

# Exercises: Artificial Intelligence

Planning & Logic: Blocks world

Planning & Logic: Blocks world

# PROBLEM

# Problem

- **Table: T & Blocks: A,B,C,D**
- **Apply STRIPS on:**
  - **Initial State, I:**
    - clear(A), clear(B), clear(C), clear(D),  
on(A,T), on(B,T), on(C,T), on(D,T)
  - **Final State, F:**
    - on(A,T), on(B,A), on(C,B), on(D,C), clear(D)
- **Indicate:** *Establish & Threaten*
- **Give:** *Before relation without loops*

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# **INITIAL & FINAL STATE**

# Initial & Final State

<b>If</b>	
<b>Add</b>	on(A,T) on(B,T) on(C,T) on(D,T) clear(A) clear(B) clear(C) clear(D)
<b>Del</b>	

<b>If</b>	on(A,T) on(B,A) on(C,B) on(D,C) clear(D)
<b>Add</b>	
<b>Del</b>	

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# **OPERATORS**

# Operators

<b>Operator 1</b>	
<b>If</b>	on(x,y) clear(x) clear(z)
<b>Add</b>	on(x,z) clear(y)
<b>Del</b>	on(x,y) clear(z)

<b>Operator 2</b>	
<b>If</b>	on(x,y) clear(x)
<b>Add</b>	on(x,T) clear(y)
<b>Del</b>	on(x,y)

<b>Operator 3</b>	
<b>If</b>	on(x,T) clear(x) clear(z)
<b>Add</b>	on(x,z)
<b>Del</b>	on(x,T) clear(z)

**Actual operators are ground instances!**

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# **STRIPS**

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
clear(D)	
<b>Del</b>	

$B(I,F)$

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

# STRIPS

I	
<b>If</b>	
<b>Add</b>	on(A,T) on(B,T) on(C,T) on(D,T) clear(A) clear(B) clear(C) clear(D)
<b>Del</b>	

O31 (x/B,z/A)	
<b>If</b>	on(B,T) clear(A) clear(B)
<b>Add</b>	on(B,A)
<b>Del</b>	on(B,T) clear(A)

F	
<b>If</b>	on(A,T) on(B,A) on(C,B) on(D,C) clear(D)
<b>Add</b>	
<b>Del</b>	

$B(I,F)$

$B(O31,F)$



Establishes



Threatens

Before constraint:

$B(x,y)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

O31 (x/B,z/A)	
If	
<b>If</b>	on(B,T)
	clear(A)
	clear(B)
<b>Add</b>	on(B,A)
<b>Del</b>	on(B,T) clear(A)

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	

B(I,F)

B(I,O31)

B(I,O31)

B(I,O31)

B(O31,F)



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

**O31** (x/B,z/A)

F	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	

B(I,O31)

B(I,F)

B(O31,F)



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
clear(D)	
<b>Del</b>	

<b>O31</b>	(x/B,z/A)
------------	-----------

<b>O32</b>	(x/C,z/B)
------------	-----------

If	
	on(C,T)
	clear(B)
	clear(C)

<b>Add</b>	on(C,B)
------------	---------

<b>Del</b>	on(C,T)
	clear(B)

F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	

$B(I,O31)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$



Establishes



Threatens

Before constraint:

$B(x,y)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

<b>O31</b> (x/B,z/A)	
<b>O32</b> (x/C,z/B)	
<b>If</b>	on(C,T)
	clear(B)
	clear(C)
<b>Add</b>	on(C,B)
<b>Del</b>	on(C,T)
	clear(B)

F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

<b>O31</b>	(x/B,z/A)
------------	-----------

<b>O32</b>	(x/C,z/B)
------------	-----------

<b>If</b>	on(C,T)
	clear(B)
	clear(C)

<b>Add</b>	on(C,B)
------------	---------

<b>Del</b>	on(C,T)
	clear(B)

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

$B(O31,O32) \vee B(O32,I)$

# STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31	(x/B,z/A)
-----	-----------

O32	(x/C,z/B)
-----	-----------

If	on(C,T)
	clear(B)
	clear(C)

Add	on(C,B)
-----	---------

Del	on(C,T)
	clear(B)

F	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

$B(O31,O32) \vee B(O32,I)$  ← Loop!

Before constraint:

$B(x,y)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

$B(I,O31)$

$B(I,O32)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

**O31** (x/B,z/A)

**O32** (x/C,z/B)

$B(O31,O32)$

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$



# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
<b>Add</b>	
<b>Del</b>	

<b>O31</b> (x/B,z/A)
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<b>O32</b> (x/C,z/B)
----------------------

<b>O33</b> (x/D,z/C)
----------------------

<b>If</b>	on(D,T) clear(C) clear(D)
-----------	---------------------------------

<b>Add</b>	on(D,C)
------------	---------

<b>Del</b>	on(D,T) clear(C)
------------	---------------------



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$



$B(O31,O32)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

$B(O33,F)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

<b>O31</b> (x/B,z/A)
----------------------

<b>O32</b> (x/C,z/B)
----------------------

<b>O33</b> (x/D,z/C)
----------------------

<b>If</b>	on(D,T) clear(C) clear(D)
-----------	---------------------------------

<b>Add</b>	on(D,C)
------------	---------

<b>Del</b>	on(D,T) clear(C)
------------	---------------------

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$

$B(I,O33)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

$B(O31,O32)$

$B(O33,F)$

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

<b>O31</b> (x/B,z/A)
----------------------

<b>O32</b> (x/C,z/B)
----------------------

<b>O33</b> (x/D,z/C)
----------------------

<b>If</b>	on(D,T)
	clear(C)
	clear(D)

<b>Add</b>	on(D,C)
------------	---------

<b>Del</b>	on(D,T)
	clear(C)

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



Establishes

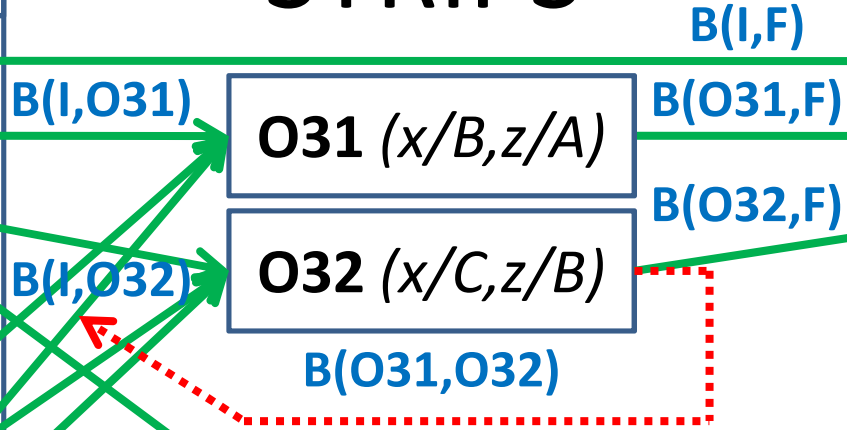


Threatens

Before constraint:

$B(x,y)$

$B(O32,O33) \vee B(O33,I)$



# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

<b>O31</b> (x/B,z/A)
----------------------

<b>O32</b> (x/C,z/B)
----------------------

<b>O33</b> (x/D,z/C)
----------------------

<b>If</b>	on(D,T)
	clear(C)
	clear(D)

<b>Add</b>	on(D,C)
------------	---------

<b>Del</b>	on(D,T)
	clear(C)

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
<b>Add</b>	
<b>Del</b>	



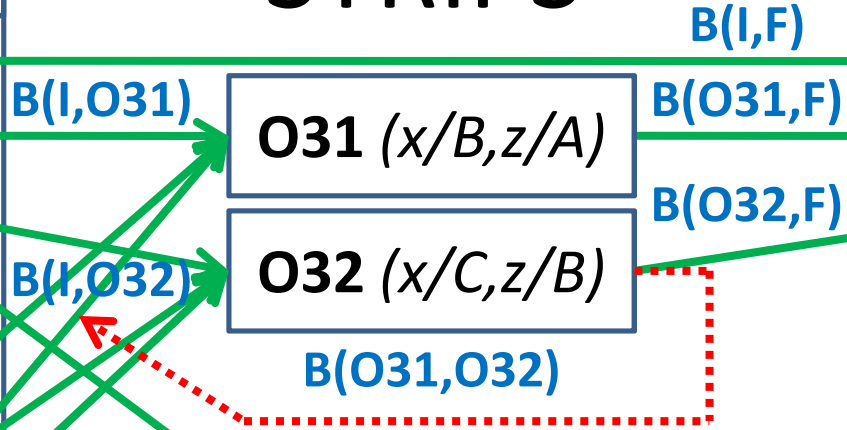
Establishes



Threatens

Before constraint:

$B(x,y)$



$B(O32,O33) \vee B(O33,I)$

**Loop!**

# STRIPS

I	
If	
<b>Add</b>	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
<b>Del</b>	

**O31** (x/B,z/A)

**O32** (x/C,z/B)

**O33** (x/D,z/C)

F	
If	
<b>If</b>	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
<b>Add</b>	
<b>Del</b>	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O31)$

$B(I,O32)$

$B(I,O33)$

$B(I,F)$

$B(O31,F)$

$B(O32,F)$

$B(O33,F)$

$B(O31,O32)$

$B(O32,O33)$

# STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
clear(D)	
Del	

F	
If	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
Add	clear(D)
Del	

$B(I, O31)$

$B(I, O32)$

$B(I, O33)$

O31 (x/B, z/A)

O32 (x/C, z/B)

O33 (x/D, z/C)

$B(O31, O32)$

$B(O32, O33)$

$B(I, F)$

$B(O31, F)$

$B(O32, F)$

$B(O33, F)$



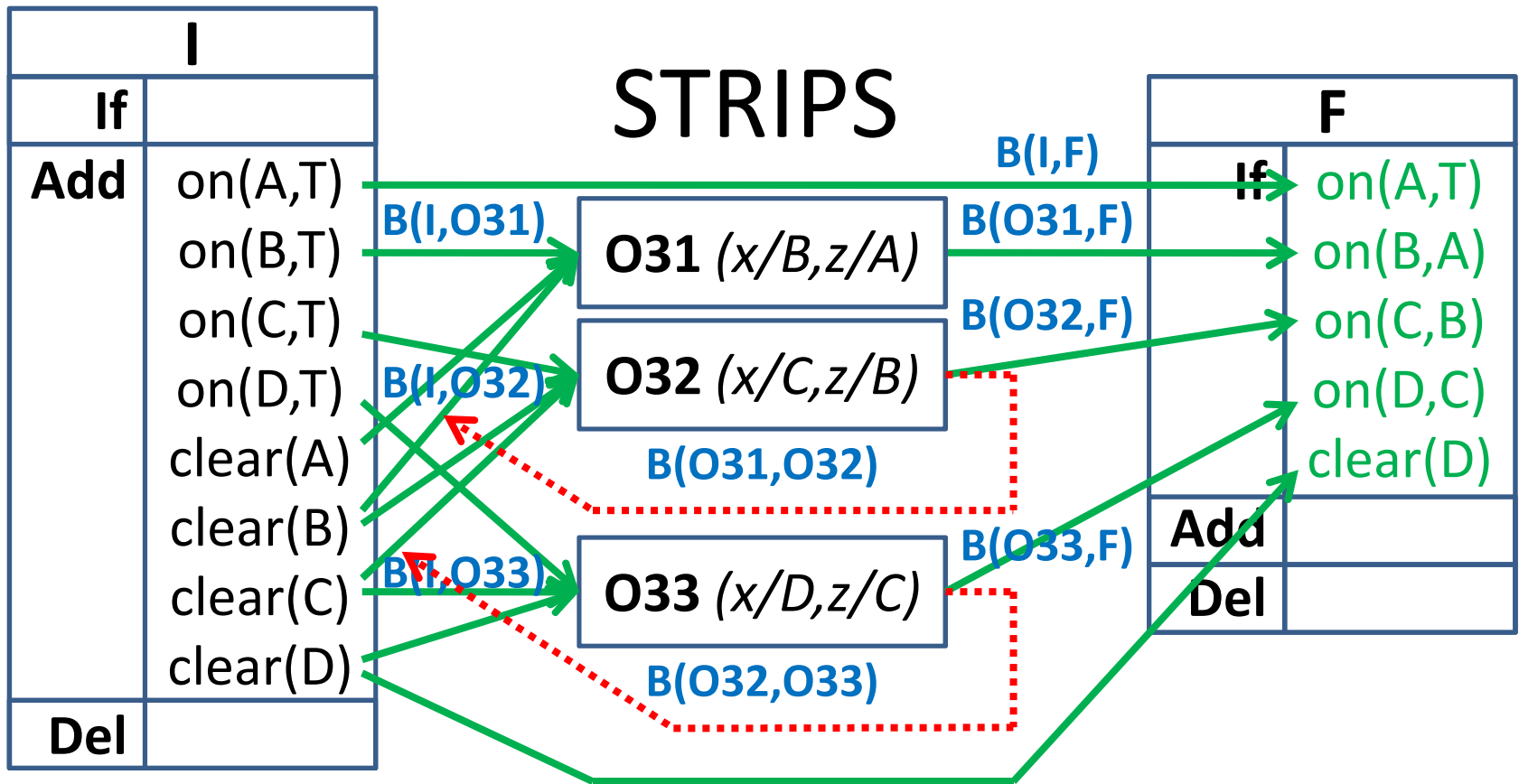
Establishes



Threatens

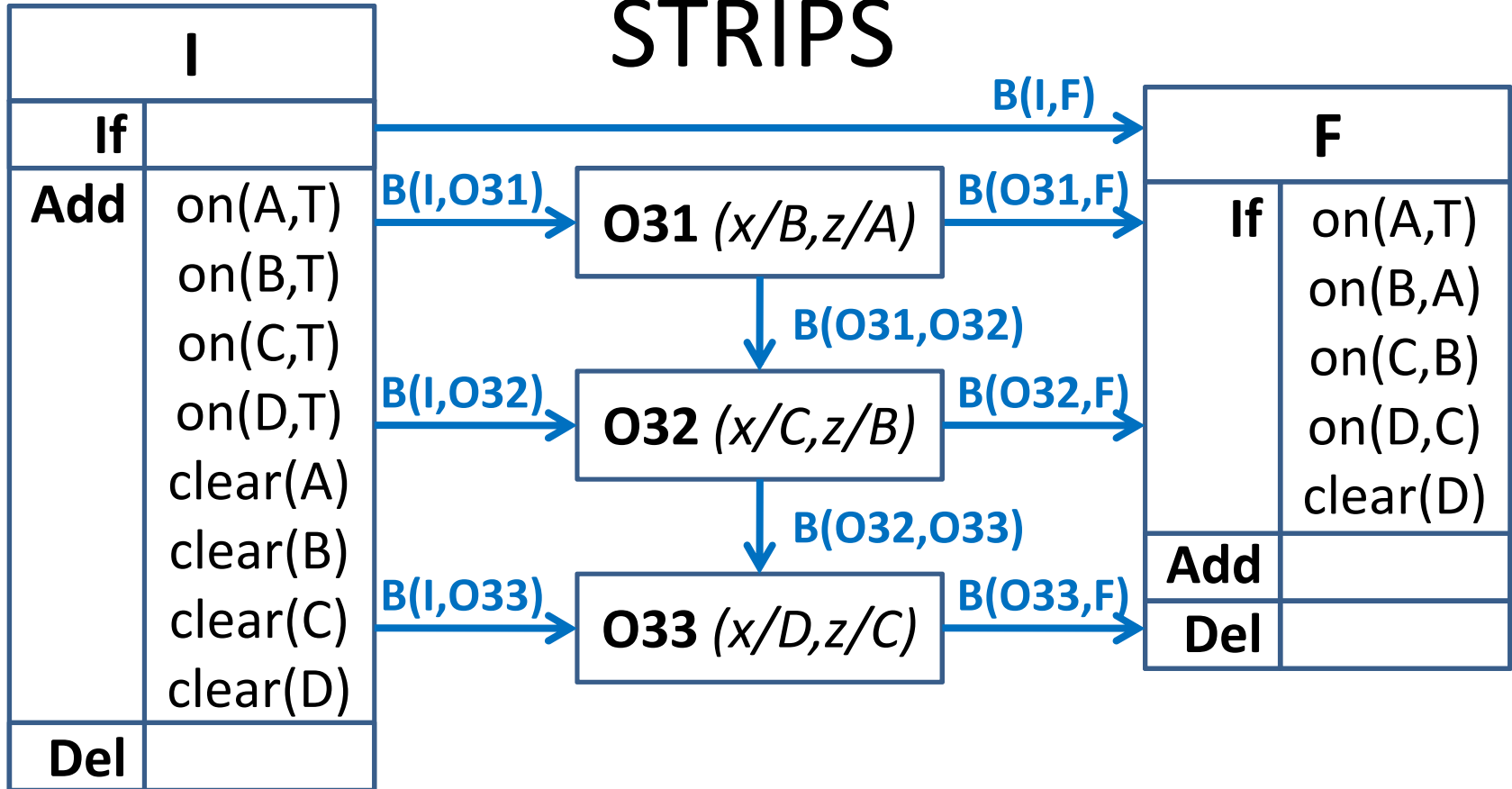
Before constraint:

$B(x, y)$



**Are the before constraints satisfiable?**

# STRIPS



Are the before constraints satisfiable?

**YES:**

→ **O31** → **O32** → **O33** →

# Exercises: Artificial Intelligence

Planning & Logic: Buying milk

Planning & Logic: Buying milk

# **PROBLEM**

# Problem

- **Apply STRIPS** on:
  - **Initial State, I:**
    - at(home)
  - **Final State, F:**
    - have(milk), at(home)
- **Indicate:** *Establish & Threaten*
- **Give:** *Before relation without loops (check!)*
- **Give:** *Possible linearisations*

Planning & Logic: Blocks world

# **INITIAL & FINAL STATE**

# Initial & Final State as Operator

<b>I</b>	
<b>If</b>	
<b>Add</b>	at(home)
<b>Del</b>	

<b>F</b>	
<b>If</b>	at(home) have(milk)
<b>Add</b>	
<b>Del</b>	

Planning & Logic: Blocks world

# **OPERATORS**

# Operators

Operator 1		Operator 2		Operator 3	
<b>If</b>	at(home)	<b>If</b>	at(home)	<b>If</b>	at(shop)
<b>Add</b>	have(money)	<b>Add</b>	at(shop)	<b>Add</b>	have(milk)
<b>Del</b>		<b>Del</b>	at(home)	<b>Del</b>	

Operator 4		Operator 5	
<b>If</b>	at(shop) paid	<b>If</b>	at(shop) have(money) have(milk)
<b>Add</b>	at(home)	<b>Add</b>	paid
<b>Del</b>	at(shop)	<b>Del</b>	have(money)

Planning & Logic: Blocks world

# **STRIPS**

# STRIPS

I	If	
	Add	at(home)
	Del	



Establishes



Threatens

Before constraint:

$B(x,y)$

F	
If	have(milk) at(home)
Add	
Del	

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 3	
If	at(shop)
Add	have(milk)
Del	

B(O3,F)

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

B(O2,O3)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

B(O3,F)

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

B(I,O2)

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

B(O2,O3)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

B(O3,F)

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

	If	
I	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

F	
If	have(milk) at(home)
Add	
Del	

$B(I,O2)$

$B(O2,O3)$

$B(I,F)$

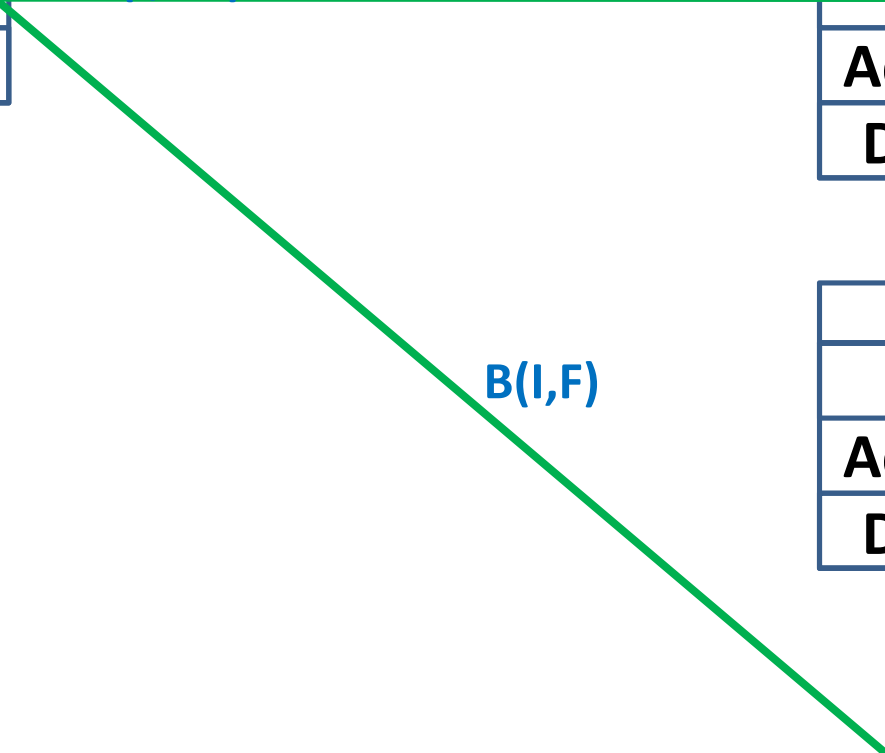
$B(O3,F)$

Establishes

Threatens

Before constraint:

$B(x,y)$



# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del	→	at(home)

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

F		
If	→	have(milk) at(home)
Add		
Del		

$B(I, O2)$

$B(O2, I) \vee B(F, O2)$

$B(I, F)$

$B(O2, O3)$

$B(O3, F)$



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del	...	at(home)

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

F		
If	→	have(milk) at(home)
Add		
Del		

$B(I,O2)$

$B(O2,I) \vee B(F,O2)$

2 x Loop!

$B(I,F)$

$B(O2,O3)$

$B(O3,F)$



Establishes



Threatens

Before constraint:

$B(x,y)$

# STRIPS

$B(I, O2)$

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

$B(I, O2)$

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

Operator 4	
If	paid at(shop)
Add	at(home)
Del	at(shop)

$B(O4, F)$

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

	If	
I	Add	at(home)
	Del	

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

Operator 4		
If	paid at(shop)	
Add	at(home)	
Del	at(shop)	

F		
If	have(milk) at(home)	
Add		
Del		

$B(I,O2)$

$B(O2,O3)$

$B(O2,O4) \vee B(F,O2)$

$B(O3,F)$

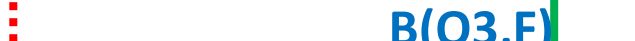
$B(O4,F)$

Establishes

Threatens

Before constraint:

$B(x,y)$



# STRIPS

	If	
I	Add	at(home)
	Del	

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

Operator 4		
If	paid at(shop)	
Add	at(home)	
Del	at(shop)	

F		
If	have(milk) at(home)	
Add		
Del		

$B(I,O2)$

$B(O2,O3)$

$B(O2,O4) \vee B(F,O2)$

$B(O3,F)$

$B(O4,F)$

Establishes

Threatens

Before constraint:

$B(x,y)$



# STRIPS

	If	
I	Add	at(home)
	Del	

$B(I,O2)$

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

$B(O2,O3)$

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

$B(O2,O4)$

$B(O3,F)$

Operator 4		
If	paid at(shop)	
Add	at(home)	
Del	at(shop)	

$B(O4,F)$

F		
If	have(milk) at(home)	
Add		
Del		



Establishes



Threatens

Before constraint:

$B(x,y)$

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

Operator 4		
If	paid at(shop)	
Add	at(home)	
Del	at(shop)	

F		
If	have(milk) at(home)	
Add		
Del		

$B(I, O2)$

$B(O4, O2) \vee B(O3, O4)$

$B(O2, O3)$

$B(O2, O4)$

$B(O3, F)$

$B(O4, F)$



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)

Operator 3		
If		← at(shop)
Add		have(milk)
Del		

Operator 4		
If		paid
		at(shop)
Add		at(home)
Del		at(shop)

F		
If	→	have(milk)
		← at(home)
Add		
Del		

$B(I, O2)$

$B(O4, O2) \vee B(O3, O4)$

$B(O2, O3)$

$B(O2, O4)$

$B(O3, F)$

$B(O4, F)$



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

Operator 4		
If		paid at(shop)
Add		at(home)
Del		at(shop)

F		
If		have(milk) at(home)
Add		
Del		

$B(I,O2)$

$B(O2,O3)$

$B(O3,O4)$

$B(O2,O4)$

$B(O3,F)$

$B(O4,F)$

Establishes

Threatens

Before constraint:

$B(x,y)$



# STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)

$B(O2, O3)$

Operator 5		
If		at(shop) have(money) have(milk)
Add		paid
Del		have(money)

$B(O5, O4)$

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

$B(O2, O4)$

$B(O3, F)$

Operator 4		
If		paid at(shop)
Add		at(home)
Del		at(shop)

$B(O4, F)$

F		
If		have(milk) at(home)
Add		
Del		



Establishes



Threatens

Before constraint:

$B(x, y)$

# STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add	→	at(shop)
Del		at(home)

B(O2,05)

Operator 5		
If	→	at(shop)
		have(money)
		have(milk)
Add		paid
Del		have(money)

B(O2,03)

Operator 3		
If		at(shop)←
Add		have(milk)
Del		

B(O3,04)

B(O2,04)

B(O3,F)

Operator 4		
If		paid
		at(shop)
Add		at(home)
Del		at(shop)

B(O4,F)

F		
If		have(milk)
		at(home)
Add		
Del		



Establishes



Threatens

Before constraint:

B(x,y)

# STRIPS

	If	
I	Add	at(home)
	Del	



Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

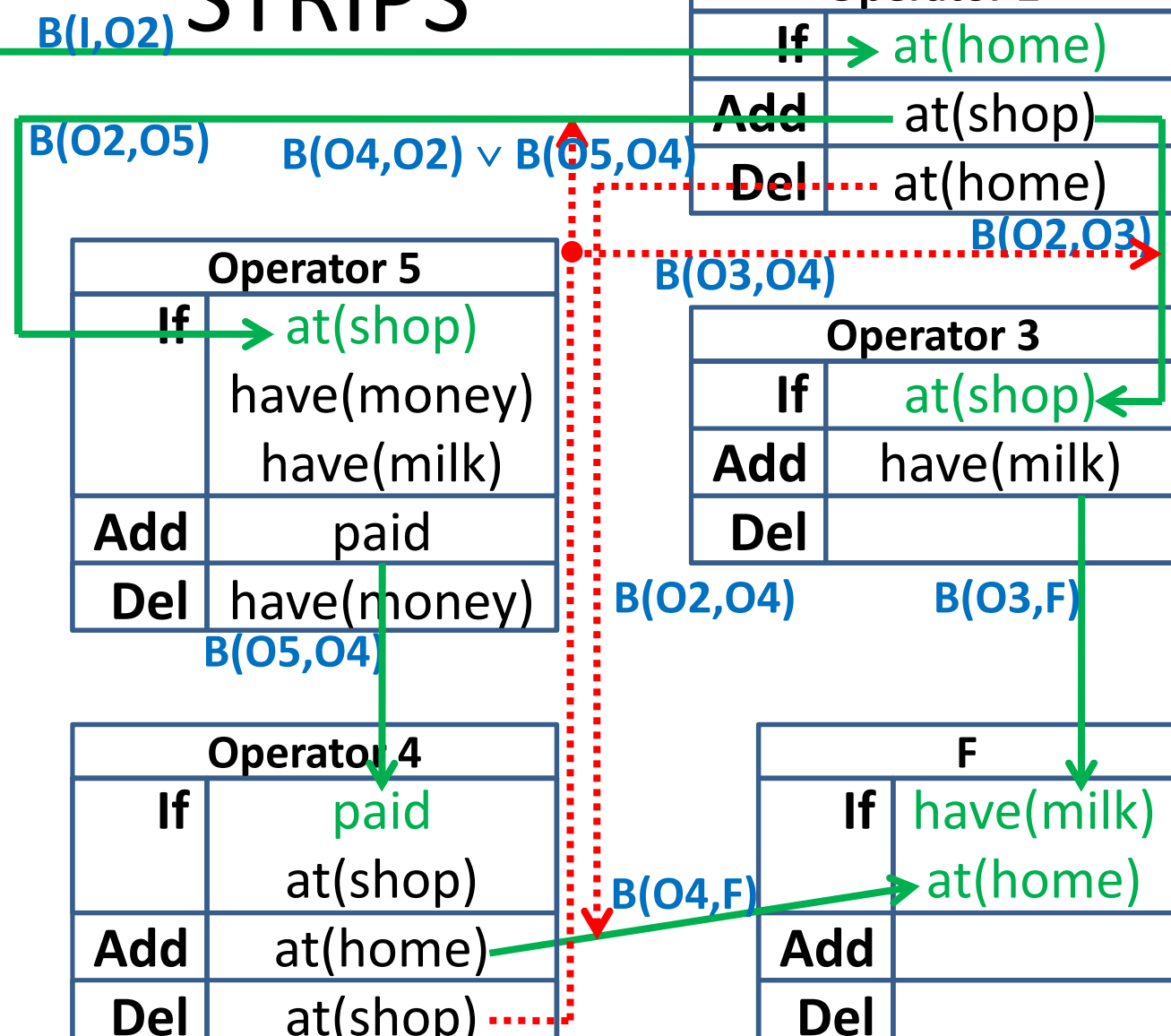
Operator 5	
If	at(shop) have(money) have(milk)
Add	paid
Del	have(money)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

Operator 4	
If	paid at(shop)
Add	at(home)
Del	at(shop)

F	
If	have(milk) at(home)
Add	
Del	

 Establishes  
 Threatens  
 Before constraint:  
 $B(x,y)$



# STRIPS

	If	
I	Add	at(home)
	Del	

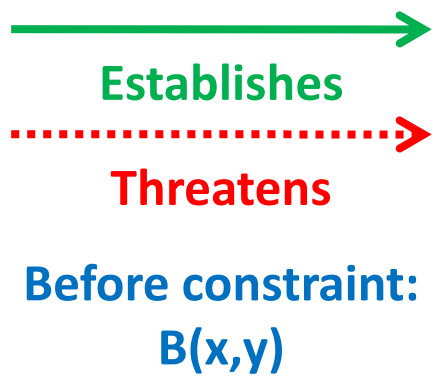
Operator 2	
If	→ at(home)
Add	→ at(shop)
Del	→ at(home)

Operator 5	
If	→ at(shop)
	have(money)
	have(milk)
Add	paid
Del	have(money)

Operator 3	
If	← at(shop)
Add	have(milk)
Del	

Operator 4	
If	← paid
	at(shop)
Add	at(home)
Del	at(shop)

F	
If	← have(milk)
	at(home)
Add	
Del	



$B(I,O2)$

$B(O2,O5)$

$B(O4,O2) \vee B(O5,O4)$

$B(O2,O3)$

$B(O3,O4)$

$B(O5,O4)$

$B(O2,O4)$

$B(O3,F)$

$B(O4,F)$

# STRIPS

	If	
I	Add	at(home)
	Del	

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

Operator 5		
If	→ at(shop)	
	have(money)	
	have(milk)	
Add	paid	
Del	have(money)	

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

Operator 4		
If	paid	
	at(shop)	
Add	at(home)	
Del	at(shop)	

F		
If	have(milk)	
	at(home)	
Add		
Del		



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,O2)$

$B(O2,O5)$

$B(O5,O4)$

$B(O3,O4)$

$B(O2,O3)$

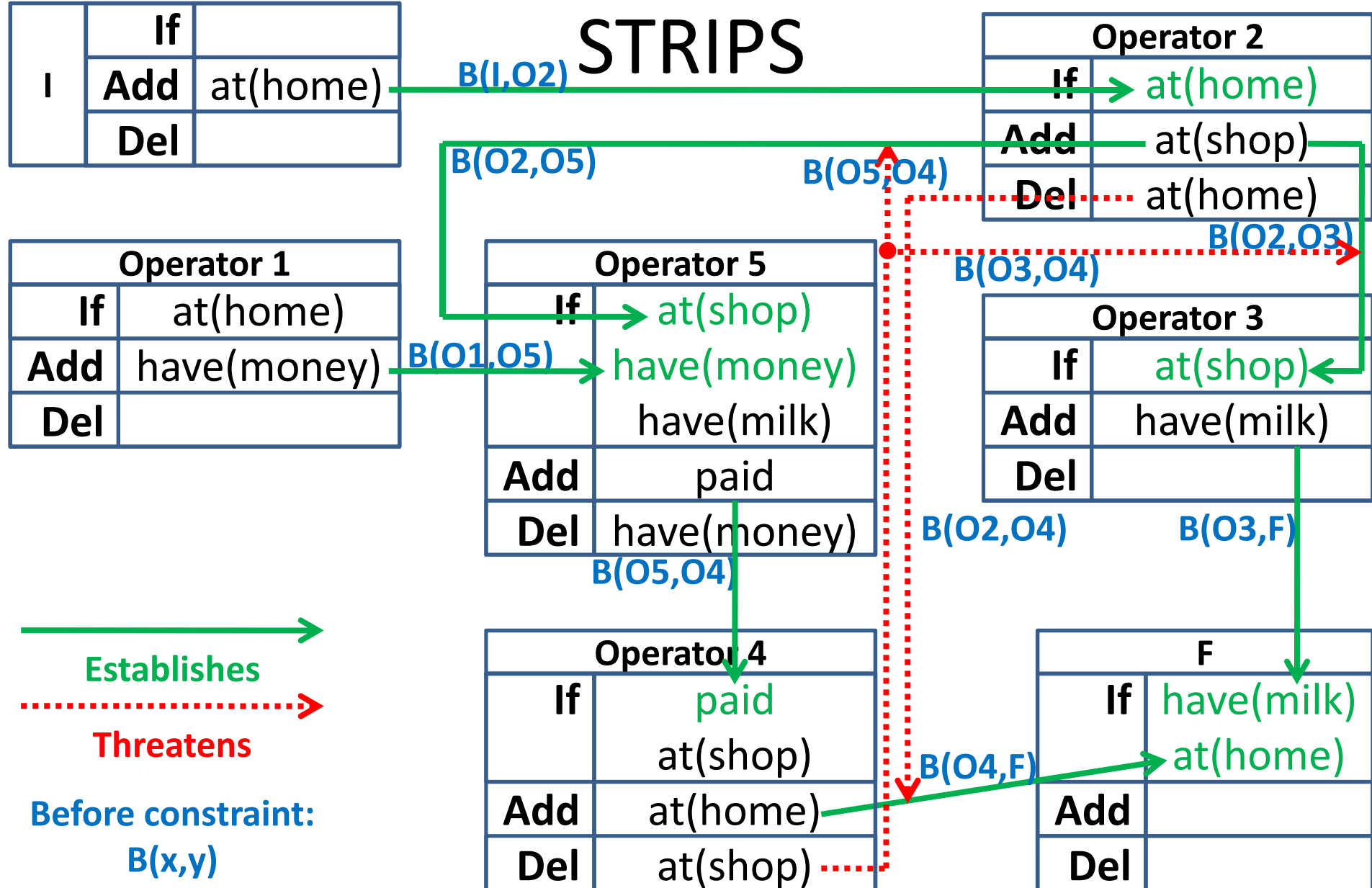
$B(O5,O4)$

$B(O2,O4)$

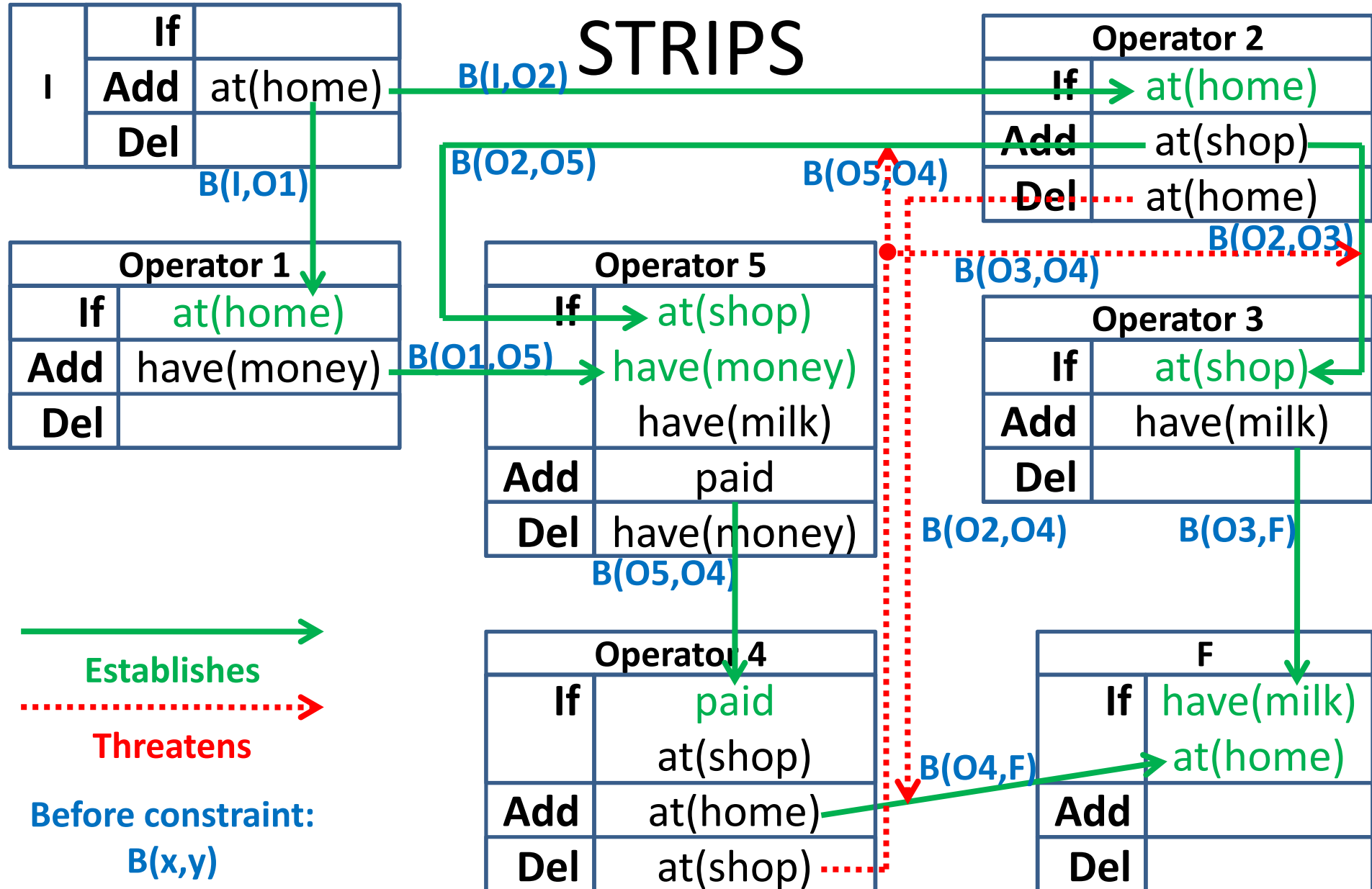
$B(O3,F)$

$B(O4,F)$

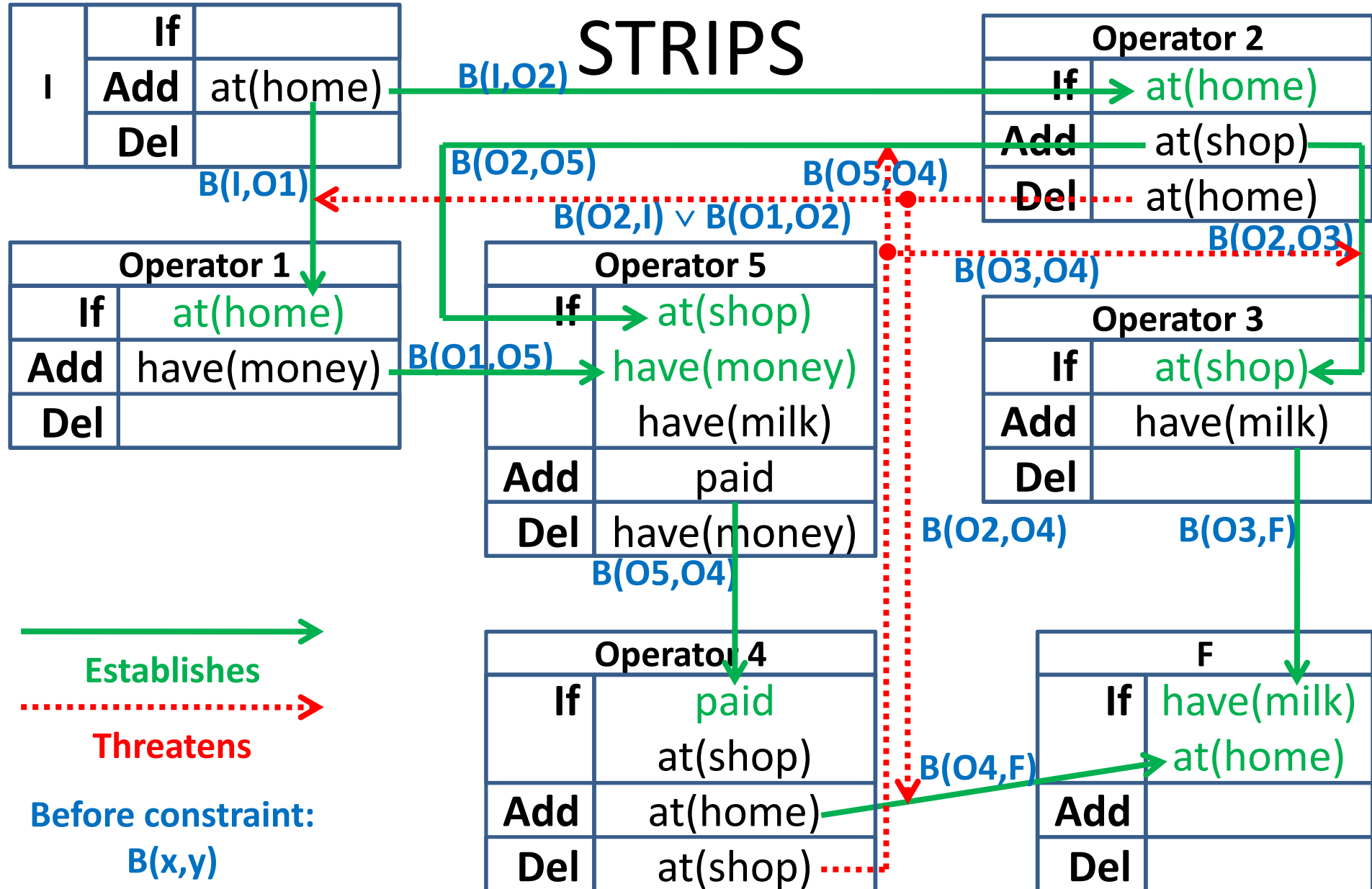
# STRIPS



# STRIPS

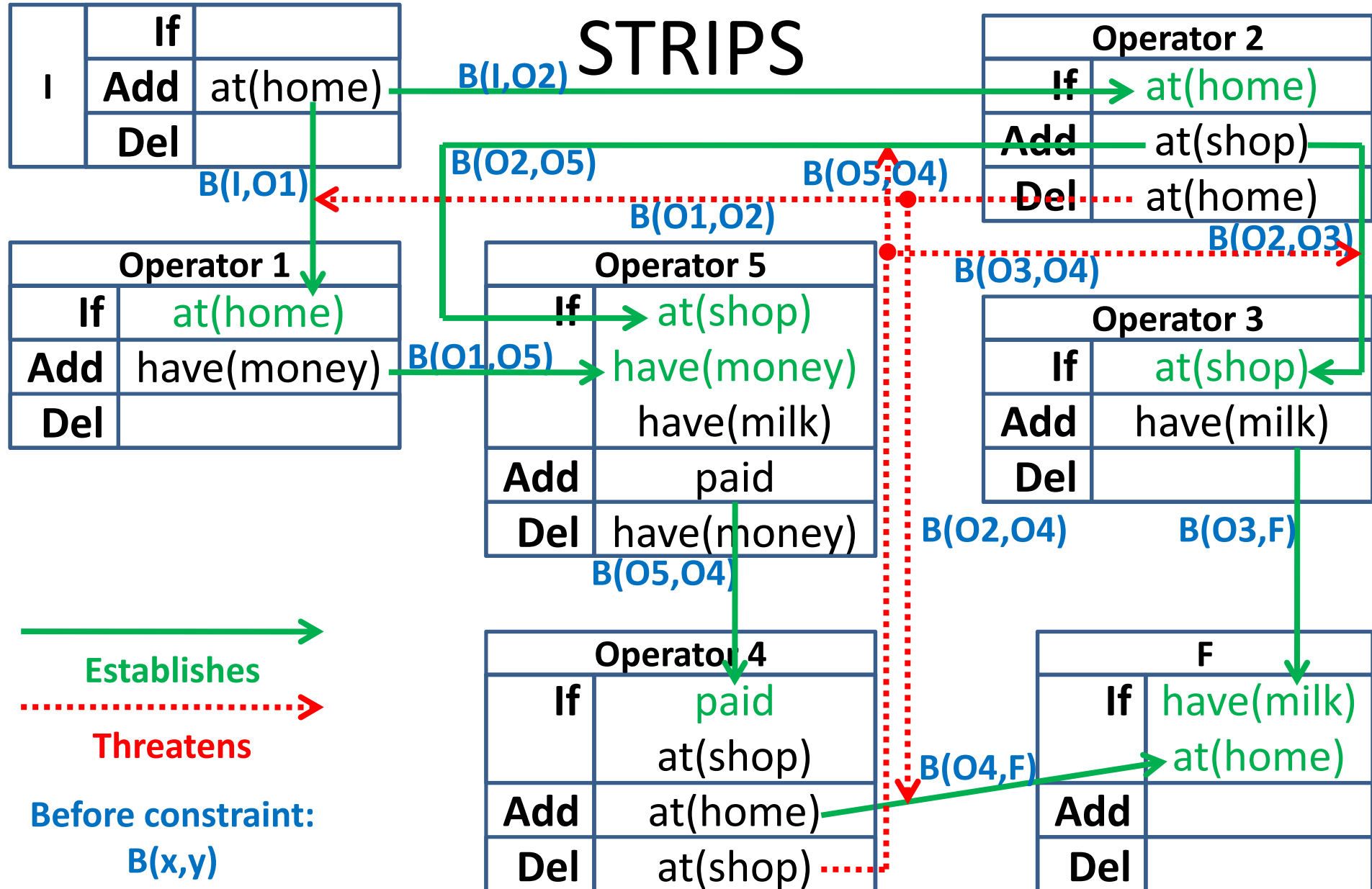


# STRIPS

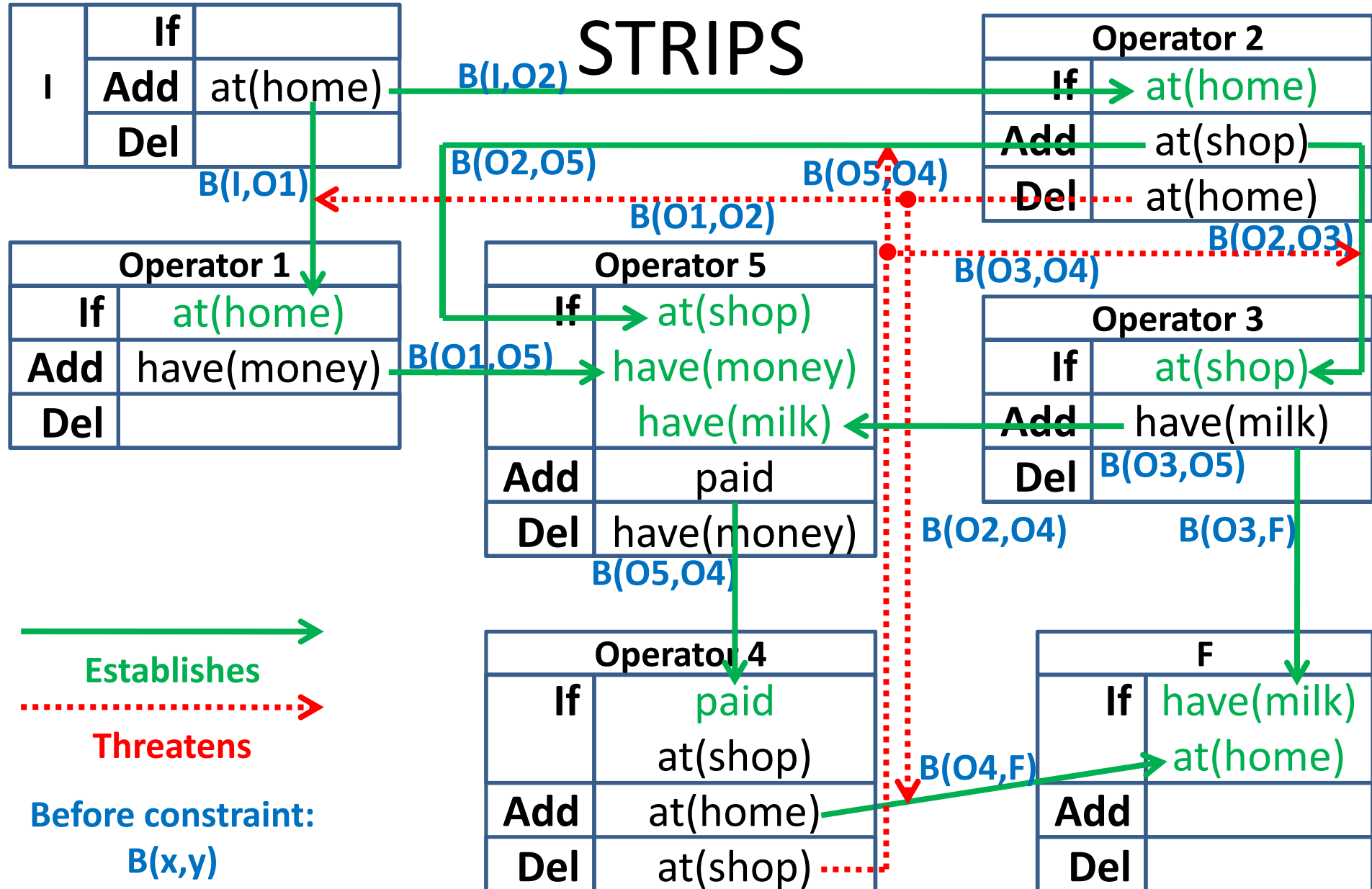




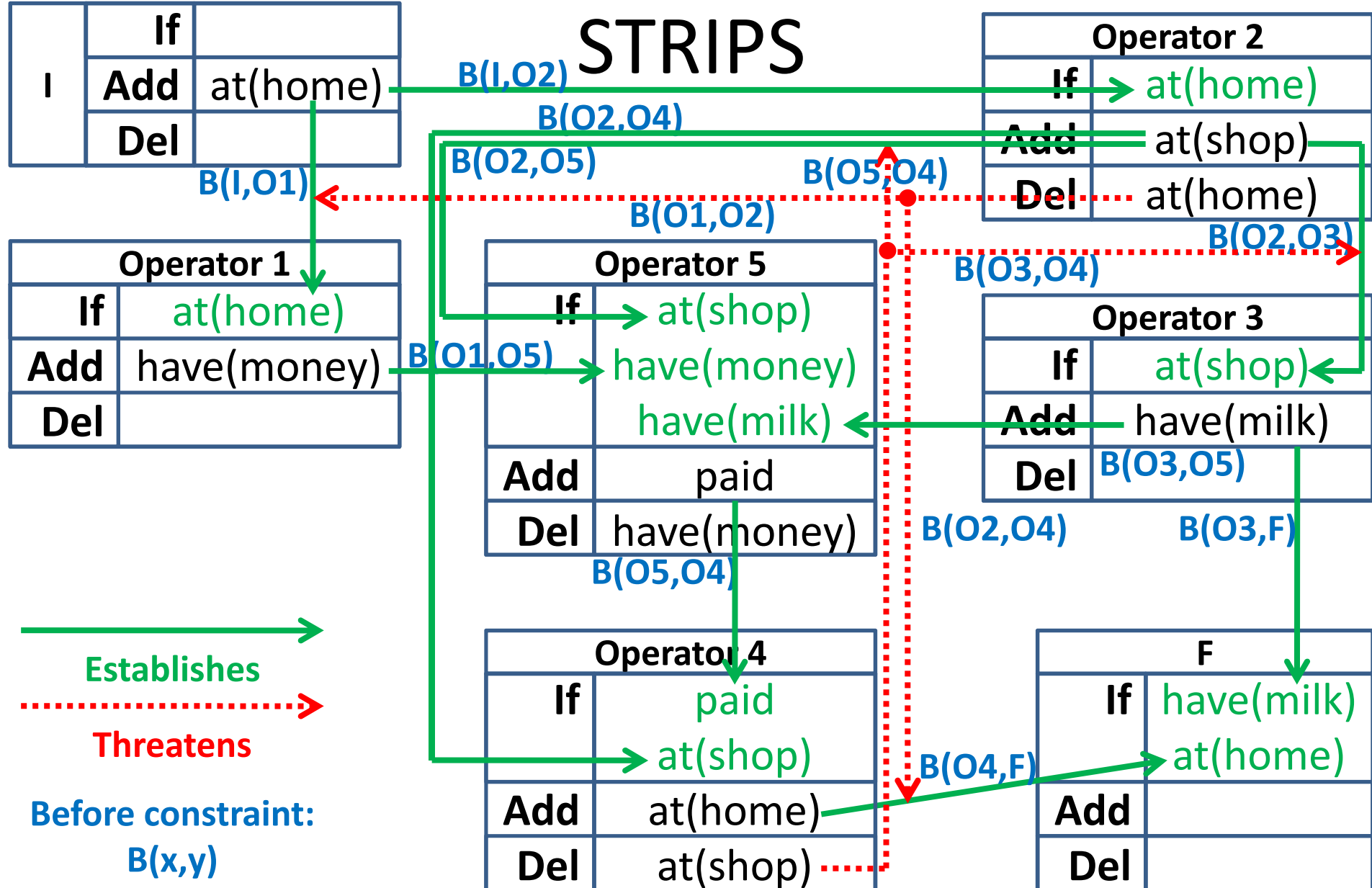
# STRIPS



# STRIPS



# STRIPS

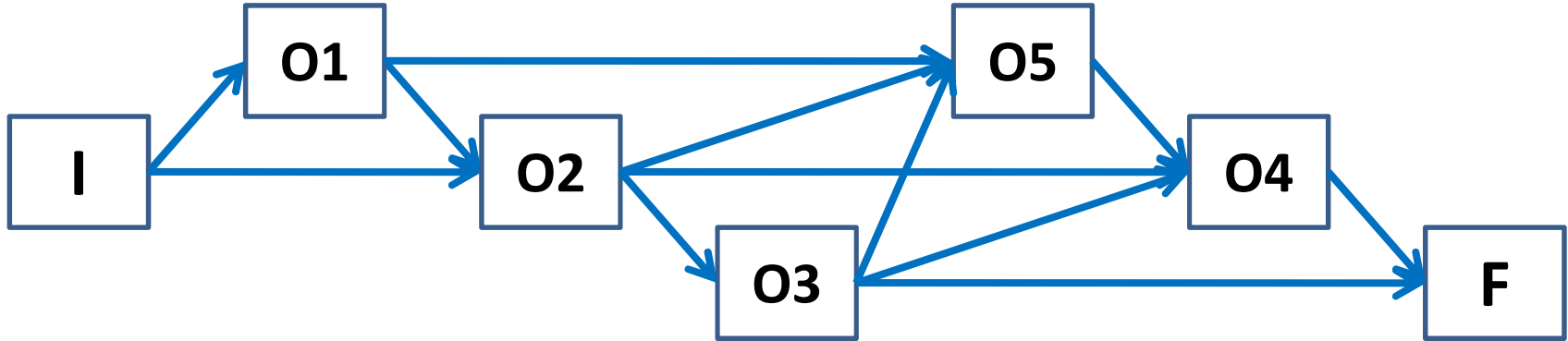


# STRIPS

B(I,O1)	B(O2,O5)
B(I,O2)	B(O3,O4)
B(O1,O2)	B(O3,O5)
B(O1,O5)	B(O3,F)
B(O2,O3)	B(O4,F)
B(O2,O4)	B(O5,O4)

**Are the before constraints satisfiable?**

# STRIPS



**Are the before constraints satisfiable?**

**YES:**

**→ O1 → O2 → O3 → O5 → O4 →**

# Exercises: Artificial Intelligence

Planning & Logic: English to Logic

Planning & Logic: English to Logic

# **PROBLEM & SOLUTION**

# Problem & Solution

- *Not all students take both history and biology*

# Problem & Solution

- *Not all students take both history and biology*
  - ¬  $\forall x$  [student(x)  $\Rightarrow$  takes(x,hist)  $\wedge$  takes(x,bio)]

# Problem & Solution

- *Not all students take both history and biology*
  - $\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$
  - $\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$
  - $\neg \forall x [\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$

# Problem & Solution

- *Not all students take both history and biology*

$$\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\neg \forall x [\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg \forall x (F) \Leftrightarrow \exists x (\neg F)]$$

$$\exists x \neg[\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

# Problem & Solution

- *Not all students take both history and biology*

$$\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\neg \forall x [\neg [\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg \forall x (F) \Leftrightarrow \exists x (\neg F)]$$

$$\exists x \neg [\neg [\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg(A \vee B) \Leftrightarrow \neg A \wedge \neg B], [\neg(A \wedge B) \Leftrightarrow \neg A \vee \neg B]$$

$$\exists x [\text{student}(x) \wedge [\neg \text{takes}(x, \text{hist}) \vee \neg \text{takes}(x, \text{bio})]]$$

# Problem & Solution

- *No person likes a smart vegetarian*

# Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

# Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

# Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [\neg A \vee \neg B \Leftrightarrow \neg(A \wedge B)]$$

$$\forall x \forall y \neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

# Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [\neg A \vee \neg B \Leftrightarrow \neg(A \wedge B)]$$

$$\forall x \forall y \neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

$$\Leftrightarrow [\forall x \neg(F) \Leftrightarrow \neg \exists x (F)]$$

$$\neg \exists x \exists y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

# Problem & Solution

- *There is a woman who likes all men who are not vegetarians.*

# Problem & Solution

- *There is a woman who likes all men who are not vegetarians.*

$$\exists x[\text{woman}(x) \wedge [\forall y [\text{man}(y) \wedge \neg \text{vegetarian}(y) \Rightarrow \text{likes}(x,y)]]]$$

# Problem & Solution

- *The best score in history was better than the best score in biology.*

# Problem & Solution

- *The best score in history was better than the best score in biology.*

$\forall x \forall y [\text{bestscore}(\text{hist},x) \wedge \text{bestscore}(\text{bio},y) \Rightarrow \text{better}(x,y)]$

# Problem & Solution

- *Every person who dislikes all vegetarians is smart.*

# Problem & Solution

- *Every person who dislikes all vegetarians is smart.*

$$\forall x [ \text{person}(x) \wedge [ \forall y [ \text{vegetarian}(y) \Rightarrow \neg \text{likes}(x,y) ] ] \Rightarrow \text{smart}(x) ]$$

# Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

# Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

# Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

# Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\forall y \neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

# Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\forall y \neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

$\Leftrightarrow$

$$\exists x [\text{barber}(x) \wedge [\neg \exists y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y \neg [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)]$$

# Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y \neg [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)] \Leftrightarrow$$

$$\neg \exists x \exists y [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)]$$

# Problem & Solution

- *Only one person failed both history and biology.*

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- *Only one person failed both history and biology.*

$\exists!x \text{ student}(x) \wedge \text{failed}(x, \text{hist}) \wedge \text{failed}(x, \text{bio})$

# Problem & Solution

- *Only one person failed both history and biology.*

$$\exists!x \text{ student}(x) \wedge \text{failed}(x, \text{hist}) \wedge \text{failed}(x, \text{bio})$$

**Note that:**  $\exists!x p(x) \Leftrightarrow \exists x p(x) \wedge [\forall y [p(y) \Rightarrow x=y]]$

# Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but they can't fool all the people all of the time.*

# Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but they can't fool all the people all of the time.*

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

# Problem & Solution

- *Politicians can fool some of the people all the time, and **they can fool all of the people some of the time**, but they can't fool all the people all of the time.*

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow [\exists t \text{ time}(t) \wedge [\forall y \text{ people}(y) \Rightarrow \text{fool}(x,y,t)]]]$

# Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but **they can't fool all the people all of the time.***

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow [\exists t \text{ time}(t) \wedge [\forall y \text{ people}(y) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow \neg[\forall y \forall t [\text{people}(y) \wedge \text{time}(t)] \Rightarrow \text{fool}(x,y,t)]]]$

# Exercises: Artificial Intelligence

Planning & Logic: And-Or-If

Planning & Logic: And-Or-If

# **PROBLEM & SOLUTION**

# Problem & Solution

- *One more outburst like that and you are in contempt of court.*

# Problem & Solution

- *One more outburst like that and you are in contempt of court.*

outburst  $\Rightarrow$  court

# Problem & Solution

- *One more outburst like that and you are in contempt of court.*

outburst  $\Rightarrow$  court

**NOT:** outburst  $\wedge$  court

# Problem & Solution

- *Either the Red Sox win or I'm out ten dollars.*

# Problem & Solution

- *Either the Red Sox win or I'm out ten dollars.*

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# Exercises: Artificial Intelligence

Planning & Logic: Weird Logic

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# **PROBLEM & SOLUTION**

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