red],$   
 $[((3,2),1),red]$

$\}$

# Version-Spaces Algorithm

$G = \{[(0,2),3,white],[(1,0),4,white],[(1,1),4,white]\}$

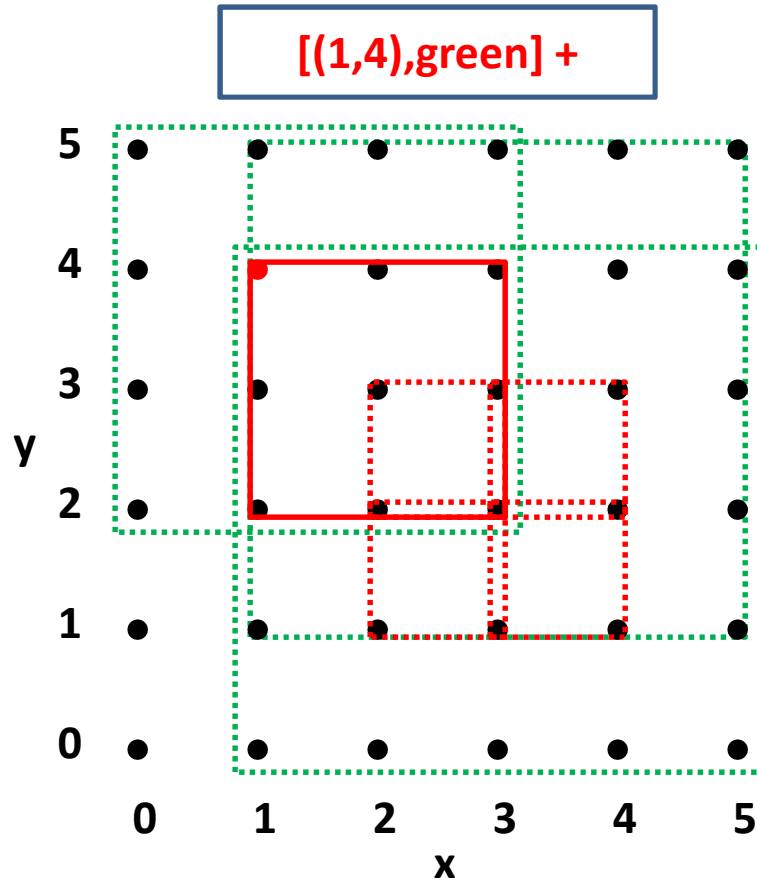
$S = \{[(2,1),1,red],[(2,2),1,red],[(3,1),1,red],[(3,2),1,red]\}$



# Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}] \}$



$G = \{$

$[((0,2),3),\text{white}],$   
 $[((1,0),4),\text{white}],$   
 $[((1,1),4),\text{white}]$

$\}$

$S = \{$

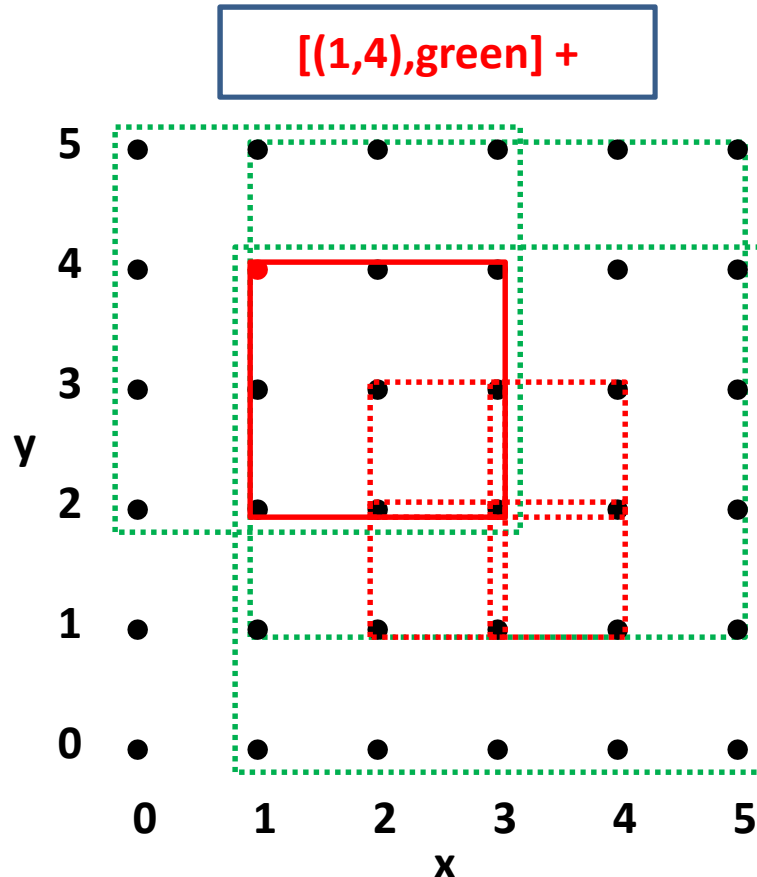
$[((1,2),2),\text{yellow}]$

$\}$

# Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}] \}$



$G = \{$

$[((0,2),3),\text{white}],$   
 $[((1,0),4),\text{white}],$   
 $[((1,1),4),\text{white}]$

$\}$

$S = \{$

$[((1,2),2),\text{yellow}]$

$\}$

Redundant:

$[((0,2),3),\text{yellow}]$

$[((1,2),3),\text{yellow}]$

$[((1,1),3),\text{yellow}]$

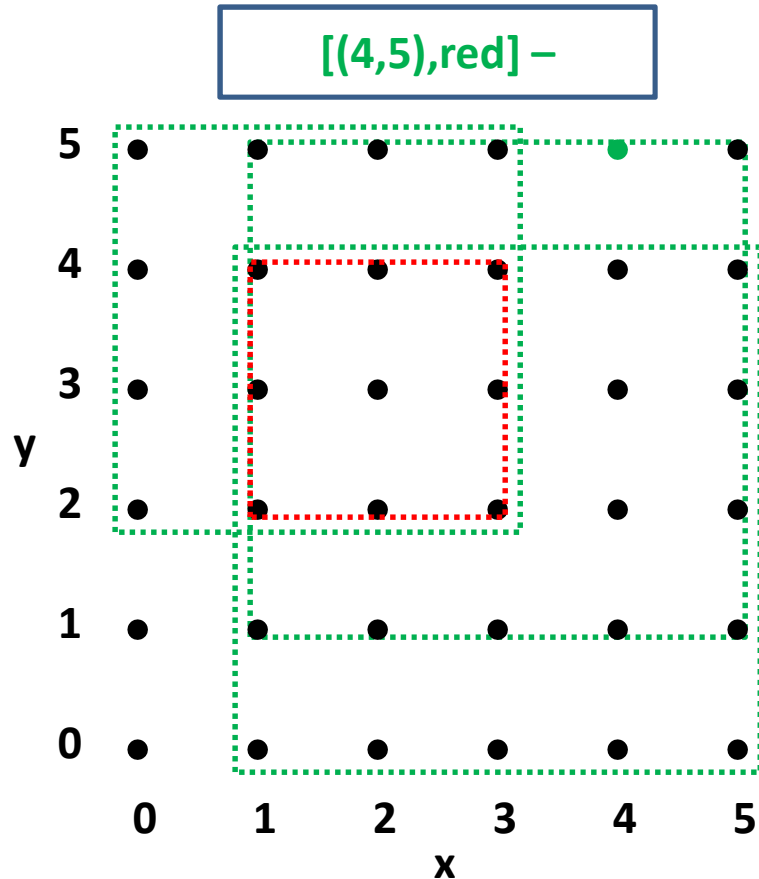
$[((1,1),4),\text{yellow}]$

$[((1,0),4),\text{yellow}]$

# Version-Spaces Algorithm

$G = \{[(0,2),3,white],[(1,0),4,white],[(1,1),4,white]\}$

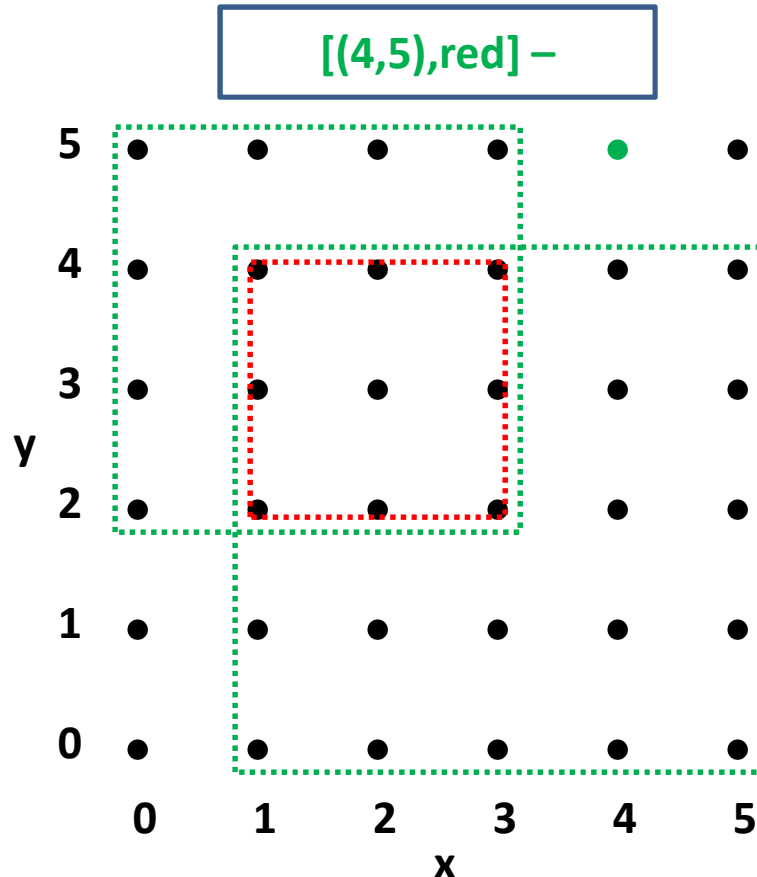
$S = \{[(1,2),2,yellow]\}$



# Version-Spaces Algorithm

$G = \{ [((0,2),3),white], [((1,0),4),white], [((1,1),4),white] \}$

$S = \{ [((1,2),2),yellow] \}$



$G = \{$   
     $[((0,2),3),white],$   
     $[((1,0),4),white]$   
 $\}$

Redundant:

$[((1,1),3),white]$

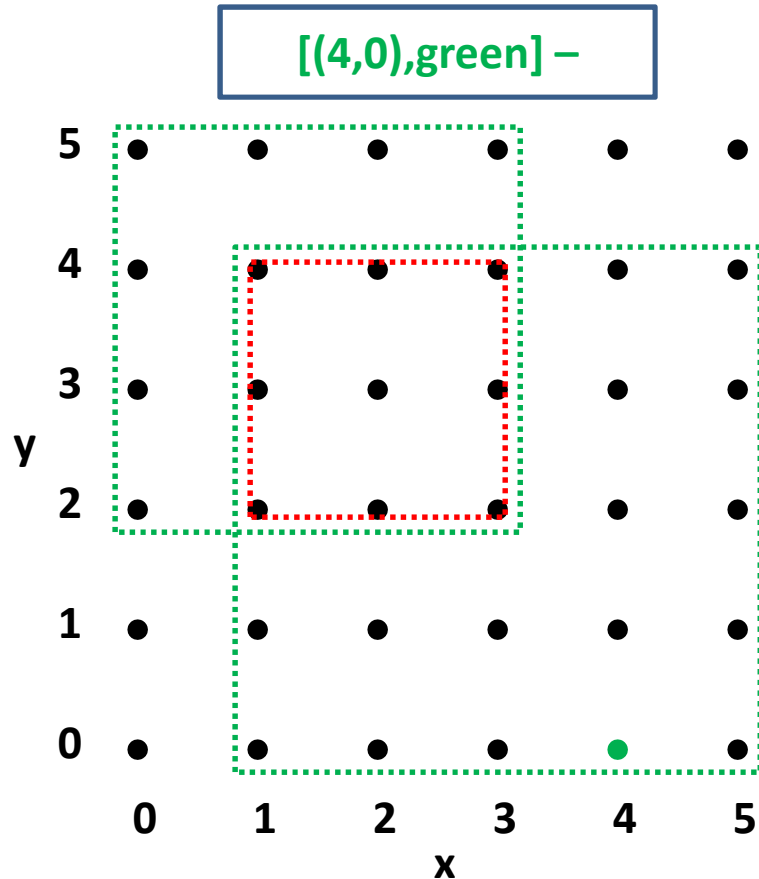
Others don't generalize S

$S = \{$   
     $[((1,2),2),yellow]$   
 $\}$

# Version-Spaces Algorithm

$G = \{[(0,2),3,white],[(1,0),4,white]\}$

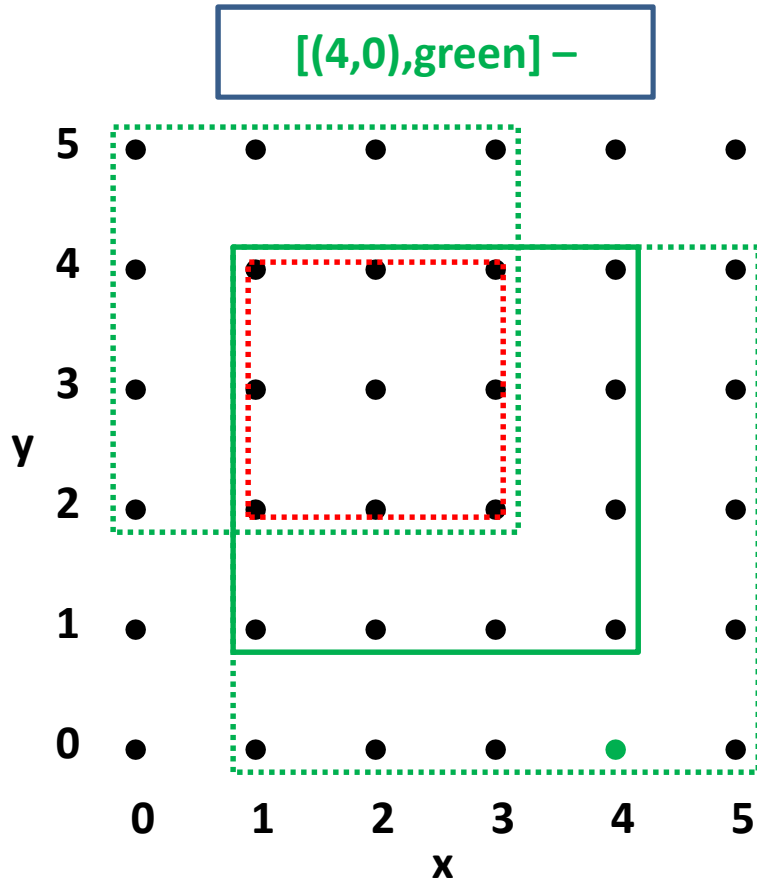
$S = \{[(1,2),2,yellow]\}$



# Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$

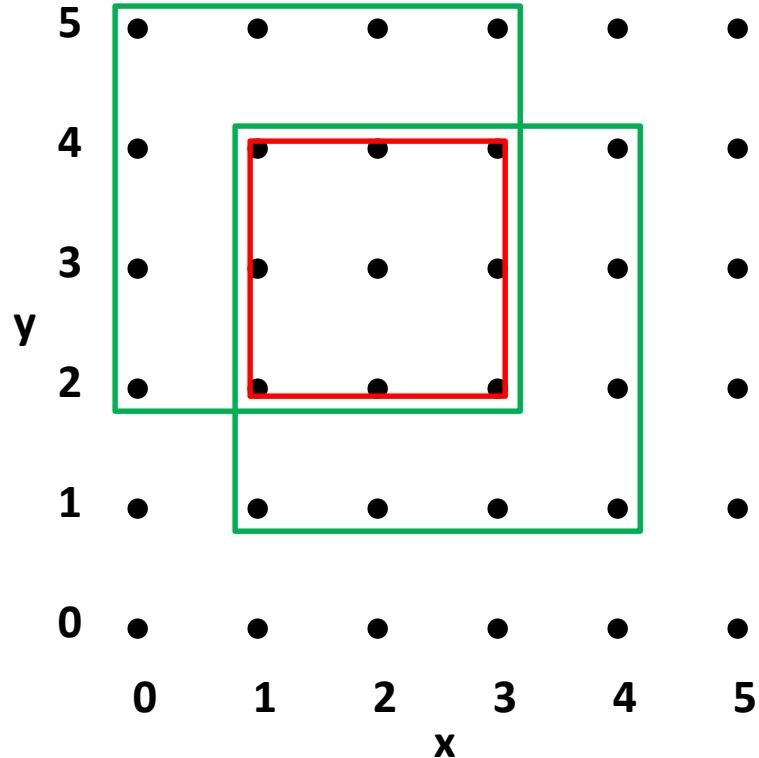


$G = \{$   
     $[((0,2),3),\text{white}],$   
     $[((1,1),3),\text{white}]$   
 $\}$   
Others don't generalize  $S$   
 $S = \{$   
     $[((1,2),2),\text{yellow}]$   
 $\}$

# Version-Spaces Algorithm

$G = \{[(0,2),3,white],[(1,1),3,white]\}$

$S = \{[(1,2),2,yellow]\}$



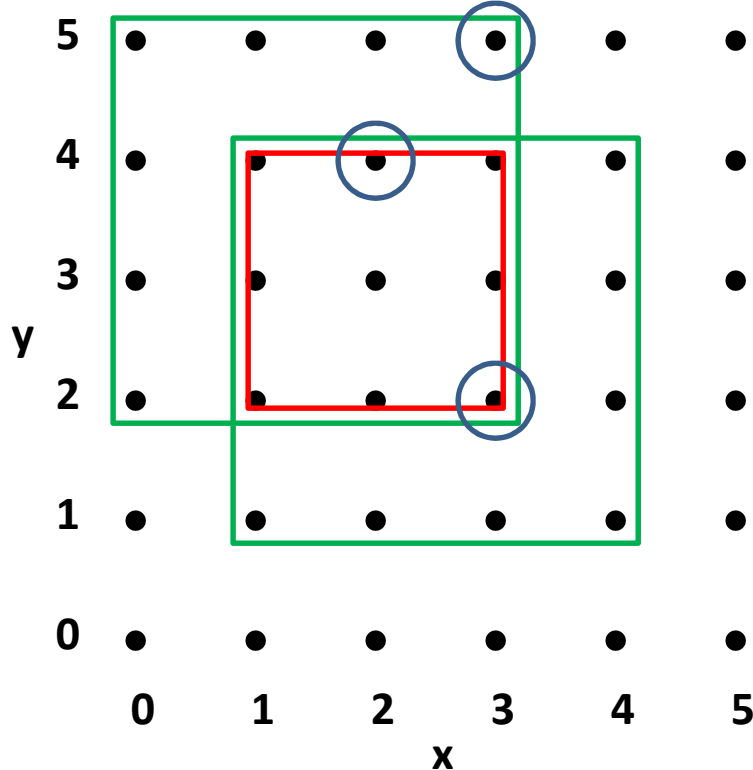
Version Spaces: Ex-exam

# **USING THE RESULT**

# Using the Result

$G = \{[(0,2),3,white],[(1,1),3,white]\}$

$S = \{[(1,2),2,yellow]\}$



$[(3,2),green]$

Yes

$[(2,4),red]$

Yes

$[(3,5),blue]$

Maybe